

# Vision par ordinateur : Approche traditionnelle

Le royaume de la créativité

- **Hans Moravec:** *"it is comparatively easy to make computers exhibit adult level performance on intelligence tests or playing checkers, and difficult or impossible to give them the skills of a one-year-old when it comes to perception and mobility"*



# Plan

- Définir une image
- Traitements de base
- Taches de haut niveau
  - Un point clé : La représentation
  - Classification
  - Détection
  - Segmentation

# Qu'est-ce que la vision ?

## Percevoir le monde

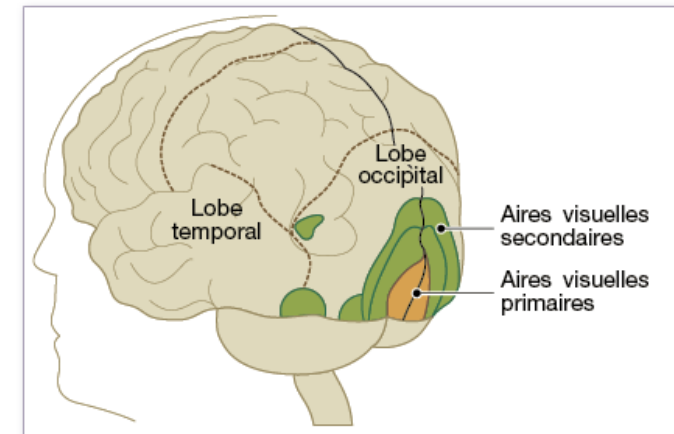
- Structure 3D
- Composé d'objets
- Efficacement interprété par l'être humain

## Info recueillie

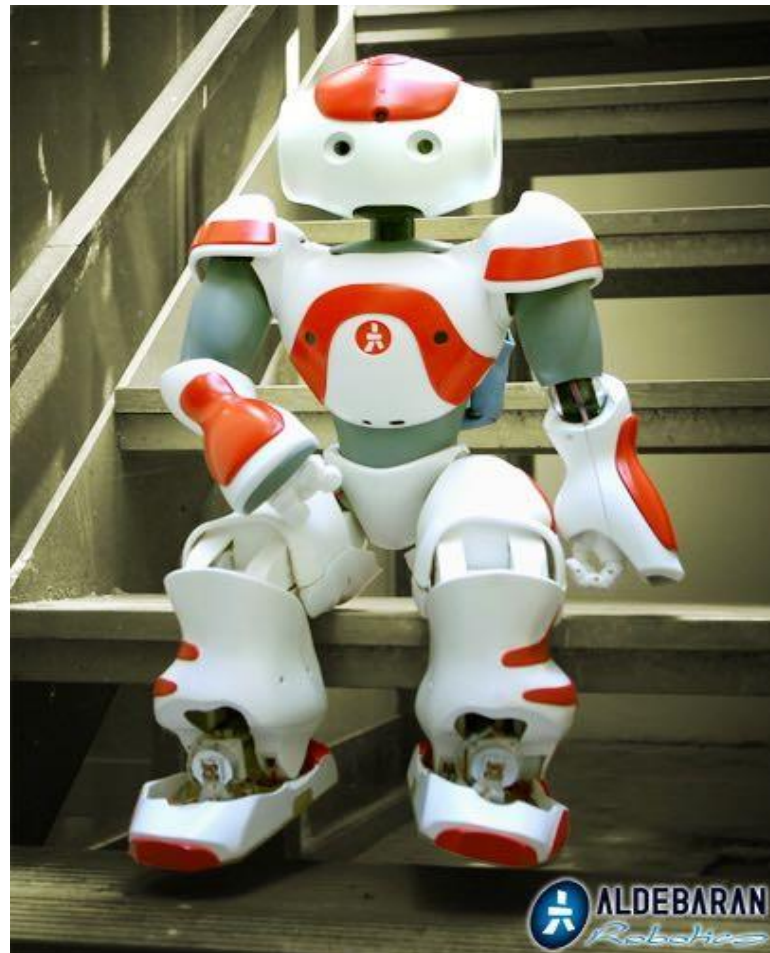
- Ensemble de points
- Pixels -> info sur la lumière
- Quantité et contenu spectral/couleur

## Comment « voir » les objets ?

- Les objets n'existent pas sur la rétine
- Interprétation -> processus visuel



# Qu'est ce qu'une image pour un ordinateur ?



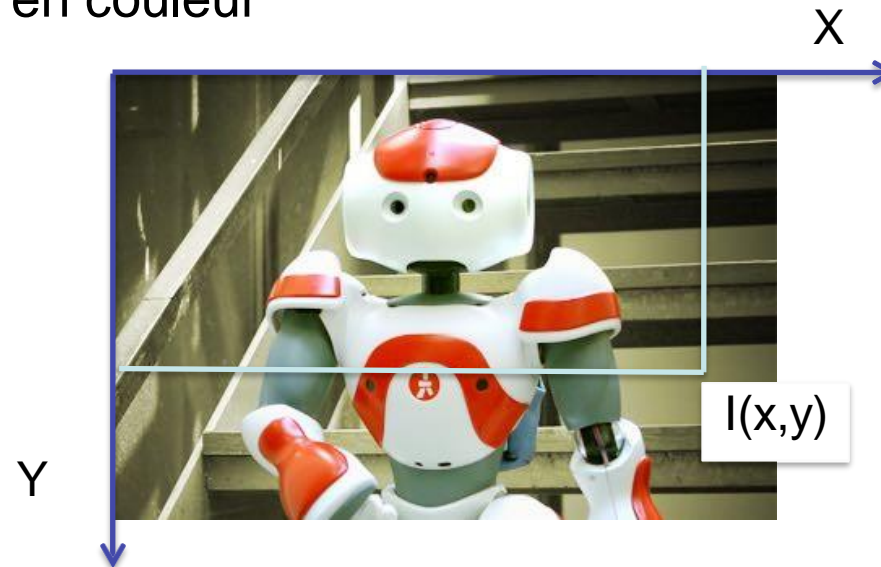
# Représentation des images

79	73	53	46	52	44	41	42	41	42	42	43	43	43	43	42	40	42	44	42	42	44	45	44	43	42	42	42	43	44	45	45	45
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# Représentation des images

## Fonction

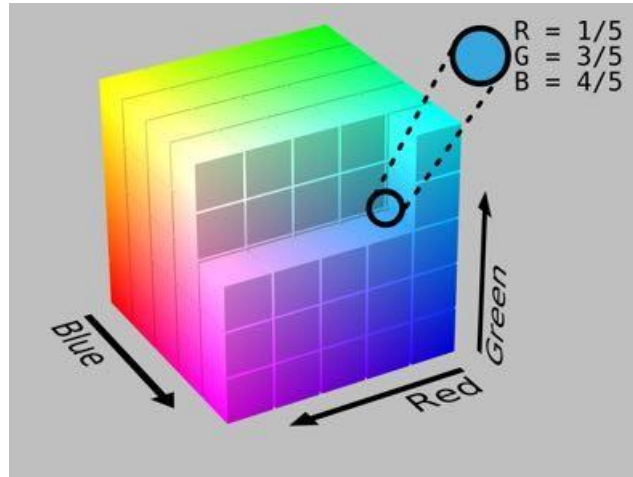
- $I(x,y)$  : valeur d'un pixel  
    **dans  $R$  en monochrome**  
    dans  $R^3$  en couleur



