



KURSKOD / COURSE CODE	PROV / TEST CODE
D 0 0 4 1 D	0 0 0 1
KURSBENÄMNING / COURSE NAME	
Datastrukturer och algoritmer	
PROVBENÄMNING / TEST NAME	
Tentamen	
TENTAMENSdatum / EXAMINATION DATE	
2 0 2 0 - 0 3 - 2 7	
TENTAMENSORT/CITY (för distansstudenter / for off campus students only)	

ÅÅÅÅMMDD-XXXX
YYYYMMDD-XXXX

PERSONNUMMER / PERSONAL NUMBER
2 0 0 0 0 3 0 2 - 5 0 9 5
NAMN (TEXTA) / FULL NAME
Morgan Nyman
NAMNTECKNING / YOUR SIGNATURE

PROGRAM	INSKR.ÅR/YEAR	ANTAL SIDOR / NO. OF PAGES

Skanningsblad/Scanning Sheet

Behandlat
uppgift nr (sätt x) /
Mark the questions you
answered with an X

Lärarens anteckningar / Teacher's notes

1	X	9.5	
2	X	8	
3	X	3	
4	X	6	
5	X	3	
6	X	Ø	
7	X	Ø	
8	X	Ø	
9	1	0	
10			
11			
12			
13			
14			
15			
16			
17			
18			
Poängsumma Points	29.5	Betyg Grade	U

23294



4, 11, 7, 2, 8

max heap

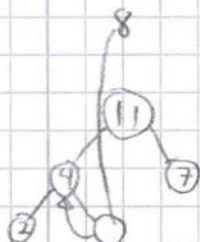
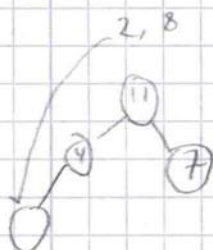
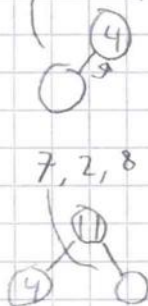
add first value as root

add next node as children left to right

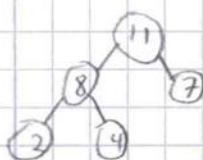
swap any children with parent if they're larger

Upp. 1
9.5

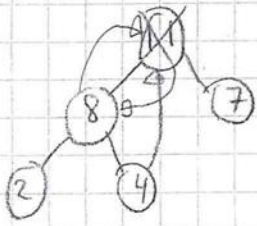
11, 7, 2, 8



stut!



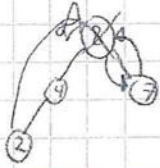
11	8	7	2	4
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11 | 8 | 7 | 2 | 4

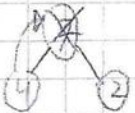
delete max

delete the root
replace it with the bottom-right node
swap with children if the parent is smaller



OK

8 | 4 | 7 | 2 | 11^{-0.5p}



7 | 4 | 2 | |



4 | 2 | | |

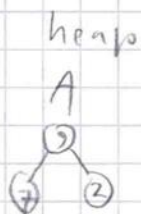


2 | | | |

slut!

| | | |

Example

merging 2 $(2^h - 1)$ heapsdelete root from heap A, and
add to the merged heap

heap B

merged

1c) ———

- 6 p.

10, 20, 4, 30

$$h(x, i) = x \bmod 10 + i(1 + x \bmod 9) \bmod 10$$

$$i = 0, 1, \dots, 9$$

0	1	2	3	4	5	6	7	8	9
10			20	4				30	

$$h(10, 0) = 10 \bmod 10 = 0$$

$$h(20, 0) = 20 \bmod 10 = 0 \text{ target}$$

$$h(20, 1) = 20 \bmod 10 + (1 + 20 \bmod 9) \bmod 10 = 3$$

$$h(4, 0) = 4 \bmod 10 = 4$$

$$h(30, 0) = 30 \bmod 10 = 0 \text{ target}$$

$$h(30, 1) = 30 \bmod 10 + (1 + 30 \bmod 9) \bmod 10 = 4 \text{ target}$$

$$h(30, 2) = 30 \bmod 10 + 2(1 + 30 \bmod 9) \bmod 10 = 8$$

Upp. 2
8

i $h(x) = x$

ii $h(x) = 2(x \bmod (\frac{m}{2}))$

Example

10, 20, 3, 40

10			
----	--	--	--

i $h(10) = 10$ out of index

ii $h(10) = 2(10 \bmod 2) = 0$

i $h(20) = 20$ out of index

ii $h(20) = 2(20 \bmod 2) = 0$ taken

- crashes -

consider the sequence a_1, \dots, a_m

where $a \bmod (\frac{m}{2}) = b$

as soon as $a_n (\text{arbitrary}) \bmod (\frac{m}{2}) = b$

the hash function is stuck

ii). incomplete.
space usage
(odd indexes).
- 2p

$$f(n) = O(h(n))$$

$$g(n) = O(h(n))$$

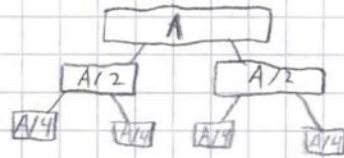
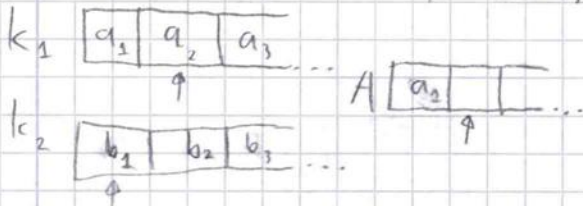
$$f(n) = O(g(n))$$

