

AdaBoost Classifier

Boosting in ML

Boosting is an ensemble learning technique where multiple weak learners(model) works together to build a strong learner(classifier) model.

Example of Boosting Algorithms → AdaBoost, Gradient Tree boosting, XBoost.

Let's say we are setting some rules to classify an Email as Spam and Not Spam. Rules →

- 1) Email has promotional Image → Spam
- 2) Email has link(s) → Spam
- 3) Email consists of sentences like "You won a prize money of \$...." → Spam
- 4) Email from our official Domain "bracu.com" → Not Spam
- 5) Email from known source → Not Spam.

If we consider these rules individually while checking for spam and not spam email, we

might mark 'spam' emails as 'not spam' and 'not spam' emails as 'spam'.

Rule-2 says, Email has link(s). ~~we may~~ receive links from known sources, which are not spam. But if Rule-2 works individually it may mark a 'not spam' email as 'spam'.

According to rule-4, if email consists of our official domain "brachu.com", the email is 'Not spam'. But we sometimes get spam and fake emails from similar domains. So, we should mark those mis-leading emails as SPAM.

So, instead of using each rule individually, we should combine all rules together while checking for spam emails.

Combining predictions of weak learners:

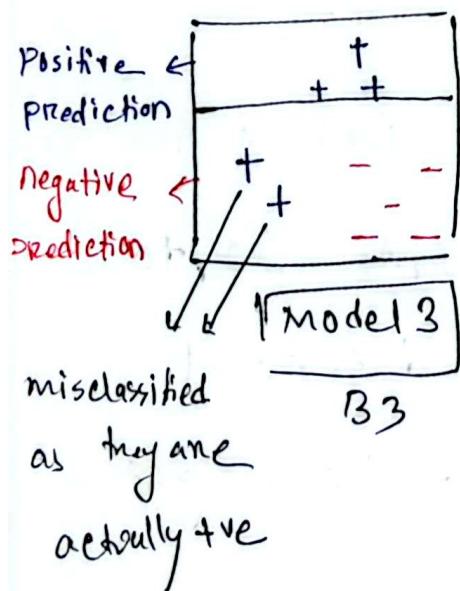
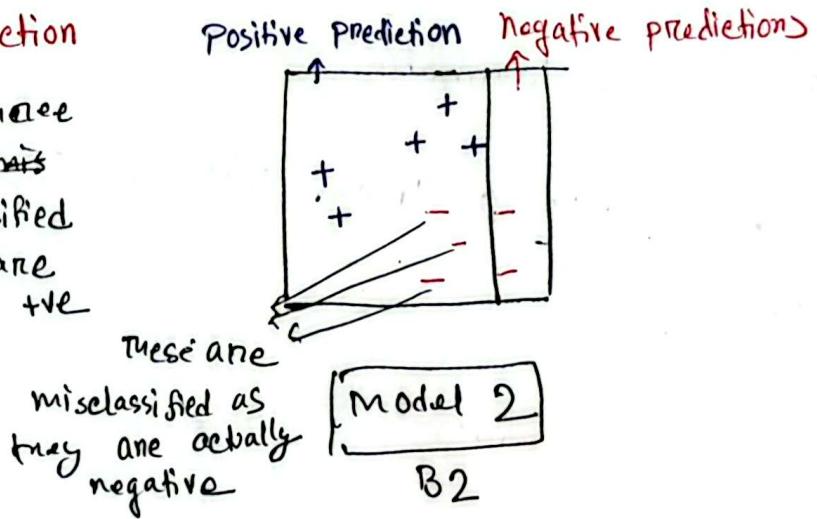
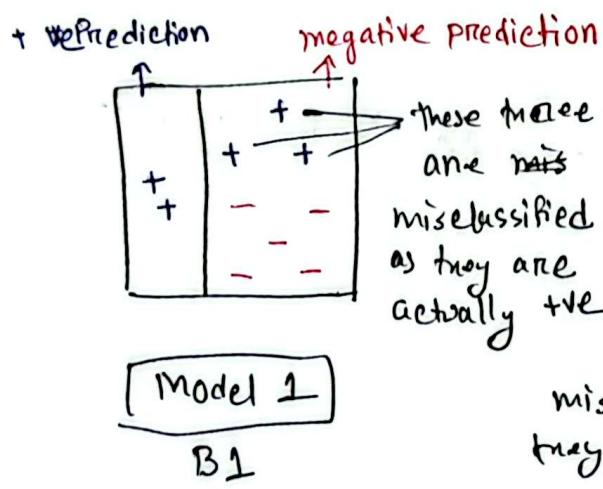
We can combine the results/predictions of multiple weak learners using the following methods →

- 1) ~~by~~ considering the prediction that has higher vote
- 2) using average/ weighted average.