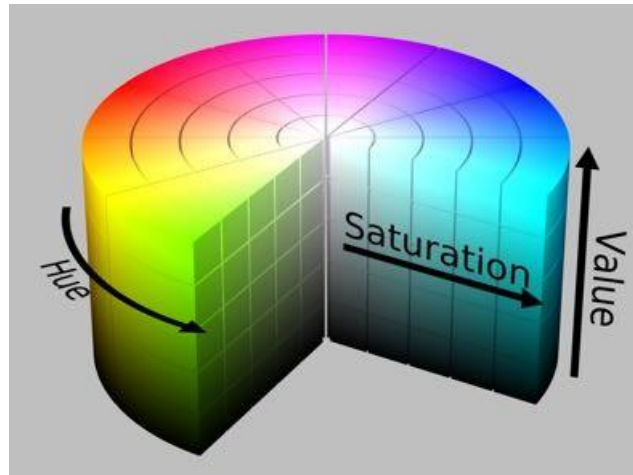


# Représentation des images

## Espaces colorimétriques

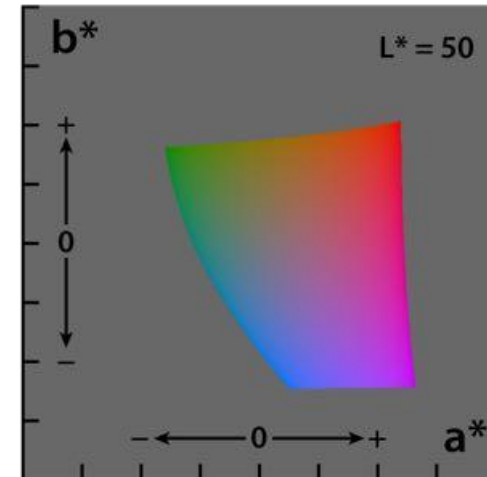
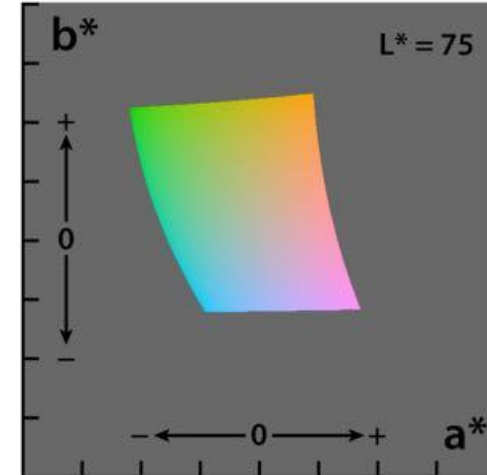


RGB



HSV

Lab





# Représentation des images

## Variations

- $I(x,y) \rightarrow I(x,y) + \alpha$  : luminosité globale
- $I(x,y) \rightarrow \lambda I(x,y)$  : changement de contraste
- $I(x,y) \rightarrow I(x+a,y+b)$  : translation
- $I \rightarrow A.I+b$  : transformation affine



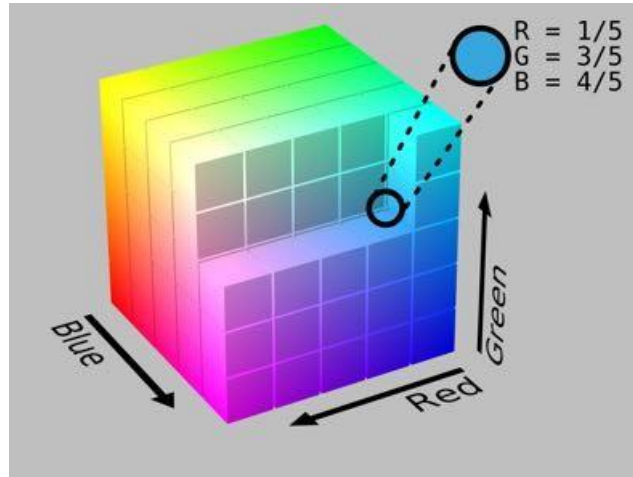
Traitements de base

# Filtrage et amélioration

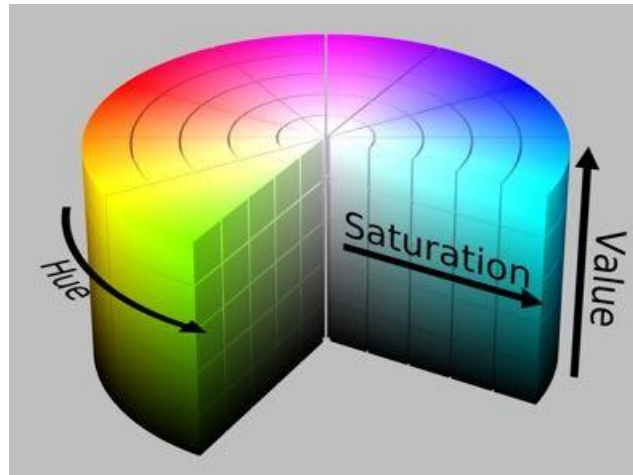
- Changement de color space
- Thresholding
- Egalisation d'histogramme
- Flou
- Morphologie mathématique