Answer: ~~a~~
- 1 p

3

3

k sorted list with n total elements to merge
 mergesort would sort in $O(n \log k)$ because it
 takes linear time two smaller list and that has to
 be done about $\log k$ times, and there is no need
 for further division since the smaller lists comes sorted.
 merging $O(n)$ times



" $A/2$ " means?

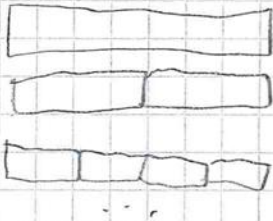
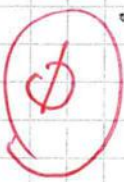
- 2p.

More details are
 needed.
 (divide and conquer).

b) —

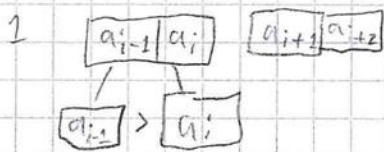
finding $a_{i-1} < a_i > a_{i+1}$

Divide the array into subarrays of size $\leq O(\log n)$



you pair a_{i-1} with a_i , merge and check $a_{i-1} < a_i$

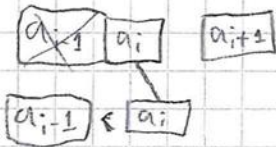
if true:



if
2. $a_{i-1} < a_i < a_{i+1} < a_{i+2}$ found

~~a_{i-1}~~ $a_i > a_{i+1} < a_{i+2}$ delete a_{i-1} from list and move on

else:

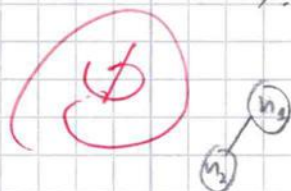


move on

comparison
 $O(\log n \cdot 2) + O(\log n) (=)$ merge

time: $\Theta(n) - \log_p$

$0, 1, \dots, n^2 - 1$ pick the first element, set as root



1. add the next at the bottom most-right
2. { if the added node appears to the
 - right: make sure it's larger than parent
 - left: make sure it's smaller than parent
 - otherwise swap with parent
 - if necessary

repeat until root which at most is

the height of the tree operations which is

less than n , because it's always

$n \geq 1$ nodes per height

X

running time

$\gg \Theta(n)$

$-10p$

$$A = \{a_1, a_2, a_3, \dots, a_n\}$$

$$B = \{b_1, b_2, b_3, \dots, b_n\}$$

$$\text{sum } A - a_i + b_j = \text{sum } B - b_j + a_i$$

$$\text{sum}_A = \text{sum}_B - 2(b_j - a_i)$$

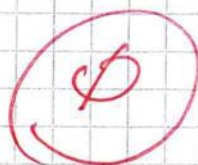
$$\text{sum}_A - \text{sum}_B = -2(b_j - a_i)$$

$$2(a_i - b_j)$$

calculate $\frac{\text{sum}_A - \text{sum}_B}{2}$

$$\text{if } a_i - b_j > \frac{\text{sum}_A - \text{sum}_B}{2} : a_i = a_{i+1}$$

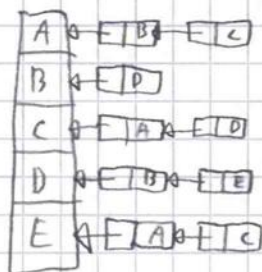
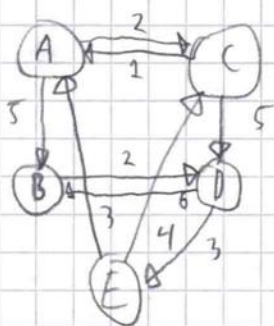
$$a_i - b_j < \frac{\text{sum}_A - \text{sum}_B}{2} : b_j = b_{j+1}$$



running time:
 $\Theta(n^2)$

— δ_p

b) —



Upp. 4
6.0

Depth first search

E, A, C, D, B $3+2+5+6=16$

E, C, A, B, D $4+1+5+2=12$

DFS tree?

— 2
P

discovery / finishing
time?

— 2
P

a	a	b	c	d
0	∞	∞	∞	∞
0	3	8	4	9

x - 5
p