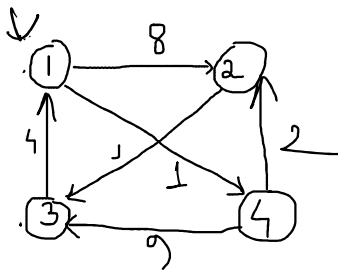


Matrix use

$N+1$ matrix = $4+1=5$.

Dimension $\rightarrow N \times N$.

Src	Dest
✓ 1	2, 3, 4
✓ 2	1, 3, 4
✓ 3	1, 2, 4
✓ 4	1, 2, 3



$D_0 =$

	1	2	3	4
1	0	8	∞	1
2	∞	0	1	∞
3	4	∞	0	∞
4	∞	2	9	0

(2, 3)

$D_0 =$

	1	2	3	4
1	0	8	∞	1
2	∞	0	1	∞
3	4	∞	0	∞
4	∞	2	9	0

$D_1 =$

	1	2	3	4
1	0	8	∞	1
2	∞	0	1	∞
3	4	12	0	5
4	∞	2	9	0

$D(2 \text{ to } 3)$
 via 1
 $= D(2 \text{ to } 1) + D(1 \text{ to } 3)$
 $= \infty$

$D(2 \text{ to } 4)$
 via 1
 $= D(2 \text{ to } 1) + D(1 \text{ to } 4)$

$3-2 = 3-1 + 1-2$
 $= 4 + 8 = 12$

$3-4 = 3-1 + 1-4$
 $= 4 + 1 = 5$

$4-2 = 4-1 + 1-2$
 $= \infty$

$4-3 = 4-1 + 1-3 = \infty$

$D_1 =$

	1	2	3	4
1	0	8	∞	1
2	∞	0	1	∞
3	4	12	0	5
4	∞	2	9	0

$D_2 =$

	1	2	3	4
1	0	8	9	1
2	∞	0	1	∞
3	4	12	0	5
4	∞	2	9	0

$1-3 = 1-2 + 2-3$
 $= 8 + 1$
 $= 9$

$1-4 = 1-2 + 2-4$
 $= 8 + \infty$

$$\begin{matrix} 3 \\ 4 \end{matrix} \begin{bmatrix} 4 & 12 & 0 & 5 \\ \infty & 2 & 9 & 0 \end{bmatrix}$$

$$\begin{aligned} 3-4 &= 3-2 + 2-4 \\ &= 12 + \infty = \infty \end{aligned}$$

$$\begin{matrix} 3 \\ 4 \end{matrix} \begin{bmatrix} 4 & 12 & 0 & 5 \\ \infty & 2 & 3 & 0 \end{bmatrix}$$

$$\begin{aligned} 4-1 &= 4-2 + 2-1 \\ &= 2 + \infty \\ &= \infty \end{aligned} \quad \left| \quad \begin{aligned} 4-3 &= 4-2 + 2-3 \\ &= 2 + \infty \\ &= \infty \end{aligned} \right.$$

$$\begin{aligned} 1-4 &= 1-2 + 2-4 \\ &= 8 + \infty \\ &= \infty \end{aligned}$$

$$\begin{aligned} 3-1 &= 3-2 + 2-1 \\ &= 12 + \infty \\ &= \infty \end{aligned}$$

$$D_2 = \begin{matrix} & 1 & 2 & 3 & 4 \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 8 & 9 & 1 \\ \infty & 0 & 1 & \infty \\ 4 & 12 & 0 & 5 \\ \infty & 2 & 3 & 0 \end{bmatrix} \end{matrix}$$

$$D_3 = \begin{matrix} & 1 & 2 & 3 & 4 \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 8 & 9 & 1 \\ 5 & 0 & 1 & 6 \\ 4 & 12 & 0 & 5 \\ 7 & 2 & 3 & 0 \end{bmatrix} \end{matrix}$$

$$1-2 = 1-3 + 3-2 = 9 + 12 = 21 \quad 1-4 = 1-3 + 3-4 = 9 + 5 = 14$$

$$2-1 = 2-3 + 3-1 = 1 + 4 = 5 \quad 2-4 = 2-3 + 3-4 = 1 + 5 = 6$$

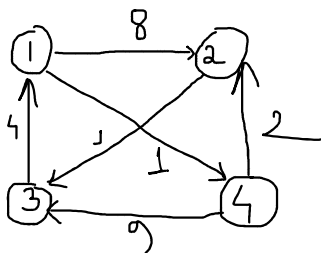
$$4-1 = 4-3 + 3-1 = 3 + 4 = 7 \quad 4-2 = 4-3 + 3-2 = 3 + 12 = 15$$

$$D_3 = \begin{matrix} & 1 & 2 & 3 & 4 \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 8 & 9 & 1 \\ 5 & 0 & 1 & 6 \\ 4 & 12 & 0 & 5 \\ 7 & 2 & 3 & 0 \end{bmatrix} \end{matrix}$$

$$D_4 = \begin{matrix} & 1 & 2 & 3 & 4 \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & 4 & 1 \\ 5 & 0 & 1 & 6 \\ 4 & 7 & 0 & 5 \\ 7 & 2 & 3 & 0 \end{bmatrix} \end{matrix}$$

$$\begin{aligned} 1-2 &= 1-4 + 4-2 = 1 + 2 = 3 \\ 2-1 &= 2-4 + 4-1 = 6 + 7 = 13 \\ 3-1 &= 3-4 + 4-1 = 5 + 7 = 12 \end{aligned}$$

$$\begin{aligned} 1-3 &= 1-4 + 4-3 = 1 + 3 = 4 \\ 2-3 &= 2-4 + 4-3 = 6 + 3 = 9 \\ 3-2 &= 3-4 + 4-2 = 5 + 2 = 7 \end{aligned}$$



$$D_4 = \begin{matrix} & 1 & 2 & 3 & 4 \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & 4 & 1 \\ 5 & 0 & 1 & 6 \\ 4 & 7 & 0 & 5 \\ 7 & 2 & 3 & 0 \end{bmatrix} \end{matrix}$$