# Représentation des images

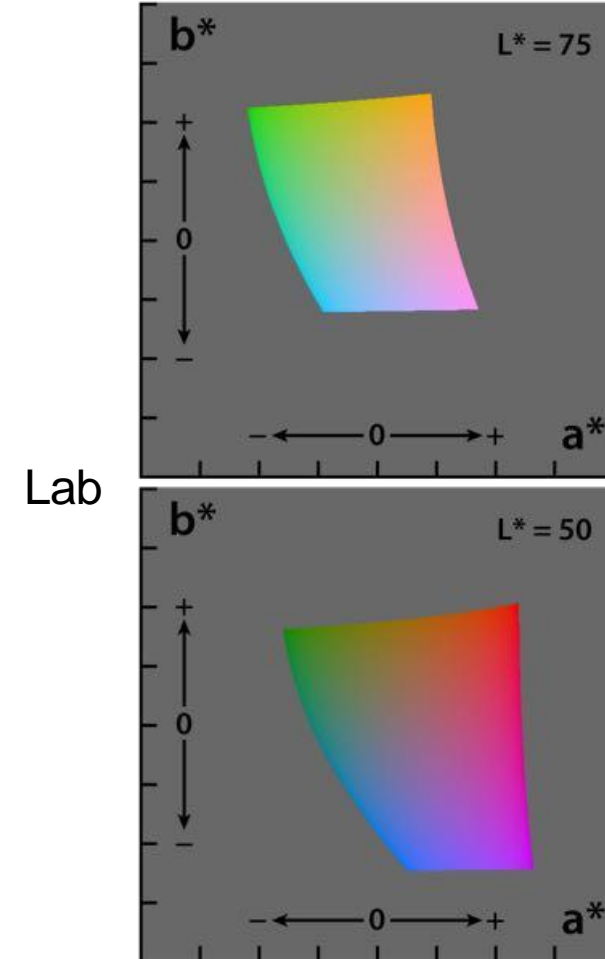
## Espaces colorimétriques



RGB



HSV



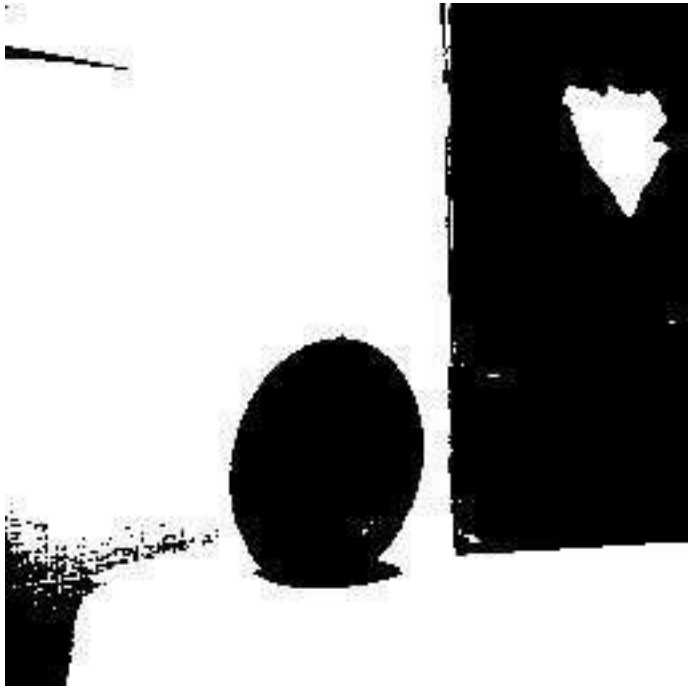
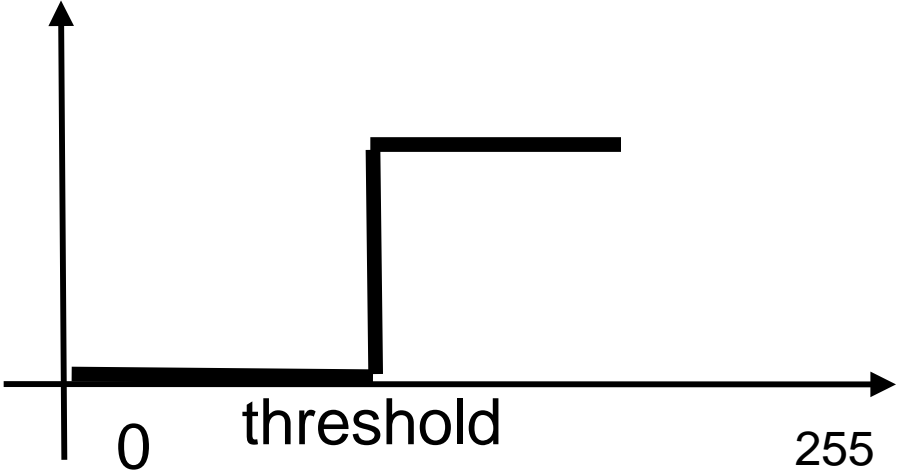
Lab

# Binarisation

Input image



T. Chateau



# Detections de contours

# Detections de contours

En 2D

– Masques de Sobel

Dérivée selon x :  $I_x$

$$H_1 = \frac{1}{8} \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$



Dérivée selon y :  $I_y$

$$H_2 = \frac{1}{8} \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

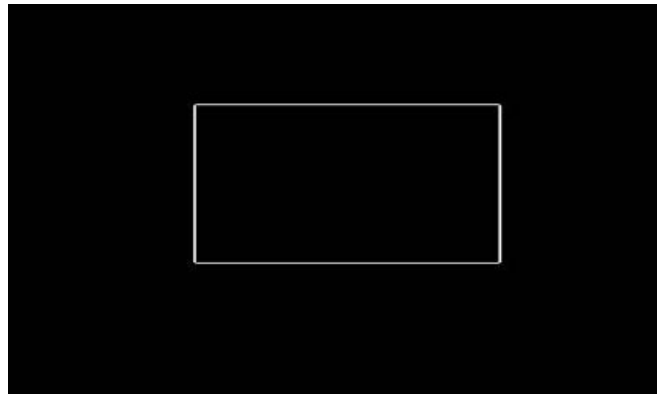




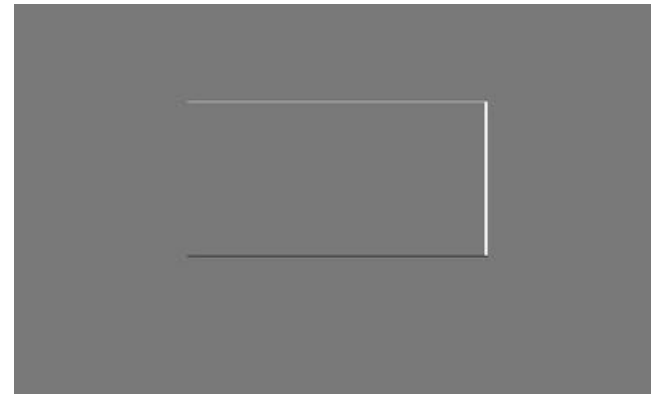
# Detections de contours

## Estimation du gradient

– Norme:  $\sqrt{I_x^2 + I_y^2}$



Direction:  $\text{atan2}(I_y, I_x)$



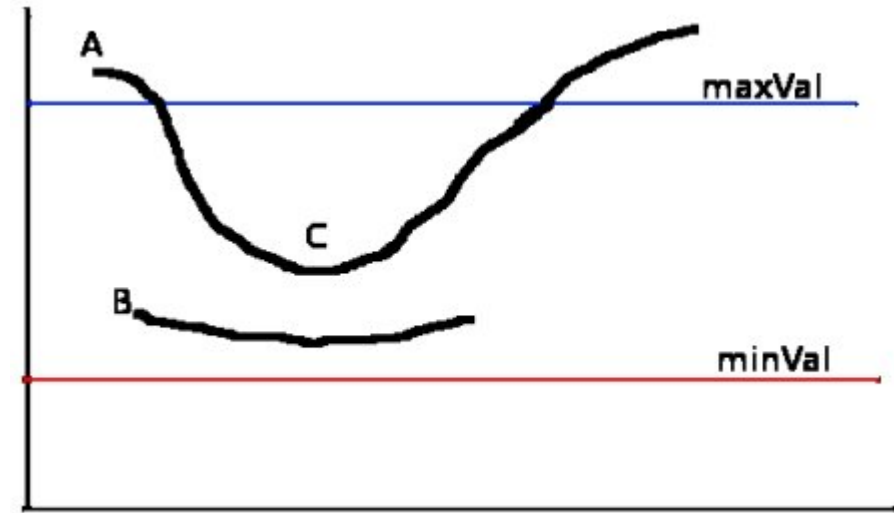
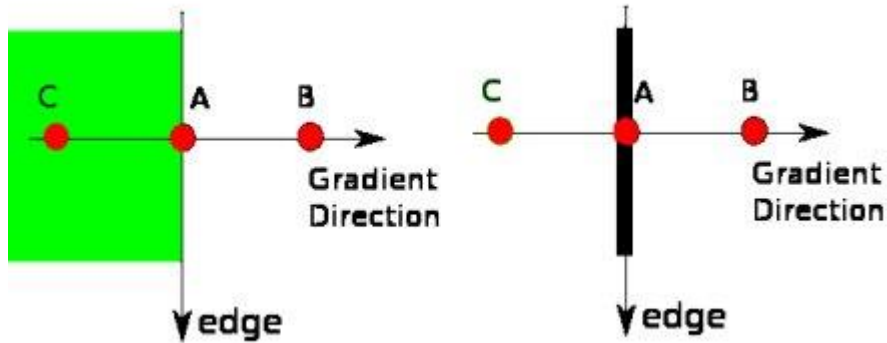
# Détections de contours

