

**Graph Data Structure** is a collection of **nodes**. Nodes are connected by **edges**. Edges represent connection between nodes.

**Directed graph:** You can go from node A to B, but not B to A. Arrow will be present.

**Undirected graph:** You can go from B to A and also from A to B. Arrow is absent.

## Graphs Traversal

To traverse a Graph means to start in one vertex, and go along the edges to visit other vertices until all vertices, or as many as possible, have been visited.

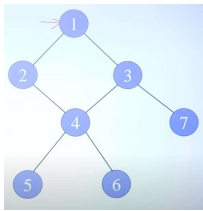
2 techniques: BFS (Breadth first search), DFS (depth first search)

BFS is a graph traversal algorithm that explores all the neighbours of a node before moving on to their neighbours.

DFS is a graph traversal algorithm that explores as far as possible along each branch before backtracking.



A to B, B to A

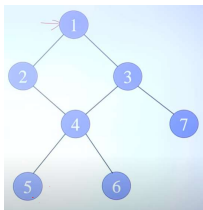
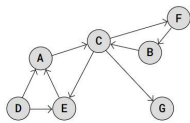
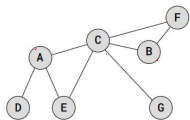


### BFS Algorithm

1. Push the starting node into the queue and mark it as visited.
2. While the queue is not empty, repeat:
  - Remove an element (node) from the front of the queue.
  - Process the node (if required). *Print it*
  - Push all its unvisited neighboring nodes into the queue and mark them as visited.

### Iterative DFS Algorithm (Using a Stack)

1. Push start element in stack, mark it visited and print it.
2. Repeat till stack is not empty:
  - a. See the top element in stack.
  - b. If all its neighbours have been visited, remove the top item from stack.
  - c. Else push one of its unvisited neighbours, print it, mark it as visited and continue the process.



BFS Traversal:-

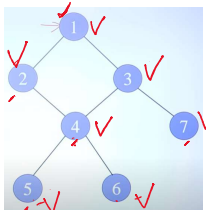
Traversal start from node 1.

1 2 3 4 7 5 6

3 1 4 7 2 5 6

3 7 4 1  
4 7 1

Start traversal from node 3.

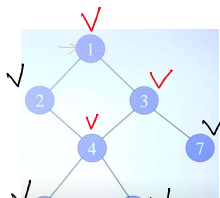


Queue:- ~~3 1 4 7 2 5 6~~

Print:- 3 1 4 7 2 5 6

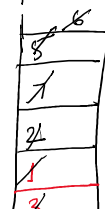
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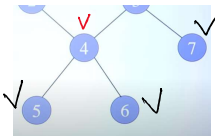
LIFO → top = ~~1 3 4 7 2 5 6~~



### Iterative DFS Algorithm (Using a Stack)

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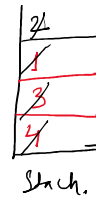




- a. See the top element in stack.
- b. If all its neighbours have been visited, remove the top item from stack.
- c. Else push one of its unvisited neighbours, print it, mark it as visited and continue the process.

DFS traversal start from node 4.

Print:- 4, 3, 1, 2, 7, 5, 6

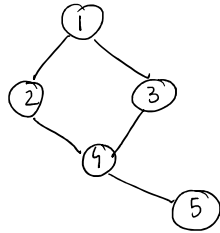


DFS traversal from node 1.

H/W, Perform BFS from node 5, 7, 2.  
Perform DFS from node 1, 7, 3.

Representation of Graph:-

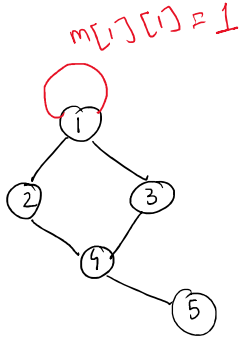
- ① Adjacency Matrix
- ② Adjacency List



	1	2	3	4	5
1					
2					
3					
4					
5					

① Adjacency Matrix -  $N = \text{No of nodes}$   
 $= 5$

Adjacency matrix dimension  
 $N \times N = 5 \times 5$ .



$$m[i][j] = 1$$

	1	2	3	4	5
1	0	1	1	0	0
2	1	0	0	1	0
3	1	0	0	1	0
4	0	1	1	0	1
5	0	0	0	1	0

$m[i][j] = 0$ , No edge from node  $i$  to  $j$ .  
 $1$ , Edge from node  $i$  to  $j$ .

$i=j$ ,  $m[i][j] = 0$ .

Matrix  $M$ .



$m[1][2] = 1$   
 $m[2][1] = 1$

	1	2
1	0	1
2	0	0

Adj Mat.



Adjacency List - List of List

