### AND GATE

- A logic gate is a physical device that implements a Boolean function
- It performs a logical operation on one or more logic inputs and produces a single logic output.
- AND gate takes two inputs and gives output as low(0) whenever any of its input is low(0).
- The representation of AND function is C=A.B

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- AND gate takes two inputs and gives output as low(0) whenever any of its input is low(0).
- The representation of AND function is C=A.B

label=AND]Truth Table for AND gate

| Α | A B C |   |
|---|-------|---|
| 0 | 0     | 0 |
| 0 | 1     | 0 |
| 1 | 0     | 0 |
| 1 | 1     | 1 |



Figure: AND gate

### OR GATE

- OR gate takes two inputs and gives output as high(1) whenever any of it's input is high(1), else it gives low(0).
- It is represented as C=A+B

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- It is represented as C=A+B

### Truth Table for OR gate

| Α | В | С |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 1 |



Figure: OR gate

### **NOT GATE**

- NOT gate is different from previous two in the sense that it has 1 input instead of two.
- The output is high(1) if input is low(0) and vice versa.

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- NOT gate is different from previous two in the sense that it has 1 input instead of two.
- The output is high(1) if input is low(0) and vice versa.

### Truth Table for NOT gate

| Α | В |
|---|---|
| 0 | 1 |
| 1 | 0 |



Figure: NOT gate

# De-Morgan's Laws

The rules given by De-Morgan allow the expression of conjunctions and disjunctions purely in terms of each other via negation. Refer to slides 1, 3, and 5 before going further.

# De-Morgan's Laws

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#### Laws

The laws if laid in plain English are as follows:

- The negation of a conjunction is the disjunction of the negations.
- The negation of a disjunction is the conjunction of the negations.

### Law 1

### Theorem

The negation of a conjunction is the disjunction of the negations. Represented mathematically:

$$\overline{A+B} = \overline{A}.\overline{B} \tag{1}$$

$$\overline{A+B}=\overline{A}.\overline{B}$$

## Proof using Truth Table

| Α | В | A+B | A' | B' | (A+B)' | A'.B' |
|---|---|-----|----|----|--------|-------|
| 0 | 0 | 0   | 1  | 1  | 1      | 1     |
| 0 | 1 | 1   | 1  | 0  | 0      | 0     |
| 1 | 0 | 1   | 0  | 1  | 0      | 0     |
| 1 | 1 | 1   | 0  | 0  | 0      | 0     |

#### Theorem

The negation of a disjunction is the conjunction of the negations. Represented mathematically:

$$\overline{A.B} = \overline{A} + \overline{B} \tag{2}$$

$$\overline{A.B} = \overline{A} + \overline{B}$$

## Proof using Truth Table

| Α | В | AB | A' | B' | AB' | A'+B' |
|---|---|----|----|----|-----|-------|
| 0 | 0 | 0  | 1  | 1  | 1   | 1     |
| 1 | 0 | 0  | 0  | 1  | 1   | 1     |
| 0 | 1 | 0  | 1  | 0  | 1   | 1     |
| 1 | 1 | 1  | 0  | 0  | 0   | 0     |

# Generalised De-Morgan's Laws

The law can be extended to more than two inputs following the definition itself.

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#### Laws

$$\overline{(A+B+C+D+E....)} = \overline{A}.\overline{B}.\overline{C}.\overline{D}.\overline{E}....$$
 (3)

$$\overline{(A.B.C.D.E....)} = \overline{A} + \overline{B} + \overline{C} + \overline{D} + \overline{E}....$$
(4)