- Définition
  - Extremas du gradient dans la direction du gradient
  - Zéros du Laplacien
- Filtrage du gradient
  - Suppression des non maxima dans la direction du gradient



# Détections de contours : Méthode de Canny

- Suppression du bruit
- Calcul gradient Sobel
- Non maximum suppression
- Seuillage à hysteresis



# Détections de contours : Méthode de Canny

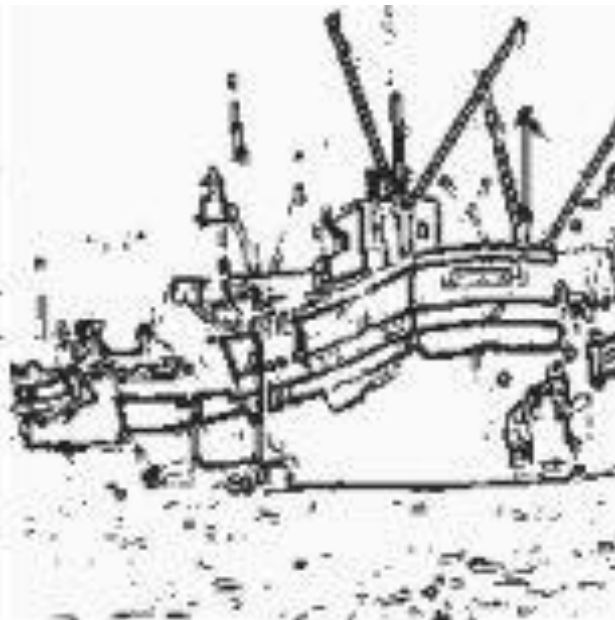
## Seuillage par hystérésis

- Gradients  $> s_1$ , connectés à des gradients  $> s_2$

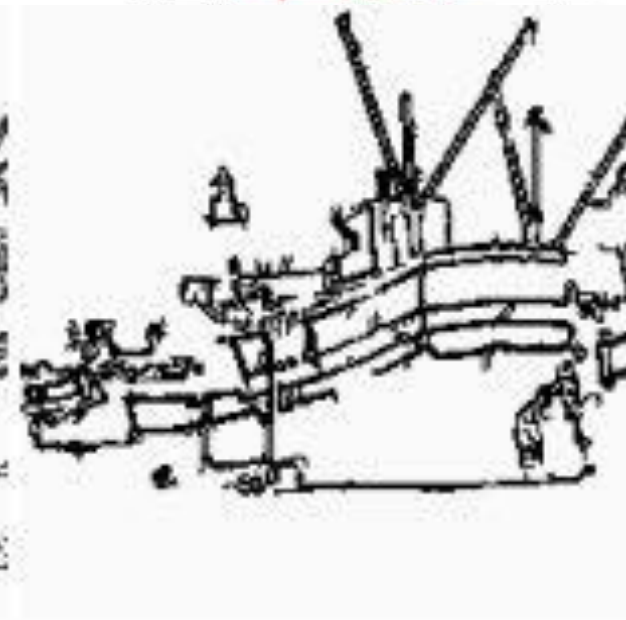
Seuil haut (72 %)



Seuil bas (60 %)