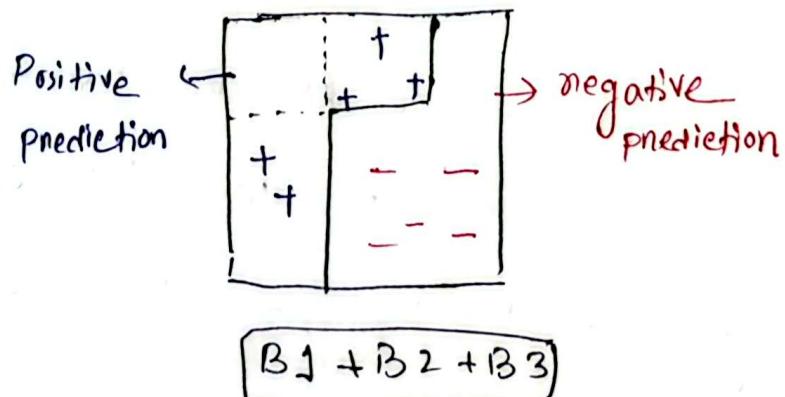
Adaptive Boosting

Adaboost is the first successful boosting algorithm developed for the purpose of binary classification.

Suppose there are three weak learners, we can see the classification done by each learners in a pictorial view as below →



Now if we combine $B_1 + B_2 + B_3$



This combined model is successfully combining all data points correctly.

ADABoost with Tree (CT and RT):

In ~~Regression~~ Random Forest we constructed multiple weak trees and combined those as Random Forest Model.

In Adaboost we will construct stumps. The Adaboost will consist of multiple stumps. Stumps will work as weak learners.

stump: It's a tree with just one Node and it's leaves.

Adaboost Procedure:

① STEP-1: Initialize the dataset and assign equal weights to each of the datapoint.

Let us assume we are running Adaboost for the following dataset with 14 datapoints, so to assign equal weight to each datapoint we will divide 1 by 14. So, the weight for each data point is $\frac{1}{14}$.

Dataset →

Day	Outlook	Temperature	Humidity	Wind	Play Tennis	Sample Weight
D1	Sunny	Hot	High	Weak	N	1/14
D2	Sunny	Hot	High	Strong	N	1/14
D3	Overcast	Hot	High	Weak	Y	1/14
D4	Rain	Mild	High	Weak	Y	1/14
D5	Rain	Cool	Normal	Weak	Y	1/14
D6	Rain	Cool	Normal	Strong	N	1/14
D7	Overcast	Cool	Normal	Strong	Y	2/14
D8	Sunny	Mild	High	Weak	No	1/14
D9	Sunny	Cool	Normal	Weak	Y	2/14
D10	Rain	Mild	Normal	Weak	Y	1/14
D11	Sunny	Mild	Normal	Strong	Y	1/14
D12	Overcast	Mild	High	Strong	Y	1/14
D13	Overcast	Hot	Normal	Weak	Y	1/14
D14	Rain	Mild	High	Strong	N	1/14

Features

target
NO / Yes

Assigned
weights

Now we will find the first stump for this dataset.

Step-2: Building the Stump:

To construct the stump we will use Gini Index as this dataset is a classification problem.

The Stump will consist of one node. We need to find the ~~node~~ value of that node using Gini Index. Unlike Random forest we have to find Gini of all features.

~~outlook~~: Outlook feature



$$\text{Gini}(\text{outlook} = \text{sunny})$$

$$= 1 - \left(\frac{2}{5}\right)^2 - \left(\frac{3}{5}\right)^2$$

$$= 0.48$$

$$\text{Gini}(\text{outlook} = \text{overcast})$$

$$= 1 - \left(\frac{4}{9}\right)^2 - \left(\frac{5}{9}\right)^2$$

$$= 0$$

$$\text{Gini} (\text{outlook} = \text{Rain})$$

$$= 1 - \left(\frac{3}{7}\right)^2 - \left(\frac{4}{7}\right)^2$$

$$= 0.48$$

$$\therefore \text{Gini}(\text{outlook}) = \frac{5}{14} \times 0.48 + \frac{4}{14} \times 0 + \frac{5}{14} \times 0.48$$

