

Weekly Report

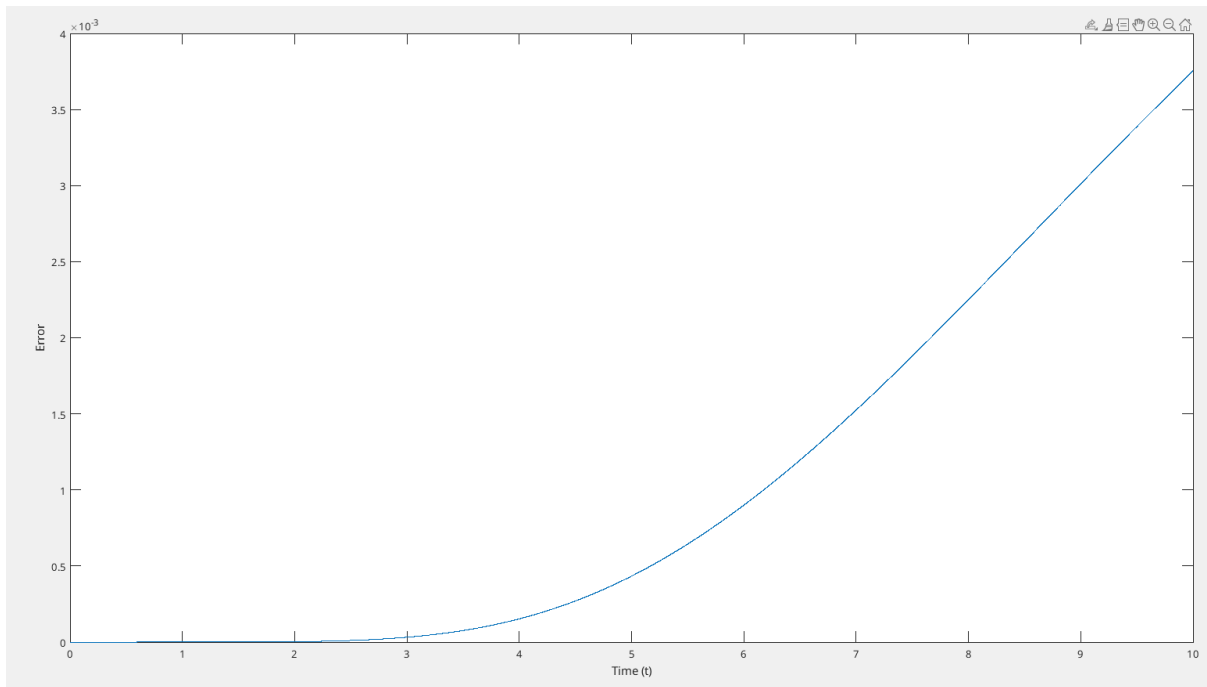
Name: Mohammed Al shuaili

Achieved goals through last week,

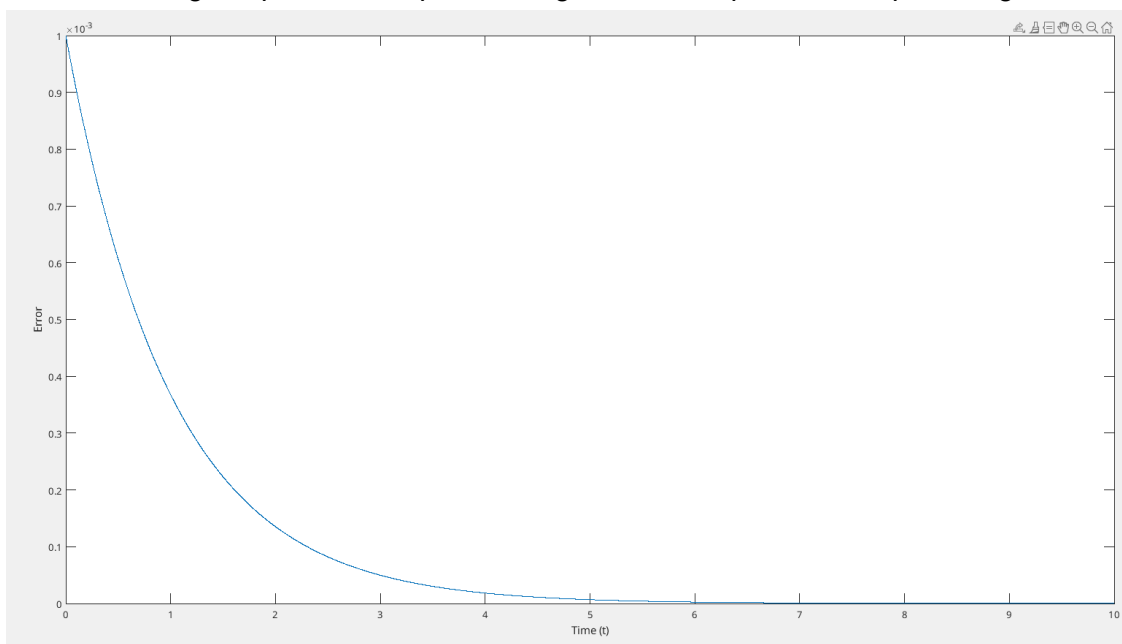
- Consider the previous step to approximate the next step in NILT0 and test it.