Hystérésis

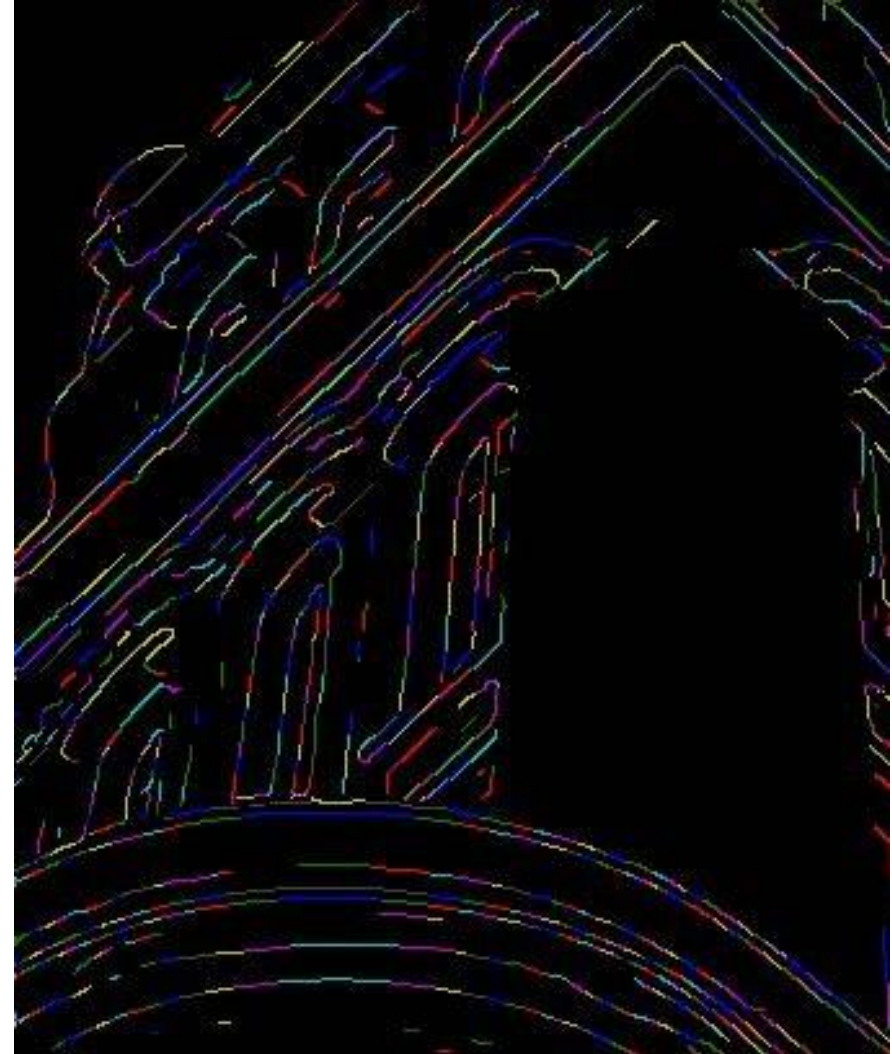




# Détections de contours : Méthode de Canny



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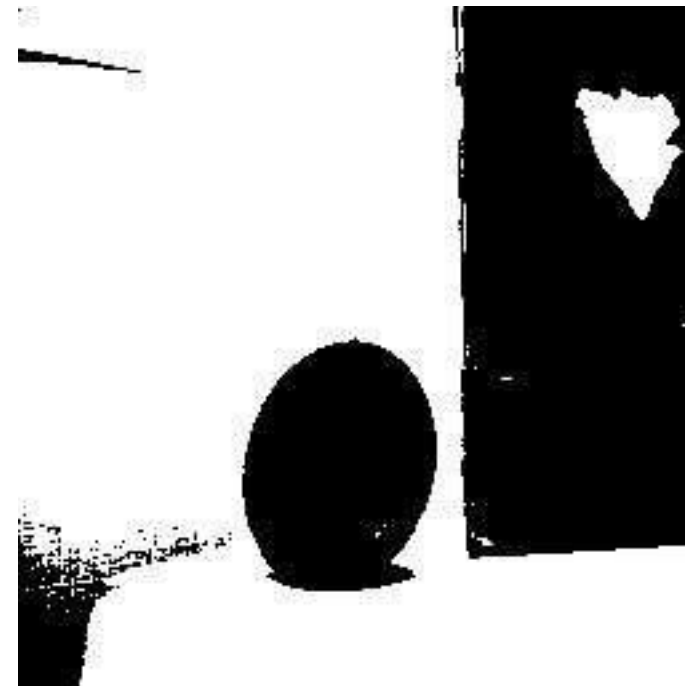
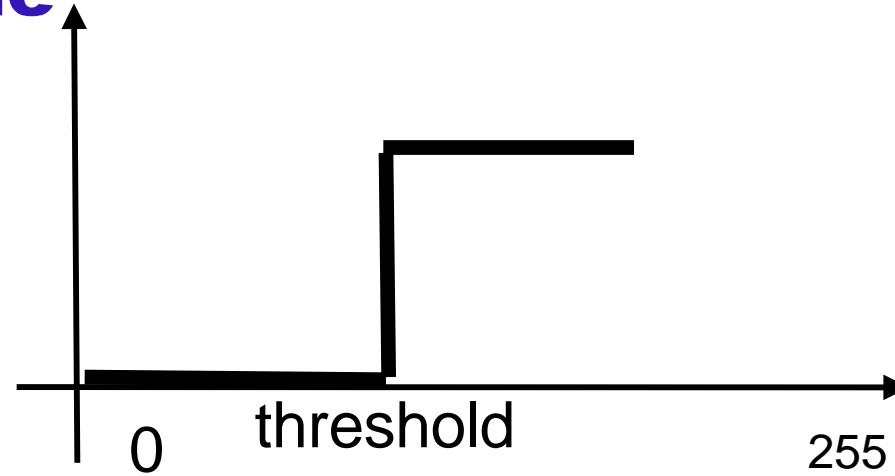
SAR - Vision et perception pour la robotique