$$= 0.348$$

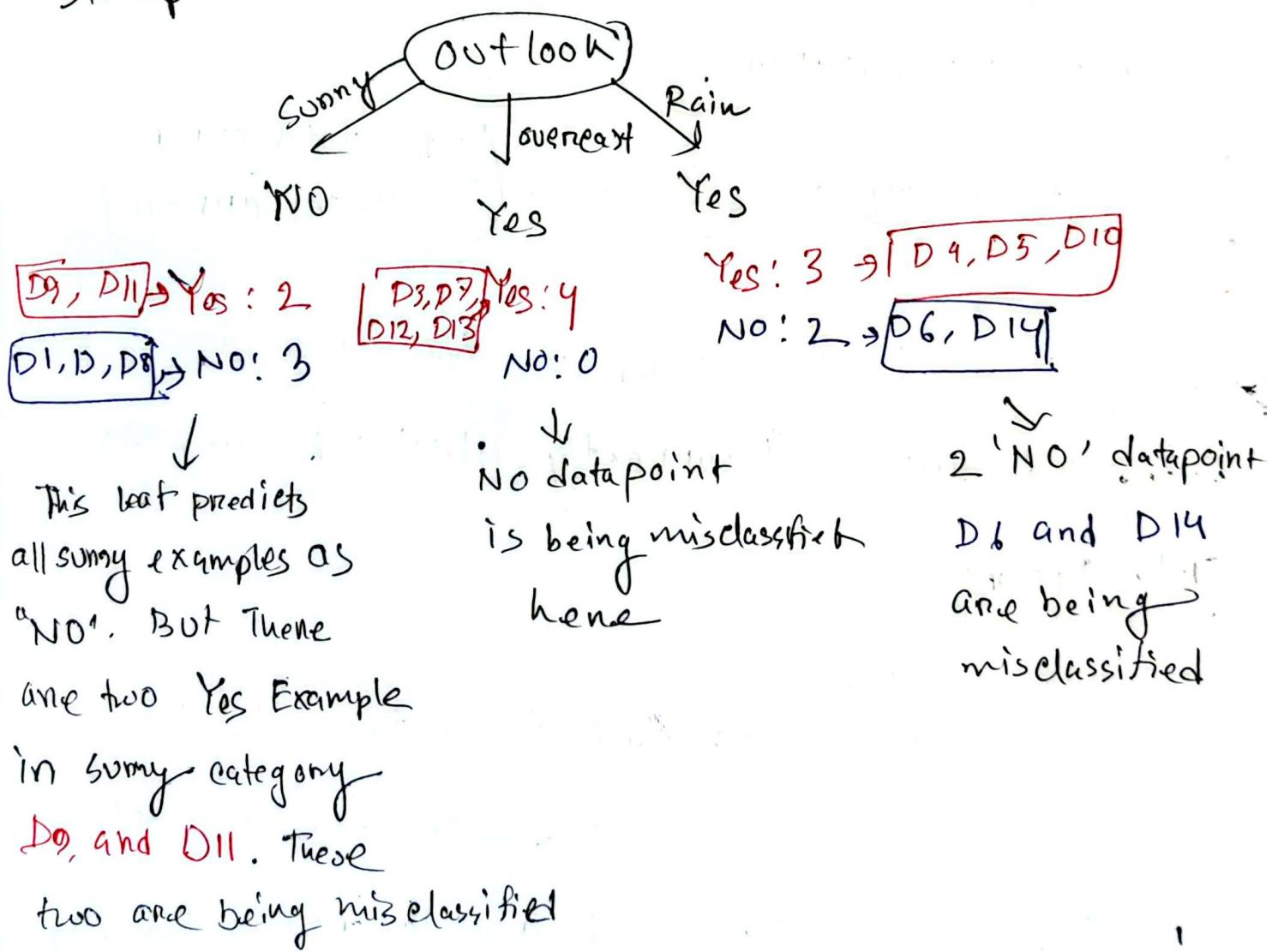
Similarly if we find Gini Impurity for all other features - we get

$$Gini(\text{Temperature}) = 0.441$$

$$Gini(\text{Humidity}) = 0.367$$

$$Gini(\text{Wind}) = 0.429$$

Among these 4 Gini impurities, $Gini(\text{outlook}) = 0.34$ is lowest. So, outlook will be the first stump.



so, this stump is not perfect as few datapoints, D9, D11, D6 and D14 are being misclassified.