I've been trying to add this but I'm seeing a strange behaviour, and not sure if this should be expected.

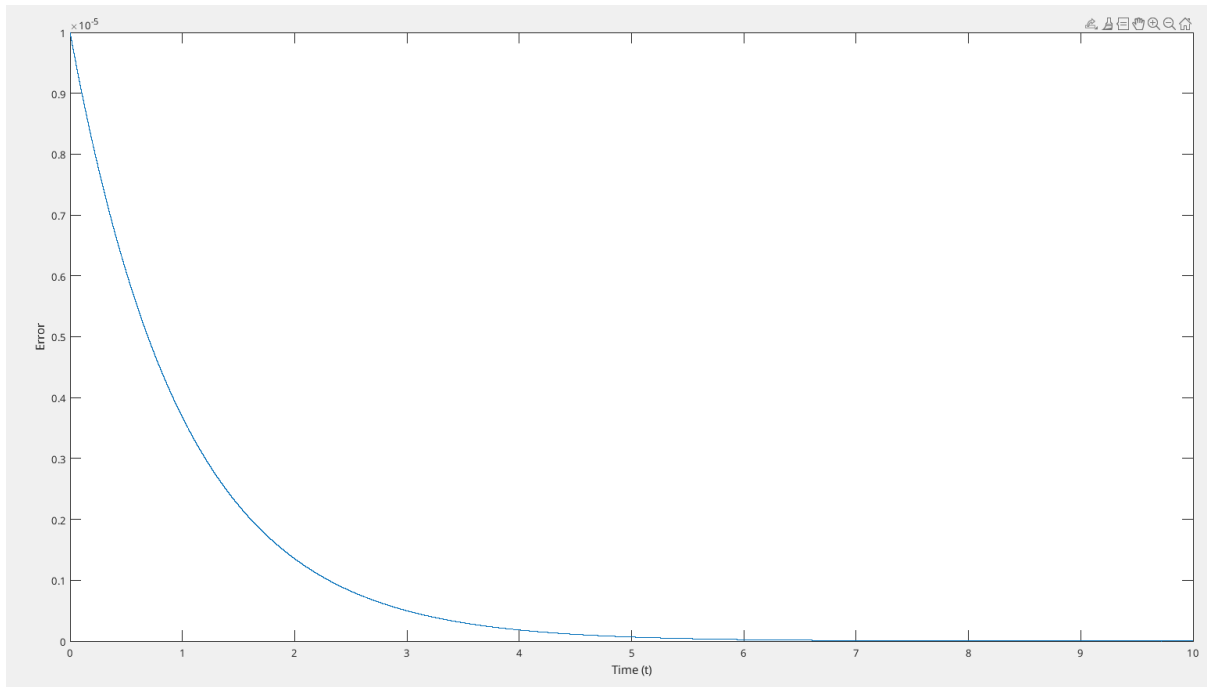
For example for $1/s+1$, if we don't consider the previous step, the error at $M = 5$ is very low but it gets higher as time increases this with the unit step response and doesn't change if we change the value of h (step size).