# Egalisation d'histogramme

Input image

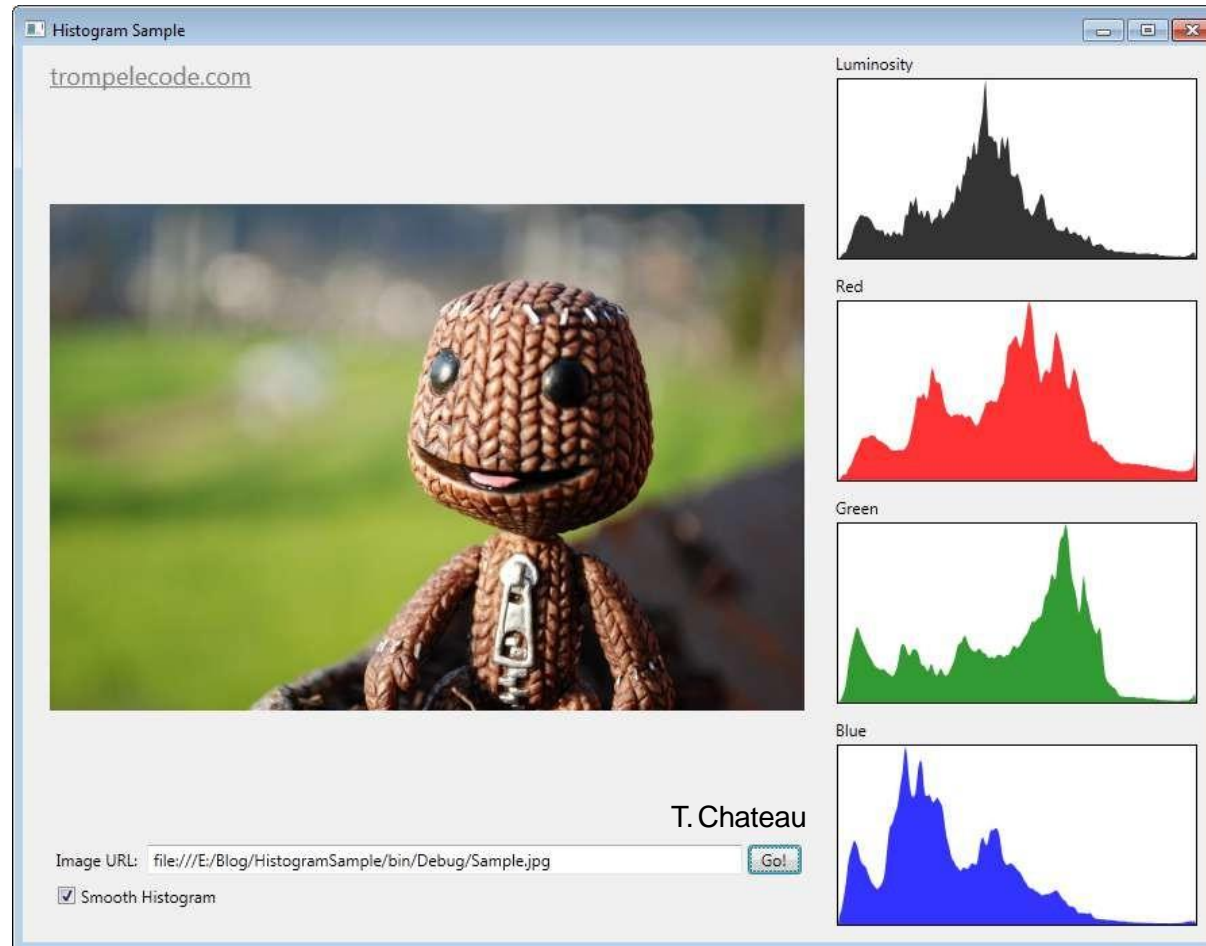


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# Egalisation d'histogramme

$$H(x) = \text{Card}\{\mathbf{p} : I(\mathbf{p}) = x\}$$



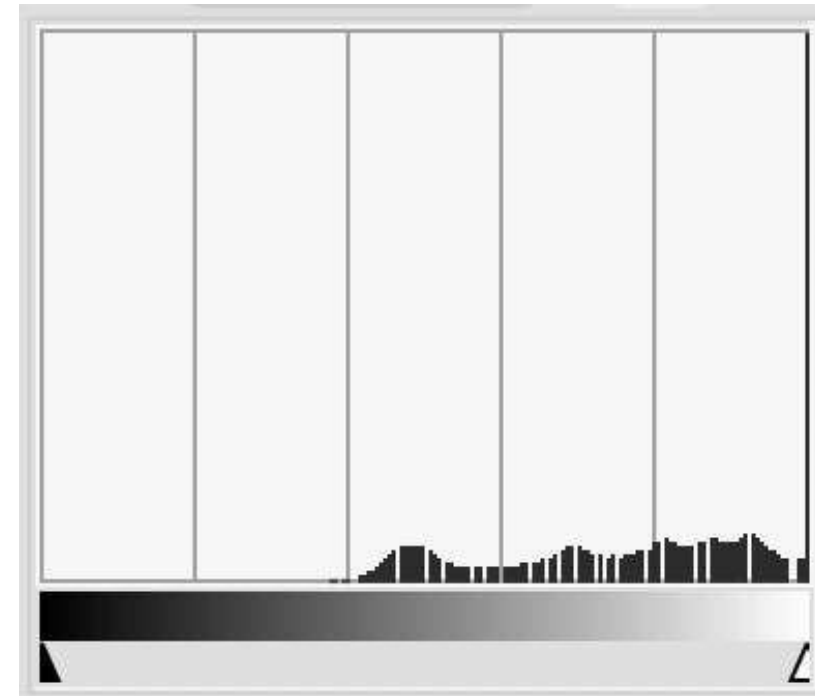


# Histogramme



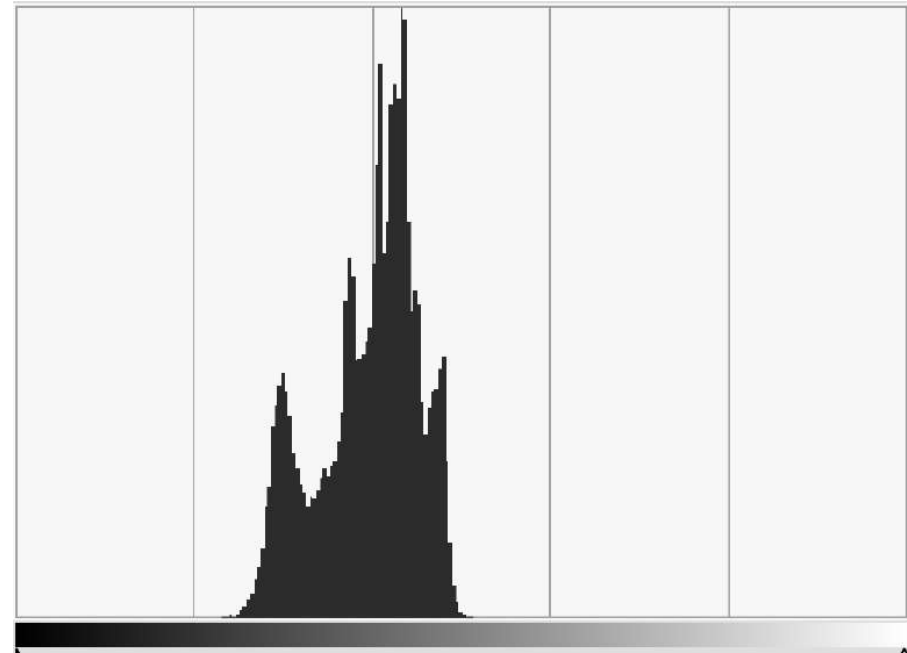
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# Histogramme

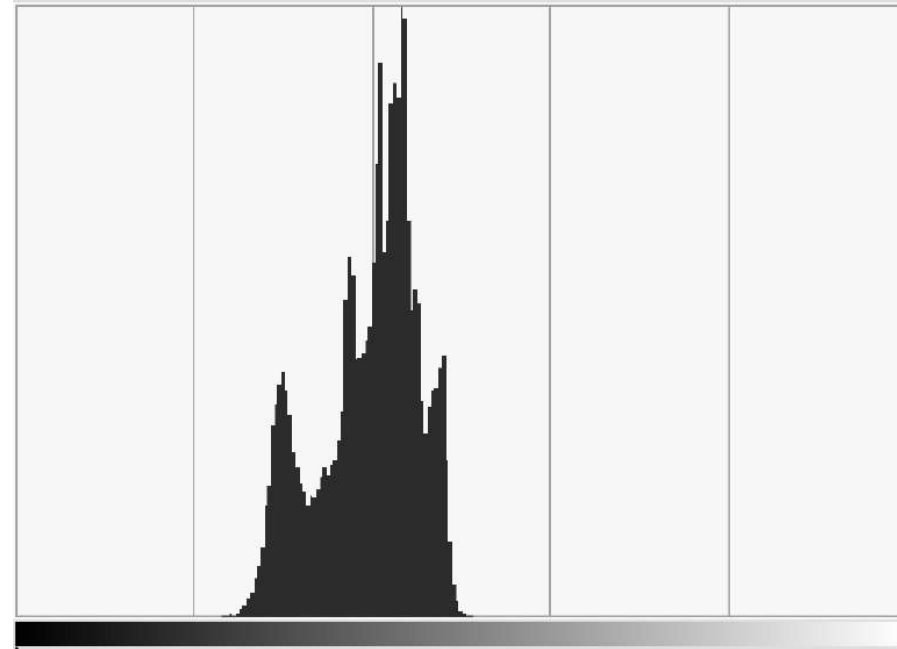
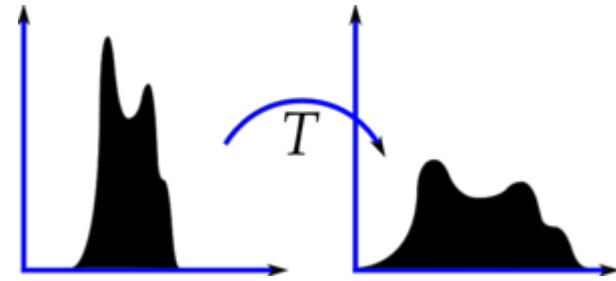