So, we need to find how well this stump is working/ classifying.

Step - 3: Determine Amount of say (α)

Amount of say is the determinatⁿ measurement of how well it classified the samples in the classification.

$$\text{Amount of say, } \alpha = \frac{1}{2} \times \ln \left(\frac{1 - \text{total error}}{\text{total error}} \right)$$

Total error is the sum of the weights associated with incorrectly classified samples.

Total Error:

We have seen,

Sunny branch misclassified two datapoints D9, D11

overcast branch did not misclassified any datapoint

Rain branch misclassified two datapoints D6, D14

The datapoints are errors. Each datapoint is weighted $\frac{1}{14}$.

$$\therefore \text{Total Error} = 2 \times \frac{1}{14} + 0 \times \frac{1}{14} + 2 \times \frac{1}{14} = 0.29$$

\downarrow \downarrow \downarrow
2 misclassified no misclassified 2 misclassified
data in sunny data in Rain data in Rain
outlook branch outlook branch branch

\therefore Amount of say. of first stump

$$\alpha = \frac{1}{2} \times \ln \frac{1 - 0.29}{0.29}$$
$$= 0.45$$

Now as 4 datapoints have been misclassified, we need to increase the attention towards these datapoints, so that the next stump focuses on these datapoints more. Also, we can decrease the attention towards the classified samples as they are already correctly classified by the first Stump. We do that by updating the sample weights.

Now we will proceed to create new dataset for the next Stump.

Step-4 : Update the Sample weight

New sample weight for incorrectly classified

$$\begin{aligned} \text{Samples} &= \text{sample weight (previous)} \times e^{+\alpha} \\ &= \frac{1}{14} \times e^{0.45} \quad \begin{array}{l} \text{+ve for increasing} \\ \text{weight/attention} \end{array} \\ &= 0.11 \end{aligned}$$

New sample weight for correctly classified

$$\begin{aligned} \text{Samples} &= \text{sample weight (previous)} \times e^{-\alpha} \\ &= \frac{1}{14} \times e^{-0.45} \quad \begin{array}{l} \text{negative for} \\ \text{decreasing weight/} \\ \text{attention.} \end{array} \\ &= 0.046 \end{aligned}$$

Step-5: Normalized and cumulative Normalized

Sample weight.

After assigning new weights for 14 data points we can see the summation of all new weight do not give us 1. So we need to normalize each weights.

Day	Features	Play tennis	Updated sample weight	Normalized sample weight	Normalizing factor
D1		N	0.096	0.051	0.051
D2		N	0.096	0.051	0.102
D3		Y	0.046	0.051	0.153
D4		Y	0.046	0.051	0.204
D5		Y	0.046	0.051	0.255
D6		No	0.11	0.122	0.377
D7		Y	0.096	0.051	0.428
D8		N	0.096	0.051	0.479
D9		Y	0.11	0.122	0.601
D10		Y	0.046	0.051	0.652
D11		Y	0.11	0.122	0.774
D12		Y	0.096	0.051	0.825
D13		Y	0.096	0.051	0.876
D14		N	0.11	0.122	0.998

Summation of Updated Sample weight = $10 \times 0.096 + 9 \times 0.11 = 0.9$

Normalized weight for correctly classified

$$\text{Samples} = \frac{0.096}{0.9} = 0.051$$

Normalized weight for incorrectly classified

$$\text{Samples} = \frac{0.11}{0.9} = 0.122$$

So, we write all Normalized weights. Now we will calculate five cumulative Normalized weight [adding immediate weight in increasing order]

Step-6: Generate random numbers between 0-1.

For each datapoint, we will generate random numbers.

Day	Features	Play Tennis	Cumulative Normalized Weight	Generated Random Numbers
D1		N	0.051	0.040
D2		N	0.102	0.100
D3		Y	0.153	0.151
D4		Y	0.204	0.200
D5		Y	0.255	0.250
D6		N	0.377	0.262
D7		Y	0.428	0.500
D8		NO	0.479	0.700
D9		Y	0.601	0.900
D10		Y	0.652	0.370
D11		Y	0.744	0.600
D12		Y	0.825	0.682
D13		Y	0.876	0.886
D14		N	0.998	0.980

Step 7 : Create New dataset for 2nd stamp.

Now we will check for each random numbers. We will ~~check~~ consider the cumulative Normalized weighted as Range.

Ranges are $0 - 0.051$, $0.051 - 0.102 \dots$
 $0.276 - 0.998$.

