

Column Generation Techniques for GAP

July 22, 2019

1 Preliminary Tests

Github page : <https://github.com/mody3062/CG>

Testing algorithms

- Classical column generation (Kelly's cutting plane)
- Stabilized column generation (O. Du Merle, et. al., 1997)
- Separation + Classical column generation
- Separation + Stabilized column generation

Algorithmic parameters RMP was constructed with a single decision variable which is dummy. The coefficient of the dummy variable on the objective function was set to a sufficiently large value, which is the sum of listed values such that `np.sum(c,axis=1)`. For stabilized column generation algorithm, I changed the parameter ϵ from 0.01 to 0.0001 for every 100 trials. (I am not sure whether I could understand the criteria for changing the parameter value(ϵ) well.)

To start the column generation procedure, an initial restricted master problem has to be provided. This initial restricted master problem must have a feasible LP relaxation to ensure that proper dual information is passed to the pricing problem. We have chosen to start with one column for each agent, corresponding to the optimal knapsack solution, and a dummy column consisting of all ones with a large negative profit. The dummy column ensures that a feasible solution to the LP relaxation exists. This dummy column will be kept at all nodes of the branch-and-bound tree for the same reason.

	Kelly			Stab.			Sep.			Sep.+Stab.		
	iteration	total(s)	M(%)	iteration	total(s)	M(%)	iteration	total(s)	M(%)	iteration	total(s)	M(%)
d05100	2485	26.13	25%	2216	33.27	32%	2296	44.57	61%	2321	49.8	66%
d10100	1223	7.83	25%	1068	11.49	42%	949	6.38	32%	858	7.25	40%
d10200	4485	133.04	54%	4423	199.37	61%	3253	132.49	67%	3703	193.21	73%
d20100	852	3.67	26%	782	6.63	49%	673	3.24	29%	629	4.15	41%
d20200	2513	38.59	41%	2549	65.75	55%	1862	32.86	51%	2288	52.38	59%
e05100	2577	15.03	42%	2356	27.73	51%	3487	74.37	86%	2761	37.61	76%
e10100	1345	6.83	36%	1405	12.45	52%	1160	6.64	54%	1261	8.93	58%
e10200	6273	153.91	77%	6580	271.2	80%	4328	186.97	87%	4455	218.22	88%
e20100	942	3.13	32%	979	7.4	52%	711	2.81	36%	644	3.5	46%
e20200	3273	37.77	57%	3374	76.73	69%	2390	44.17	75%	2713	61.78	78%

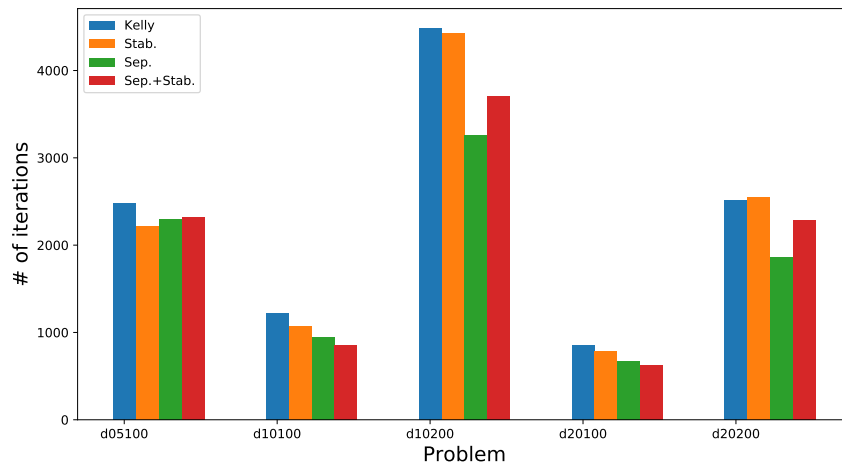


Figure 1: Performance comparison of the algorithms (gap_d)

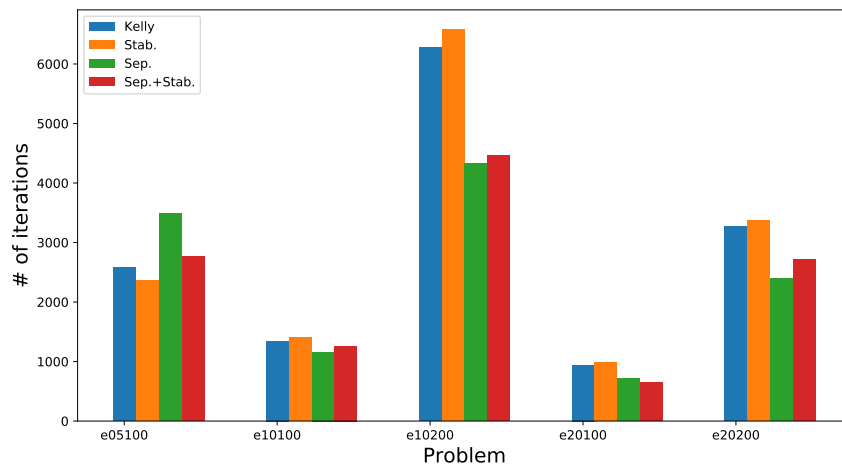


Figure 2: Performance comparison of the algorithms (gap_e)