But considering the previous step and using the same input as the top one, I got this ,



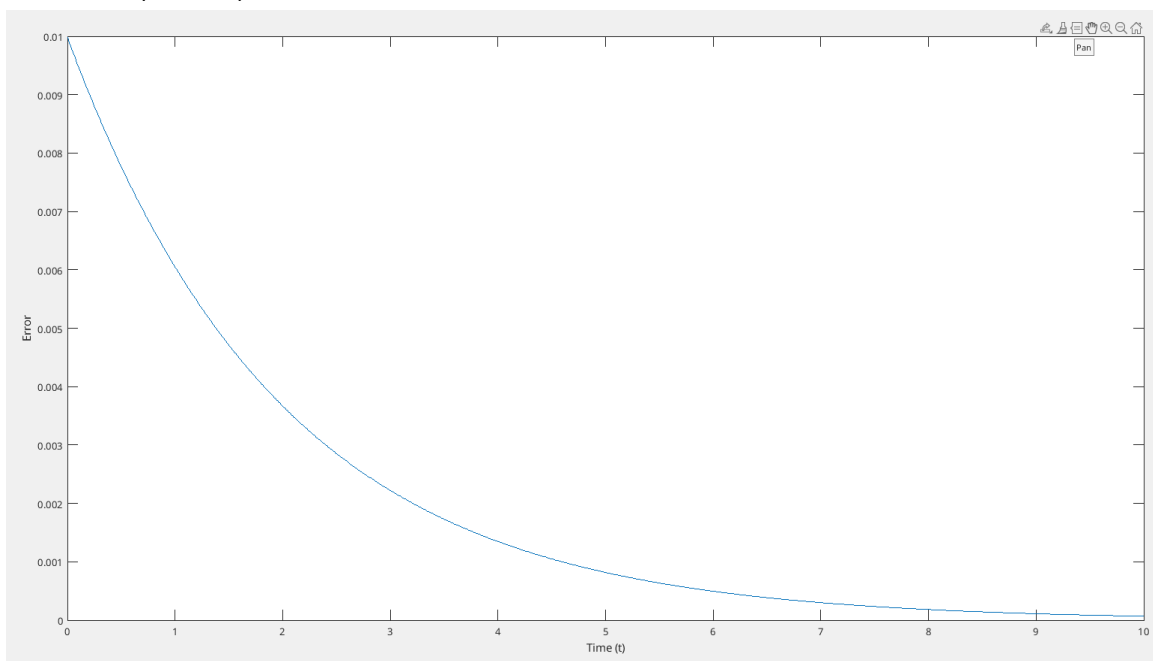
The error was kind of high at low t but it went down as time increased. However ,



