## Binomial tree note

06 February 2025 20:38

## A Binomial Tree $B_k$ is an ordered tree defined recursively, where k represents the order of the binomial

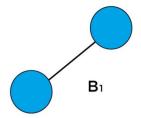
## tree.

- If the binomial tree is of order  ${\bf 0}$  ( $B_0$ ), it consists of a single node.
- In general, a binomial tree of order k ( $B_k$ ) consists of two binomial trees of order k-1, where one is linked as the left subtree of the other.

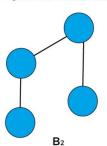
If Bo, where k is 0, there would exist only one node in the tree.



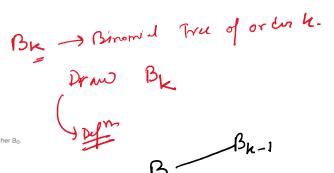
If  $B_1$ , where k is 1. Therefore, there would be two binomial trees of  $B_0$  in which one  $B_0$  becomes the left subtree of another  $B_0$ .

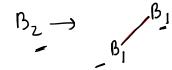


If B<sub>2</sub>, where k is 2. Therefore, there would be two binomial trees of B<sub>1</sub> in which one B<sub>3</sub> becomes the left subtree of another B<sub>3</sub>.

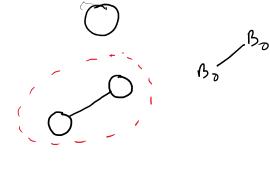


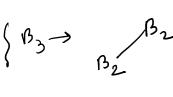
If  $B_3$ , where k is 3. Therefore, there would be two binomial trees of  $B_2$  in which one  $B_2$  becomes the left subtree of another  $B_2$ .





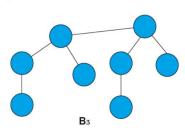






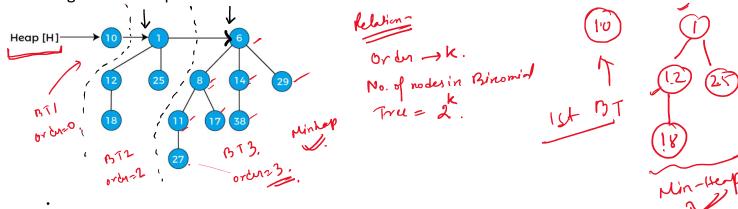






A binomial heap is a collection of binomial trees that satisfies the following binomial heap properties:

- No two binomial trees in the collection have the same order.
- 2. Every binomial tree in the heap must follow the min-heap property, i.e., the value of a child node is greater than parent node.



**Binomial Heap Union Operation** 

To perform the union of two binomial heaps, we have to consider the below cases -

Case 1: If degree[x] is not equal to degree[next x], then move pointer ahead.

Case 2: if degree[x] = degree[next x] = degree[sibling(next x)] then,

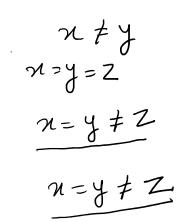
Move the pointer ahead.

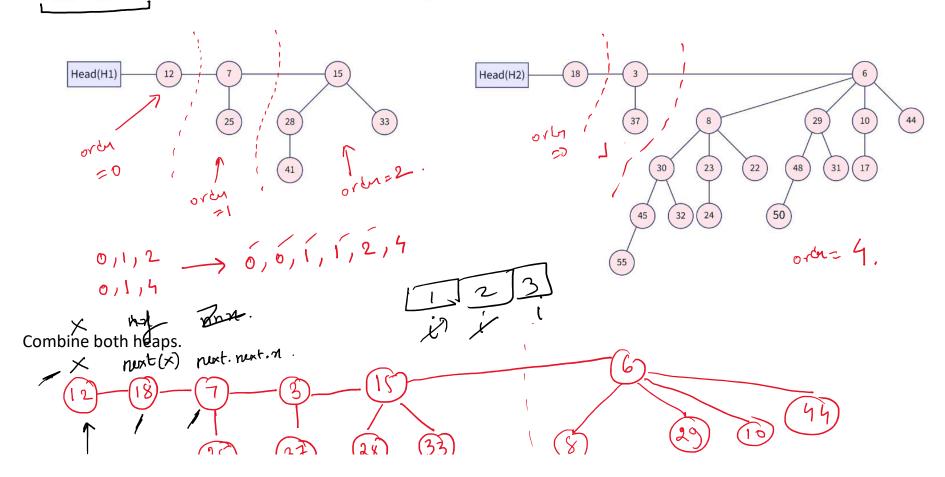
Case 3: If degree[x] = degree[next x] but not equal to degree[sibling[next x]]

and key[x] < key[next x] then remove [next x] from root and attached to x.

Case 4: If degree[x] = degree[next x] but not equal to degree[sibling[next x]]

and key[x] > key[next x] then remove x from root and attached to [next x].





 $\frac{1}{0} = \frac{1}{0} = \frac{1}$