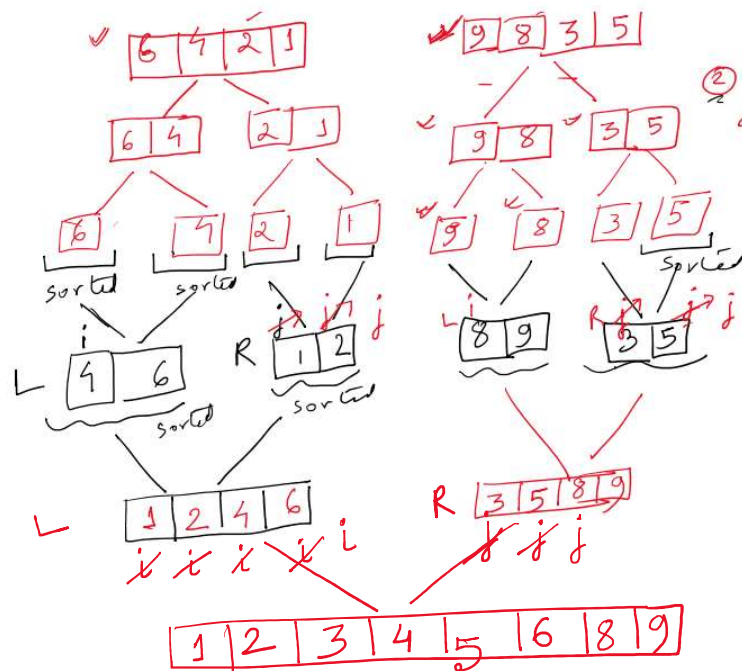
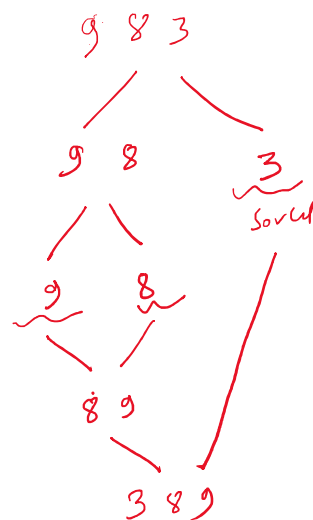


Note-
 ① Repeatedly divide the array into 2 equal parts.



part. 2
 Merge 2 sorted arrays into 1 sorted array.

Compare
 $L[i]$ $R[j]$

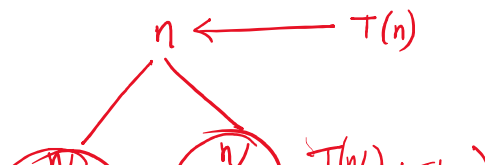
Merge Sort is Recursive.

TC - $T(n)$

Recursive Code \rightarrow Recurrence Relation \rightarrow Solve \rightarrow Time Complexity

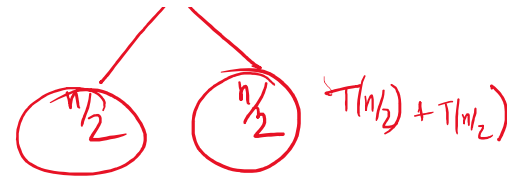
Suppose - Merge Sort ka code $T(n)$

$T(n) = T(n/2) + T(n/2) + 1 \cdot n$ ← Merge karne ka



$$T(n) = T(n/2) + T(n/2) + n$$

Actual problem → $T(n)$
 2 subproblems → $T(n/2) + T(n/2)$
 Merge karne ka Time → $+n$



$$T(n) = 2T(n/2) + n$$

Master Th^m →

$$a=2, b=2, n=1, p=0$$

$$a = b^k$$

$$2 = 2^1$$

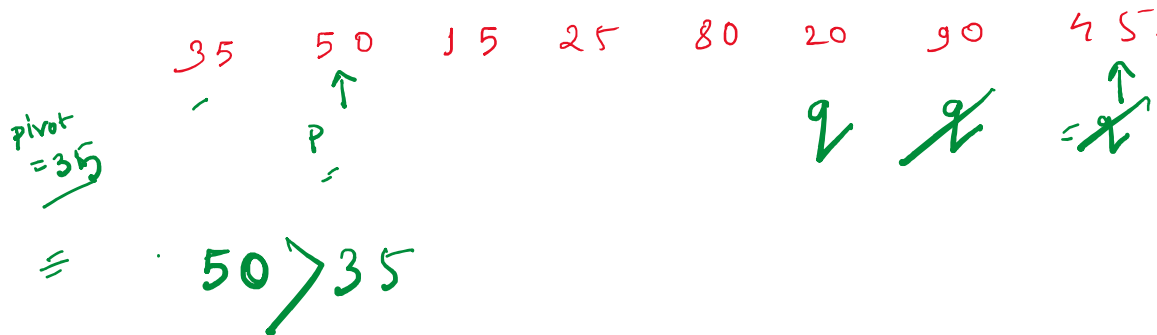
2nd condition

$$k=1$$

$$p=0$$

$$2^n \rightarrow n^{\log_b a} \cdot \log^{p+1} n = n^{\log_2 2} \cdot \log^{0+1} n = n \cdot \log n$$

Quick Sort - Divide & Conquer Technique.



Note -

① pivot element.

② pivot element = 1st element.

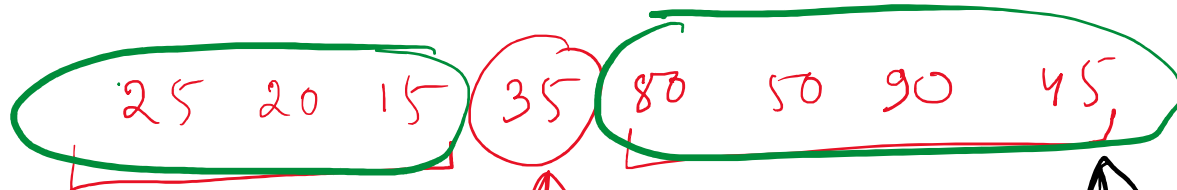
③ $p \rightarrow arr[p] \leq \text{pivot}$

$q \rightarrow arr[q] > \text{pivot}$

$\Rightarrow 50 / 35$

35 20 15 25 80 50 90 45

\uparrow \uparrow \uparrow \uparrow \uparrow
 q q q p q
 \downarrow \downarrow



$q \rightarrow \text{arr}[q] > \text{pivot}$

④ If $p \& q$ haven't crossed each other, swap them

⑤ If $p \& q$ crossed each other, swap ($\text{pivot}, \text{arr}[q]$)

Same step apply

original position

Same step apply here

Left

25

20

15

\uparrow

\rightarrow
 q
 p

pivot = 25

Swap ($\text{arr}[q], \text{pivot}$)

15 20 25

80 50

~~P~~ →

9 0

P

45

2

pivot = 80

Swap(arr(p), arr(2))

80 50

45

90

~~P~~ → q

~~2~~ →

Swap(pivot, arr(2))

45 50

<= pivot -

80

↑
original
pos

90

> pivot