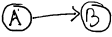



**Graph Data Structure** is a collection of **nodes**. Nodes are connected by **edges**. Edges represent connection between nodes.

Directed graph:  You can go from node A to B, but not B to A. Arrow will be present.

Undirected graph:  You can go from B to A and also from B to A. Arrow is absent.

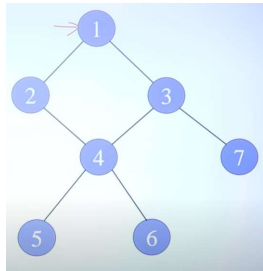
## Graphs Traversal

To traverse a Graph means to visit each and every node of graph only once.

2 techniques: BFS (Breadth first search), DFS (depth first search)

BFS is a graph traversal algorithm that explores all the neighbours of a node before moving on to their neighbours.

DFS is a graph traversal algorithm that explores as far as possible along each branch before backtracking.

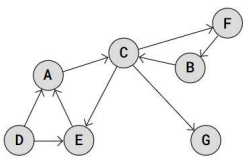
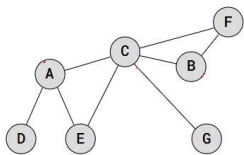


### BFS Algorithm

1. Push the starting node into the queue and mark it as visited.
2. While the queue is not empty, repeat:
  - Remove an element (node) from the front of the queue.
  - Process the node (if required). *Print it*
  - Push all its unvisited neighboring nodes into the queue and mark them as visited.

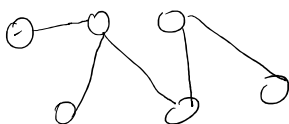
### Iterative DFS Algorithm (Using a Stack)

1. Push start element in stack and print it.
2. Repeat till stack is not empty:
  - a. See the top element in stack.
  - b. If all its neighbours have been visited, remove the top item from stack.
  - c. Else push one of its unvisited neighbours and continue the process.



Graph-

- Non-linear Data structure.
- finite number of vertices/nodes.
  - Nodes — Connectors — Edges.



Types-

① Directed



② Undirected.



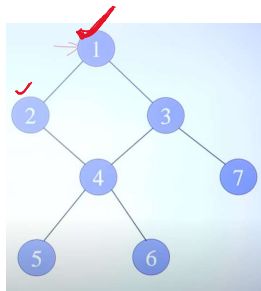
Representation of Graph-

① Adjacency Matrix

② Adjacency List.

$n$  = Number of nodes in your graph.

## ① Adjacency Matrix



## ② Adjacency List

$n$  = Number of nodes in your graph.

$n = 7$ .

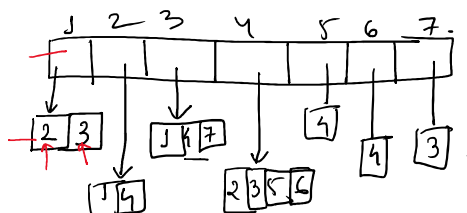
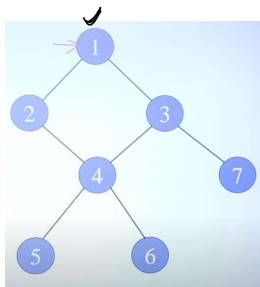
adj-matrix  $[7][7]$ .  $n^2 = 49$  cells.

	1	2	3	4	5	6	7
1	0	1	1	0	0	0	0
2	1	0	0	1	0	0	0
3	1	0	0	1	0	0	1
4	0	1	1	0	1	1	0
5	0	0	0	1	0	0	0
6	0	0	0	1	0	0	0
7	0	0	1	0	0	0	1

## Adjacency List -

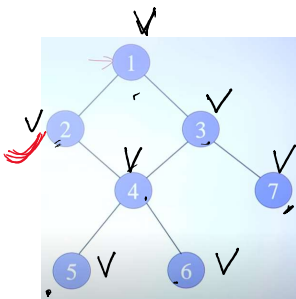
### ① List of List

`ArrayList<ArrayList<Integer>>` *adjList;*



Graph Traversal - visit every node in the graph.