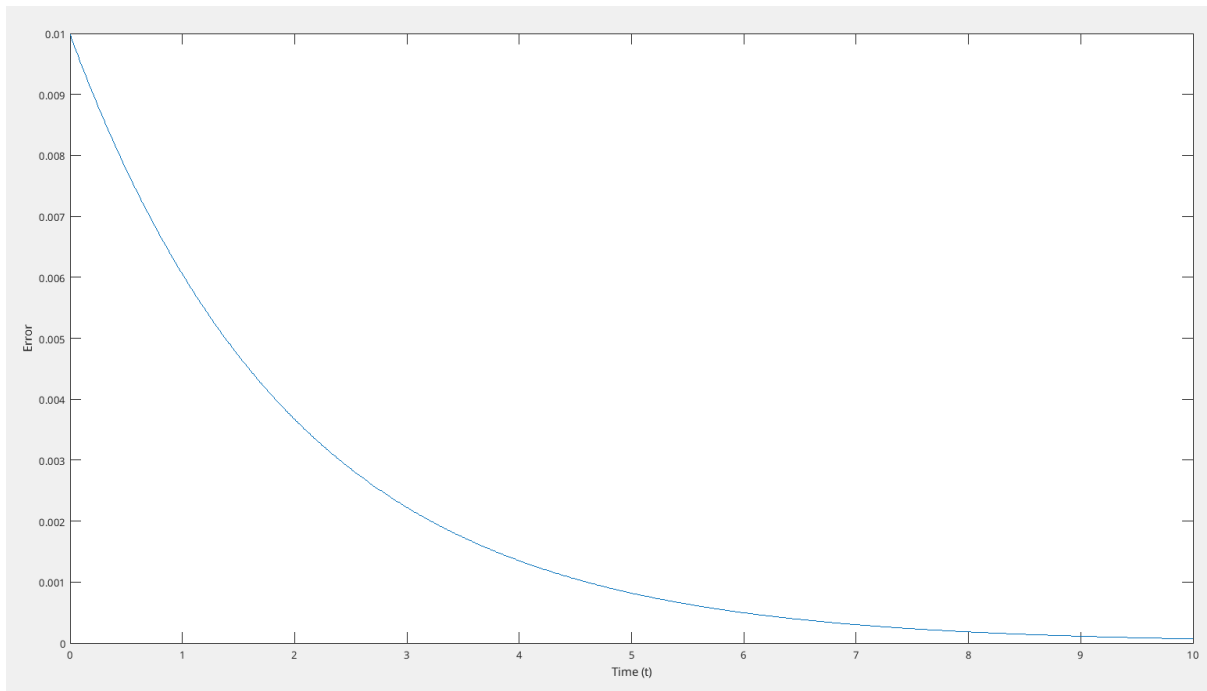
With the same M , but make more sections (i.e lower value for h).

However, when I consider $dy/dt = -0.5y + 1$, changing the value of M if we consider the previous step doesn't make any difference unless M goes above 13. additionally , only changing h (step size can have an effect).

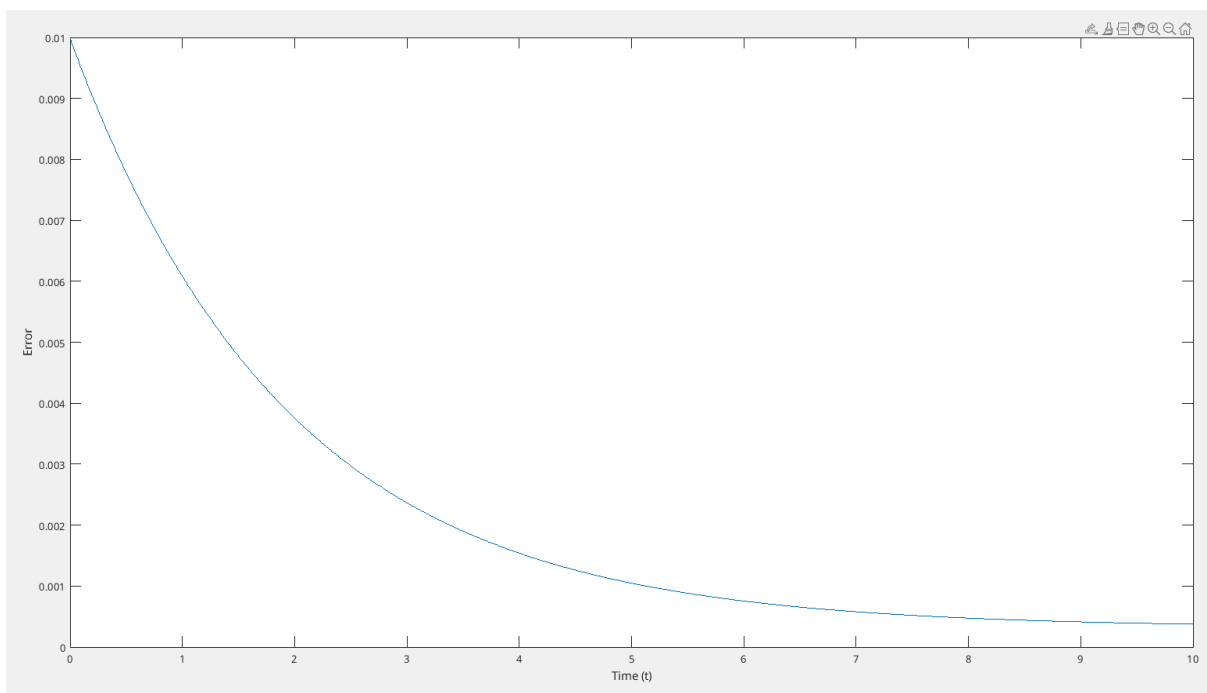
At $M = 2$. ($h=0.01$)