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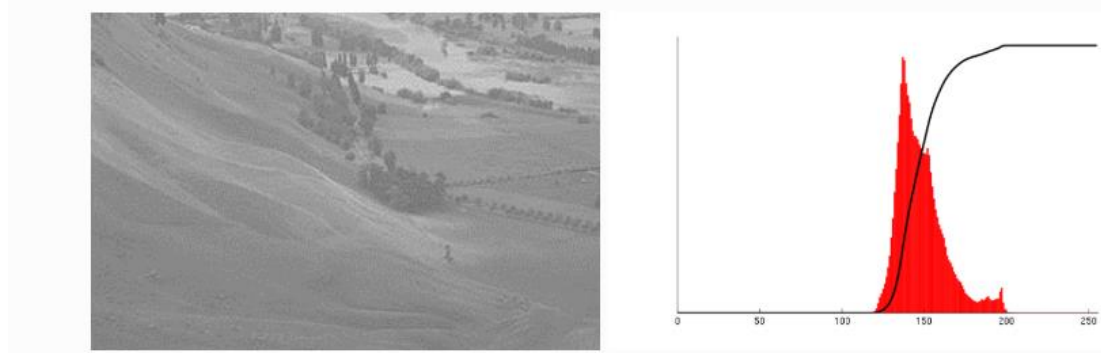
# Histogramme



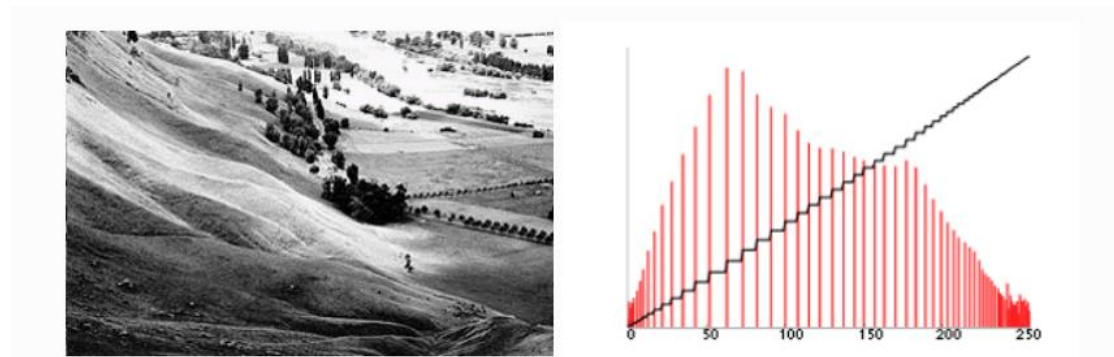
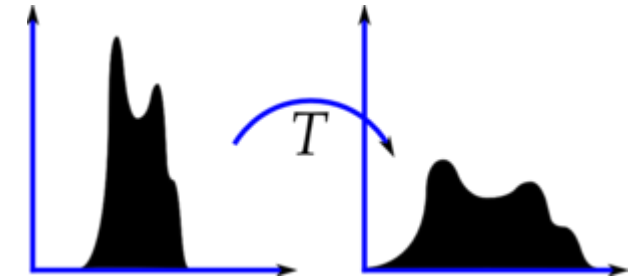
# Egalisation d'histogramme



