FIT3155: Week 8 tutorial Covering concepts from Weeks 5-7

Objectives: The tutorials, in general, give practice in problem solving, in analysis of algorithms and data-structures, and in logic useful in the above.

Instructions to the class: Prepare your answers to the questions **before** the tutorial. It will probably not be possible to cover all questions unless the class has prepared them all in advance.

Instructions to Tutors:

- i. The purpose of the tutorials is not to solve the practical exercises.
- ii. The purpose is to check answers, and to discuss particular sticking points, not to simply make answers available.
- 1. Write pseudocode to compute which (order) binomial trees form a binomial heap for any given n elements.
- 2. Using mathematical induction, for a binomial tree B_k of order k, prove that:
 - (a) B_k contains 2^k nodes.
 - (b) B_k has a height k.

Binomial heap H_1

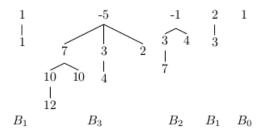
- (c) B_k has exactly k-choose-d nodes at each depth $0 \le d \le k$.
- 3. Insert the following elements in a binomial heap:

4. Insert the following elements in a binomial heap:

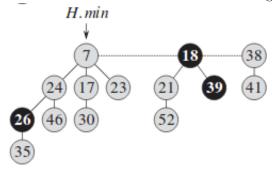
5. Perform merge on the following two binomial heaps:

Binomial heap H_2

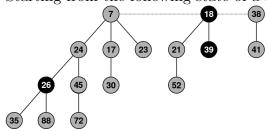
6. Perform merge followed by extract-min on the following (improper state of) binomial heap:



- 7. Show that the amortized complexity to insert n elements into a binomial heap is O(n).
- 8. Perform extract-min on the following Fibonacci heap:



9. Starting from the following state of a Fibonacci heap:



Run the following sequence of operations, and after each step, draw the resultant heap:

- (a) decrease-key of 45 to 40.
- (b) decrease-key of $40\ \mathrm{to}\ 12.$
- $\left(c\right)$ decrease-key of 35 to 1.
- (d) extract-min.