

# Solution Summary

## Approach:

### Translation to a Search Graph

The problem was translated into a graph structure where:

- Nodes represent train stations.
- Edges represent train routes between stations with attributes such as departure time, arrival time, and travel distance.

Two types of graphs were constructed:

1. Mini-Schedule Graph for simplified problems.
2. Full-Schedule Graph for complex problems.

These graphs were expanded to include virtual start and end nodes, allowing for dynamic calculations like waiting times and adjustments based on input times.

### Choice of Search Algorithm

We used a custom graph traversal approach tailored to the problem's requirements:

- Dijkstra-like algorithm was implemented to handle weighted edges efficiently.
- The choice of traversal methods was guided by the nature of the cost function. Dijkstra ensures the shortest weighted paths.
- Graph Adjustments: For arrival time problems, we dynamically adjusted edge weights for specific start nodes to incorporate waiting times at stations. This added complexity but improved solution accuracy and performance.

## Key Insights

### Graph Expansion for Detailed Timing

By introducing detailed arrival and departure nodes with attributes like departure time and arrival time, the solver captured realistic scheduling details.

- **Intra-Station Connections:** Arrival nodes were linked to departure nodes within the same station, modeling waiting times.
- **Virtual Nodes:** Virtual start and end nodes ensured all possible transitions were represented, even for complex schedules.

### **Adjusting Start Times for Arrival-Time Cost Function**

- **Dynamic Wait Time Calculation:** The function recalculates the time from the virtual start node to neighboring departure nodes by computing the waiting time between the input time and the scheduled departure time.
- **Flexibility in Input Timing:** This adjustment ensures that the solver accurately incorporates user-provided input times.

### **Performance and Evaluation:**

- **Graph Expansion:** Virtual start and end nodes reduced the complexity of handling multiple schedules.
- **Efficient Iteration:** A single loop was used to evaluate all problem types, minimizing redundant computations.

### **What Worked Well:**

**Use of NetworkX Library:** Utilizing the NetworkX library for graph representation and manipulation was a significant advantage..

**Adapting Dijkstra's Algorithm:** It ensured that the shortest path calculation was efficient and accurate, leveraging the capabilities of Network