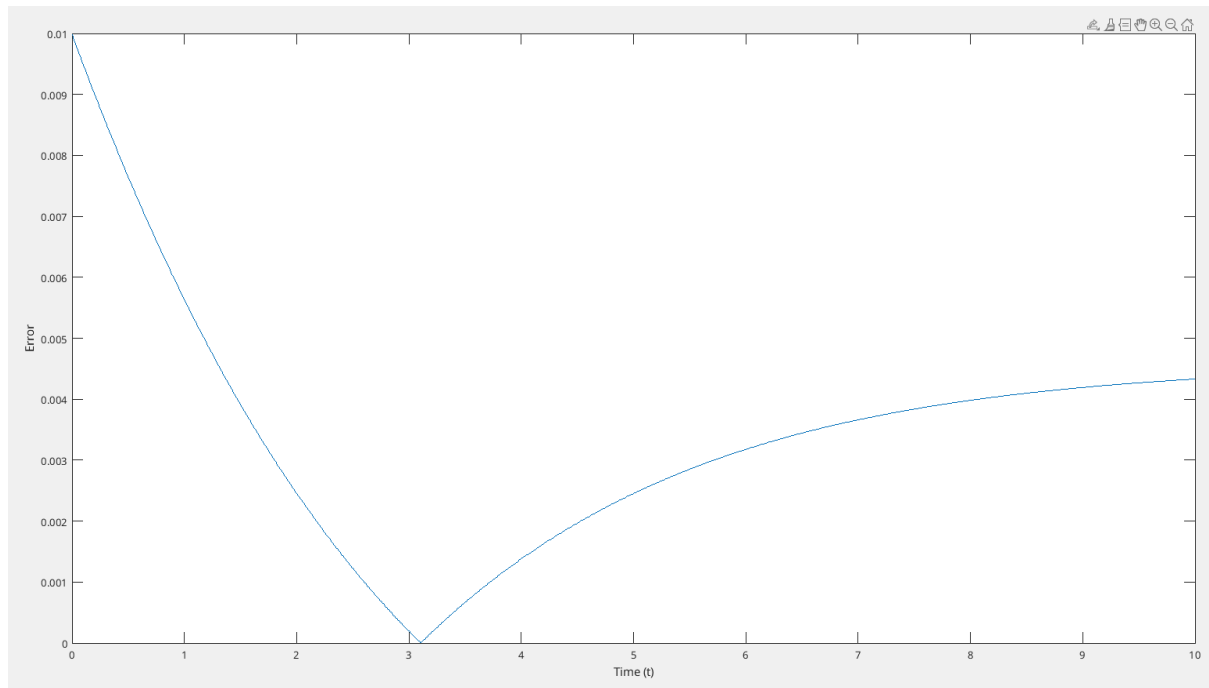
At $M = 5$,



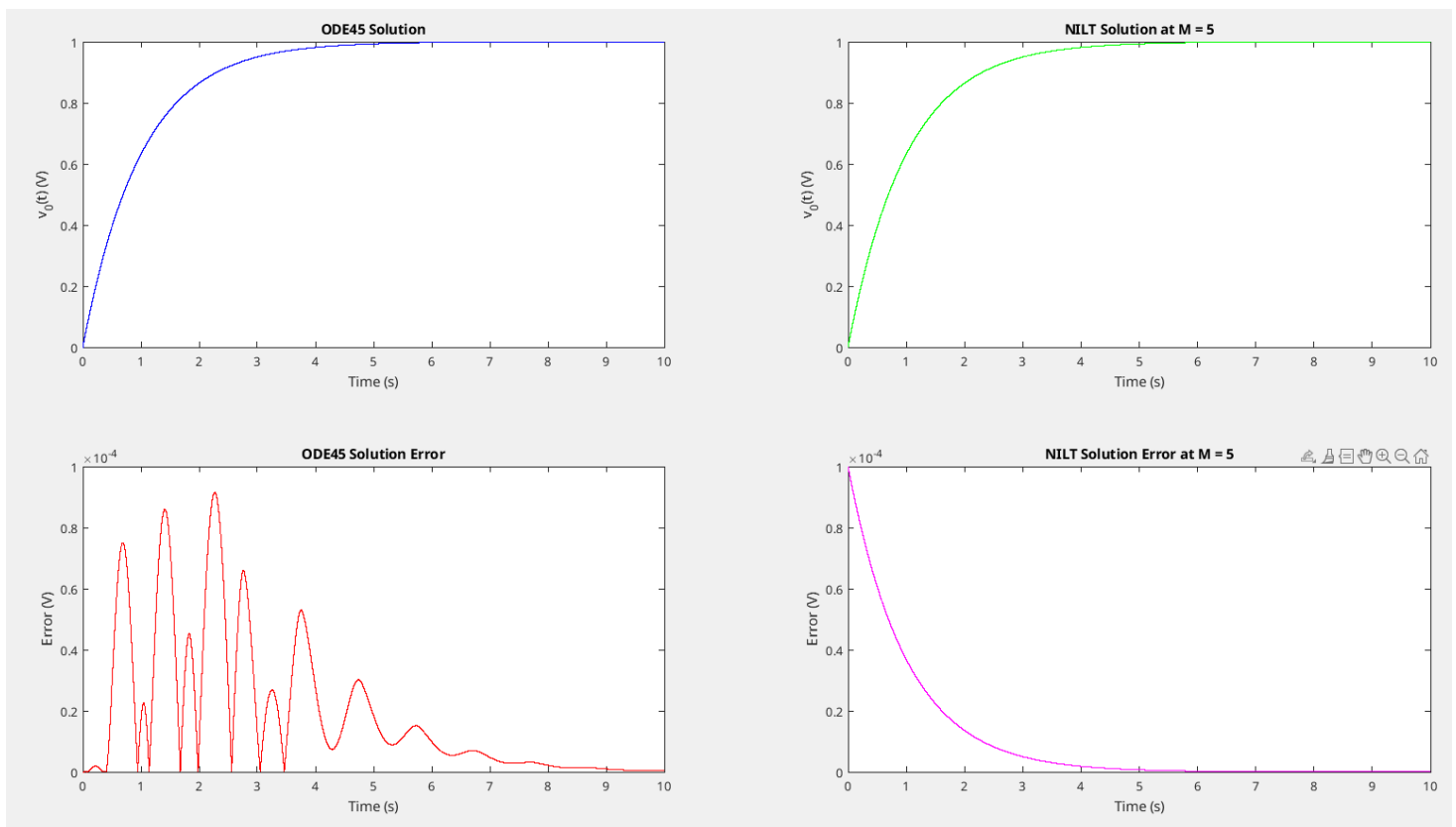
At $M = 12$



At $M = 13$,

