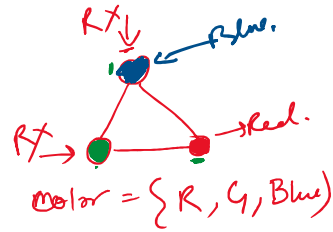
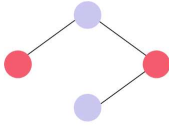


We are given a graph, we need to assign colours to the vertices of the graph. In the graph colouring problem, we have a graph and m colours, we need to find a way to colour the vertices of the graph using the m colours such that any two adjacent vertices are not having the same colour. The chromatic number is the minimum number of colors needed to color the graph with the constraint that no two adjacent vertices have the same color.



$m = \{\text{Red, Blue}\}$
Not possible.
Minimum color = 3.

◆ **Backtracking Approach — Theory**

Backtracking is a depth-first search-based technique that builds the solution step-by-step, and backtracks as soon as a constraint is violated.

1. **State Space**
Each state represents a partial assignment of colors to the graph's vertices.

2. **Decision Tree**
At each level of the recursion:

- ✓ Pick a vertex.
- ✓ Try assigning each of the M colors to that vertex.
- ✓ Check if this color is safe (i.e., none of its adjacent vertices has the same color).
- ✓ If yes, recurse for the next vertex.
- ✓ If no color works, backtrack.

3. **Base Case**
If all vertices are colored without conflict → Solution found.

◆ **Time Complexity**

In the worst case:
 $O(M^V)$ — M choices (colors) for each of V vertices.
But backtracking prunes invalid paths early, making it faster in practice.

Available colours = {R, G, B}

Possible Solution -

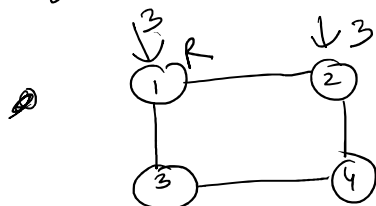
	1	2	3	4
1	R	G	R	G
2	R	G	R	B
3	R	G	G	R
4	R	G	G	B

Valid answer.

Invalid answer:

- $N_1 = R, N_2 = R$ (Invalid)
- $N_1 = R, N_2 = G, N_3 = R$ (Invalid)
- $N_1 = R, N_2 = G, N_3 = G, N_4 = R$ (Invalid)
- $N_1 = R, N_2 = G, N_3 = G, N_4 = B$ (Valid)

Invalid answer
R R R R
G G G G



Color = {Red, Blue, Green}

Total combinations = $3 \times 3 \times 3 \times 3 = 3^4$
Valid answer + Invalid answer.
No. of vertices

Node 1 = 3.
Node 2 = 3.
3
3