We will check in which random numbers falls into.

The first random number 0.040 falls into range $0 - 0.051$, or $0.040 < 0.051$. So we will select the data point corresponding to 0.051 , which is Day 1. so Day 1 is selected for the ~~set~~ new dataset.

Let's check another random number 0.700 , which falls into $0.652 - 0.774$ range, or $0.700 < 0.774$. so we select the Day 11 that is corresponding to 0.774 weight we do this for all 14 random numbers, and will get 14 ~~new~~ datapoints for the new dataset as below →

New dataset

Day	Outlook	Temparature	Humidty	Wind	Play Tennis
D1					
D2					
D3					
D4					
D5					
D6					
D9					
D11					
D14					
D6					
D9					
D11					
D14					
D14					

Hence we can see, the misclassified examples D6, D9, D11 and D14 has been repeated multiple times. So, the next stump will focus more on this datapoints.

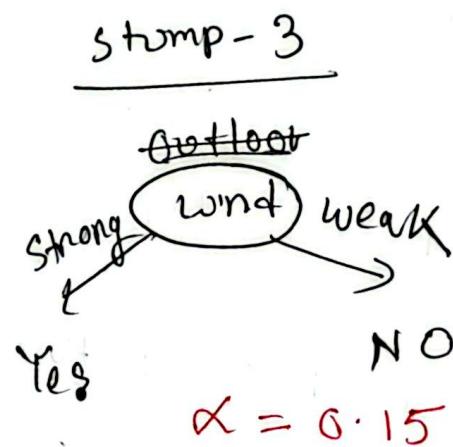
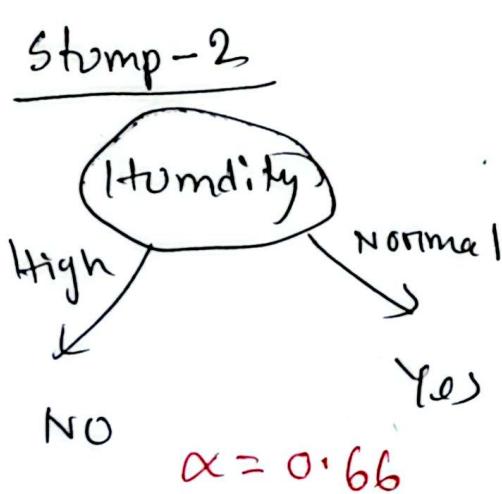
~~6.6~~

Now Repeat Step 1 - Step 7 for this new dataset and create the second Stump.

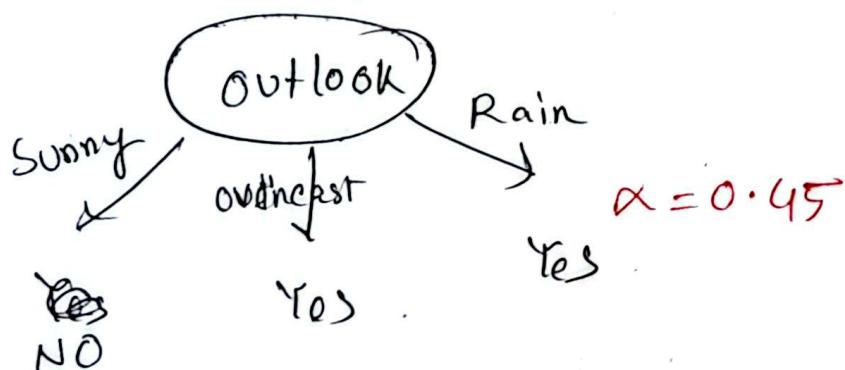
If we continue this process two times more, we will get two more Stumps.

Let's assume, we got the following

two Stumps,



The Stump + we got



Now we will do the Bagging process.

Bugging:

Now let's we will ~~assume~~ predict the class

For, Outlook = sunny, temperature = mild,
Humidity = Normal and Wind = weak.

If we run this input all three stumps \rightarrow
we get \rightarrow

Stump-1 : NO $\alpha = 0.45$

Stump-2 : Yes $\alpha = \cancel{0.60} 0.66$

Stump-3 : NO, $\alpha = 0.05$

so, The final prediction,

Weighted vote of Yes $= 0.66$

Weighted vote of NO $= 0.45 + 0.05 = 0.50$

As weight of Yes is larger, the final
result will be Yes.

We can use adaboost Algoitum for Regression
problem as well.