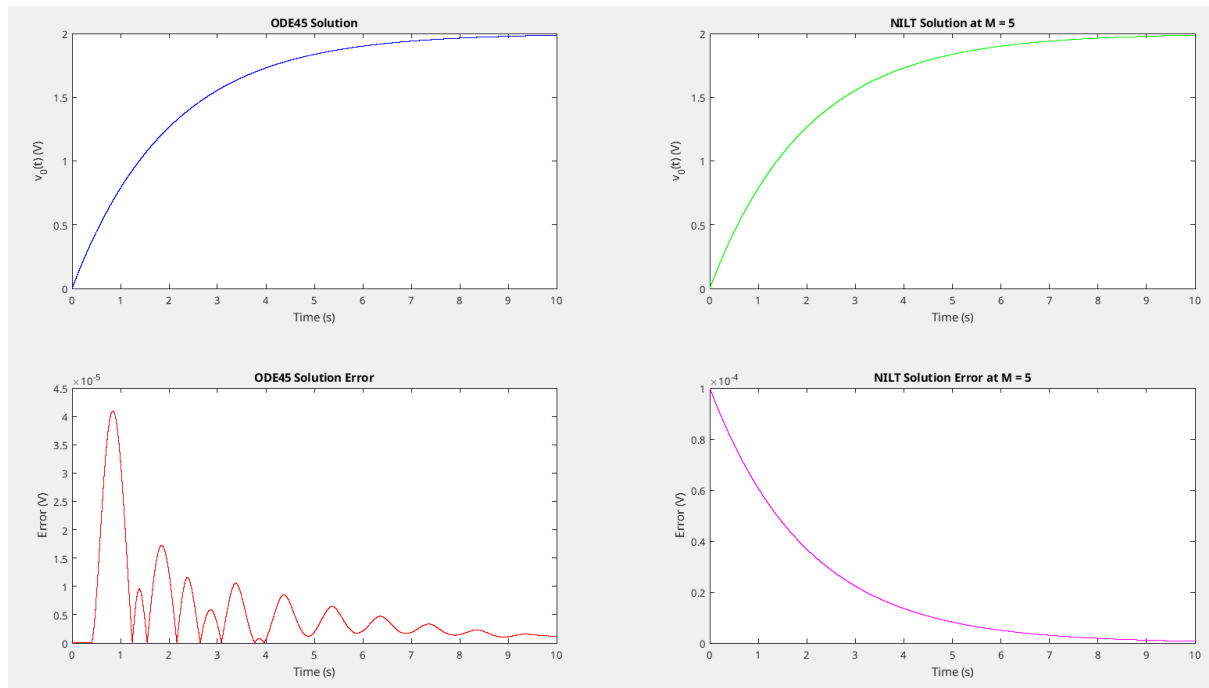


- Ode45 vs NILT0 with ($h = 0.0001$) with step response of $(1/s+1)$