- ① BFS (Breadth First Search)      ② DFS (Depth First Search)



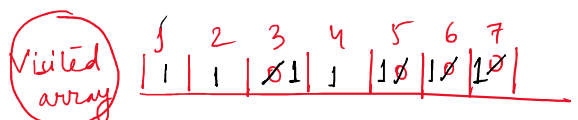
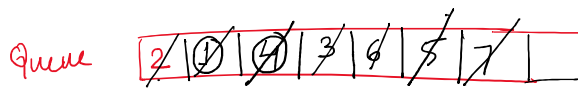
BFS Algorithm

Push the starting node into the queue and mark it as visited.

2. While the queue is not empty, repeat:

- Remove an element (node) from the front of the queue.
- Process the node (if required).
- Push all its unvisited neighboring nodes into the queue and mark them as visited.

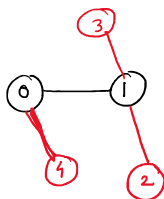
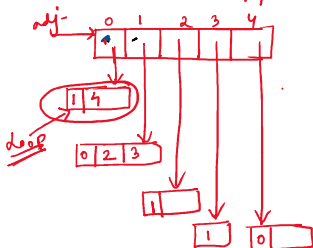
Queue Data Structure??? FIFO



Print: 2 1 4 3 6 5 7  $n=7$  = no of nodes

```
ArrayList<ArrayList<Integer>> adj = new ArrayList<>();
```

```
for (int i = 0; i < 5; i++) {
    adj.add(new ArrayList<>()); // Initialize with an empty list.
}
adj.get(0).add(1);
adj.get(1).add(0);
adj.get(0).add(4);
adj.get(4).add(0);
adj.get(1).add(2);
adj.get(2).add(1);
adj.get(1).add(3);
adj.get(3).add(1);
```



```

public ArrayList<Integer> bfsOfGraph(int V,
ArrayList<ArrayList<Integer>> adj) {
    ArrayList<Integer> bfs = new ArrayList<>();
    boolean vis[] = new boolean[V];
    Queue<Integer> q = new LinkedList<>();

    q.add(0);
    vis[0] = true;

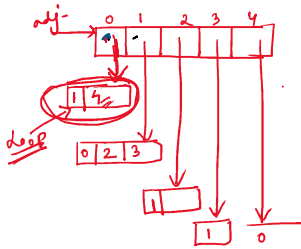
    while (!q.isEmpty()) {
        Integer node = q.poll(); // Remove front element
        bfs.add(node); // Print it
        for (Integer it: adj.get(node)) {
            if (vis[it] == false) {
                vis[it] = true;
                q.add(it);
            }
        }
    }

    return bfs;
}

```

1. Push the starting node into the queue and mark it as visited.
2. While the queue is not empty, repeat:
  - Remove an element (node) from the front of the queue.
  - Process the node (if required). Print it
  - Push all its unvisited neighboring nodes into the queue and mark them as visited.

Print: 2 1

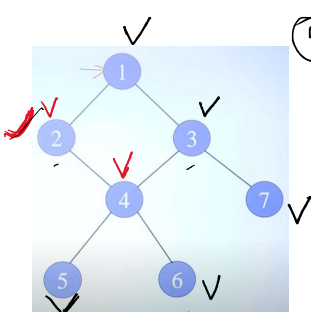


```

q.add(0);
vis[0] = true;
while (!q.isEmpty()) {
    Integer node = q.poll();
    bfs.add(node);
    for (Integer it: adj.get(node)) {
        if (vis[it] == false) {
            vis[it] = true;
            q.add(it);
        }
    }
}

```

2. 0 1 2 3 4  
 visited 1 0 0 0 0  
 print: 0



(5) (6) (3)

#### Iterative DFS Algorithm (Using a Stack)

1. Push start element in stack and print it. mark it as visited.
2. Repeat till stack is not empty:
  - See the top element in stack.
  - If all its neighbours have been visited, remove the top item from stack.
  - Else push one of its unvisited neighbours and continue the process.

Stack Data Structure → FIFO / LIFO.

Print: 2 4 5 3 7 1 6  
 Stack: 6, 5, 2



visited 1 0 0 0 0 0 0  
 1 2 3 4 5 6 7