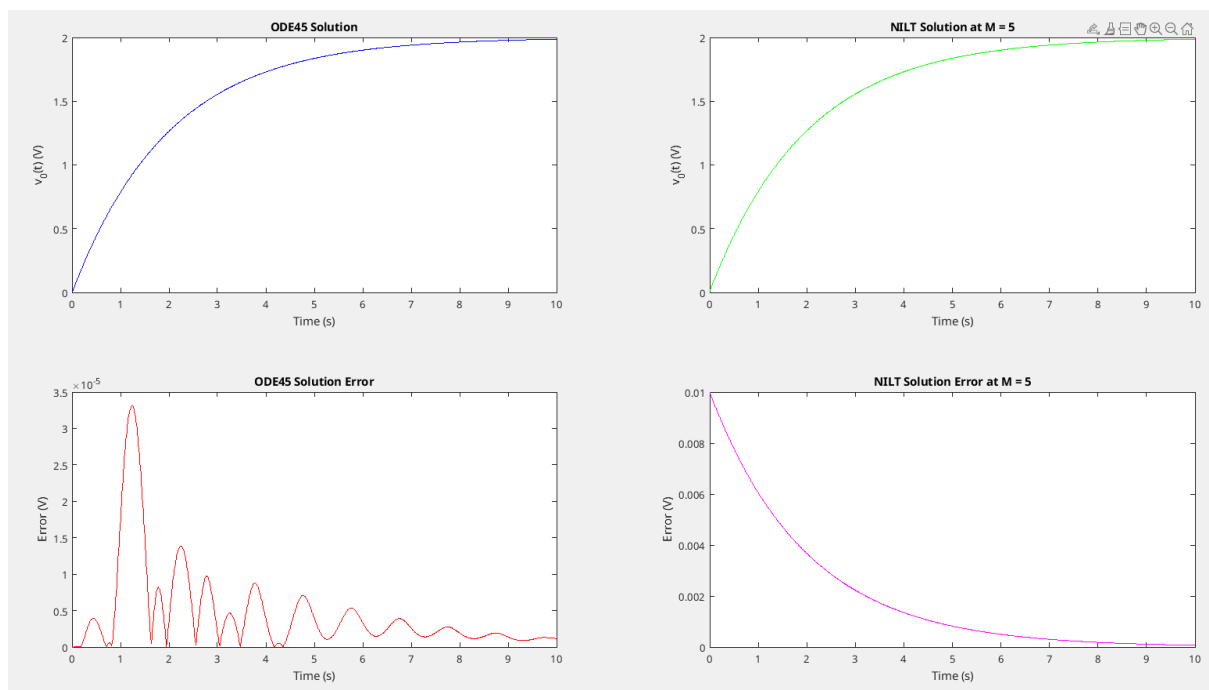


Overall , NILT performed much better than the Ode45 solver as time increased.

Testing with $(1/s+0.5)$.

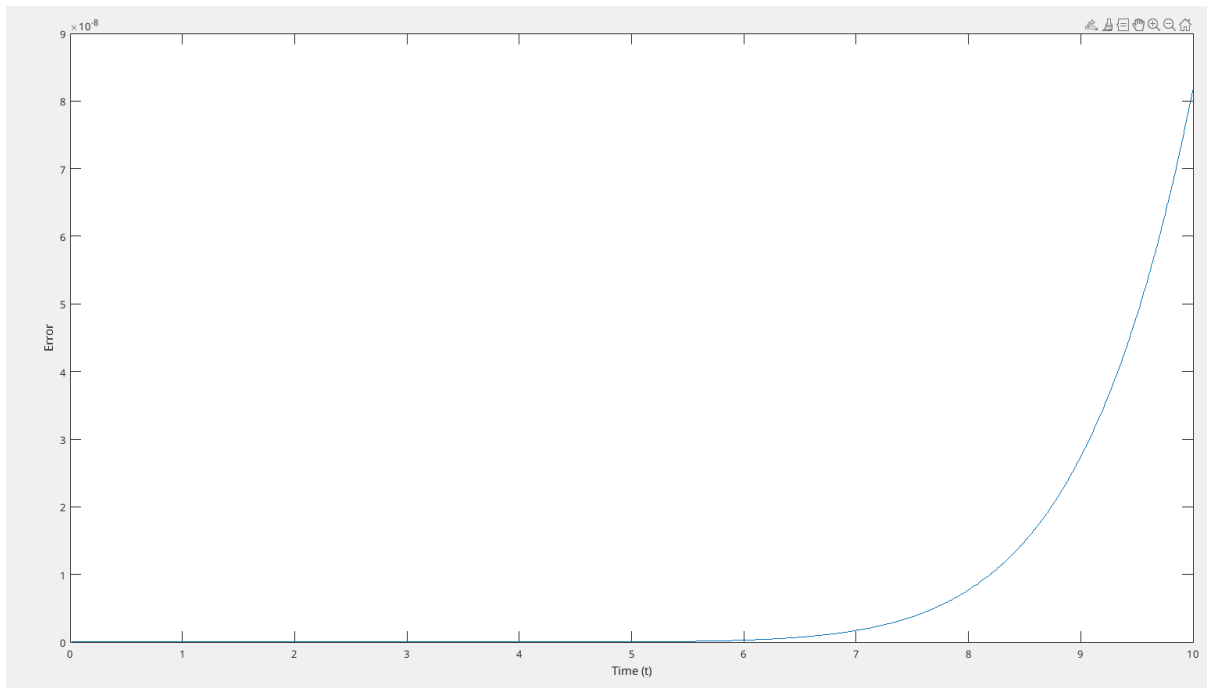


but , with $h = 0.01$,



The error in NILT is very high compared to Ode45.

Without considering the time marching, at $M=8$, for $1/s+0.5$, the error was much lower than when considering the previous step.



- **Problems:**

1. The issue I'm encountering is that, in my implementation, some functions perform better without considering the previous step. Additionally, changing the value of M has minimal impact when I do account for previous steps to approximate the next one. This suggests there may be a problem in the implementation, but I haven't been able to identify it yet.
2. I've struggled to implement the marching time method for second-order differential equations, as on pages 124 and 125. When I try incorporating the previous step into the next step's approximation, I encounter extremely high errors. This means something might be off in my implementation, though I haven't been able to find the issue yet. For reference, I'm looking at an example of an RLC circuit.