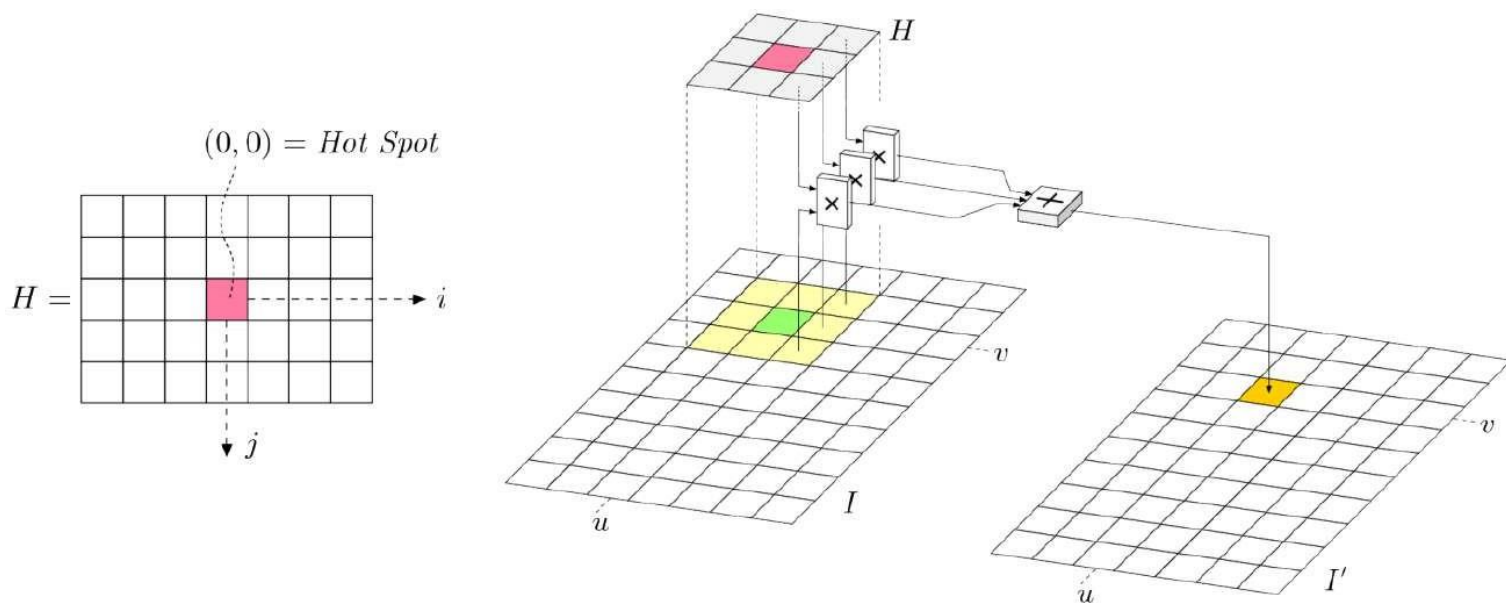
# Egalisation d'histogramme



$$\forall v \in [0..n], eg(v) = \frac{V_{max} - V_{min}}{N} C_f(v) + V_{min}$$



# Filtrage par convolution



10	5	3
4	5	1
1	1	7

Local image data

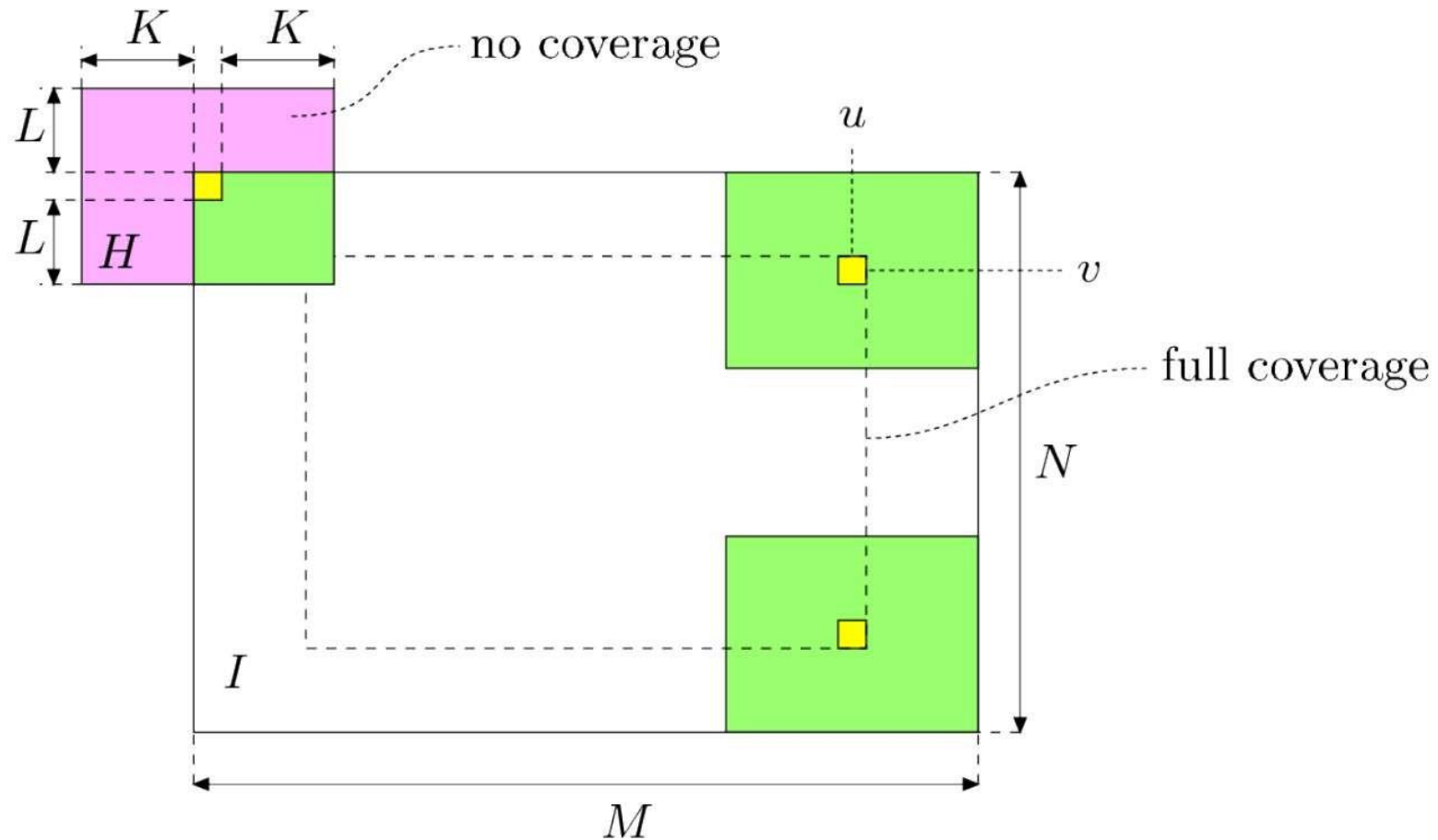
0	0	0
0	0.5	0
0	1	0.5

kernel

	7	

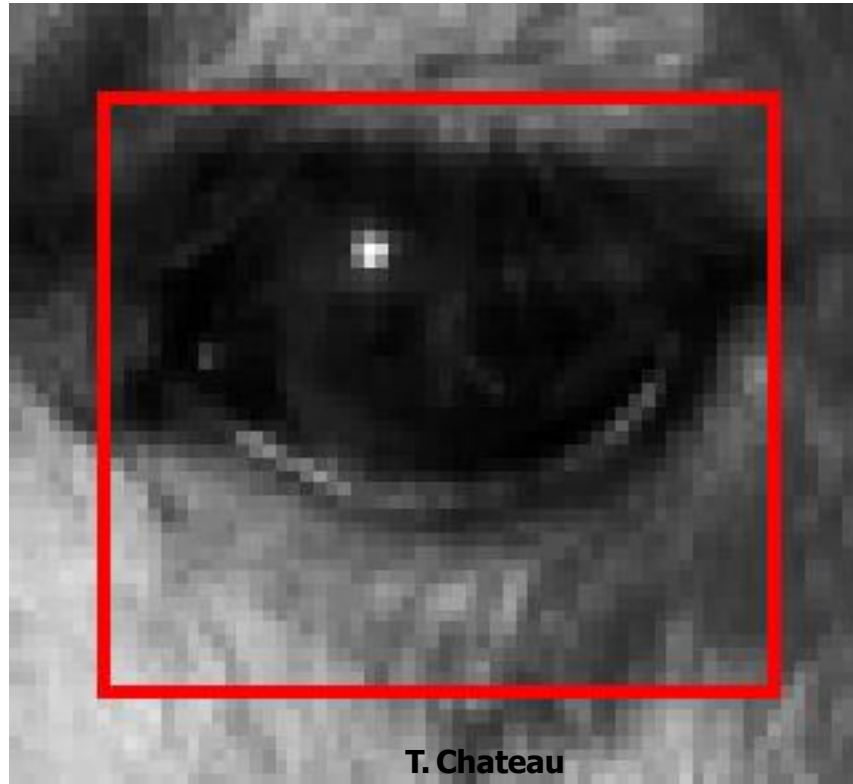
Modified image data

## How to cope with image boundary?





## Filtrage par convolution : Crop



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# Filtrage par convolution : PAD

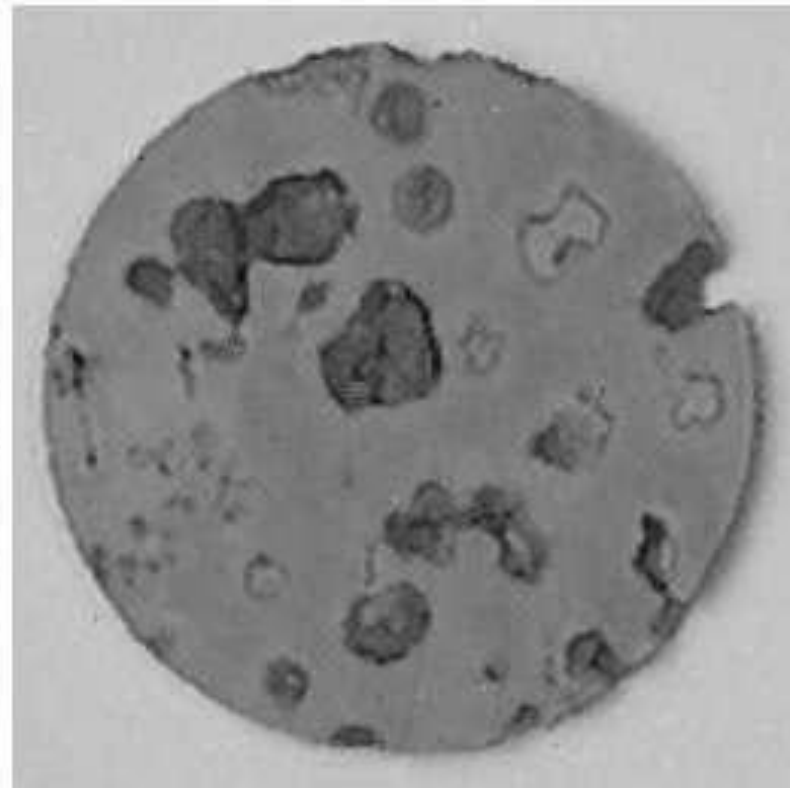
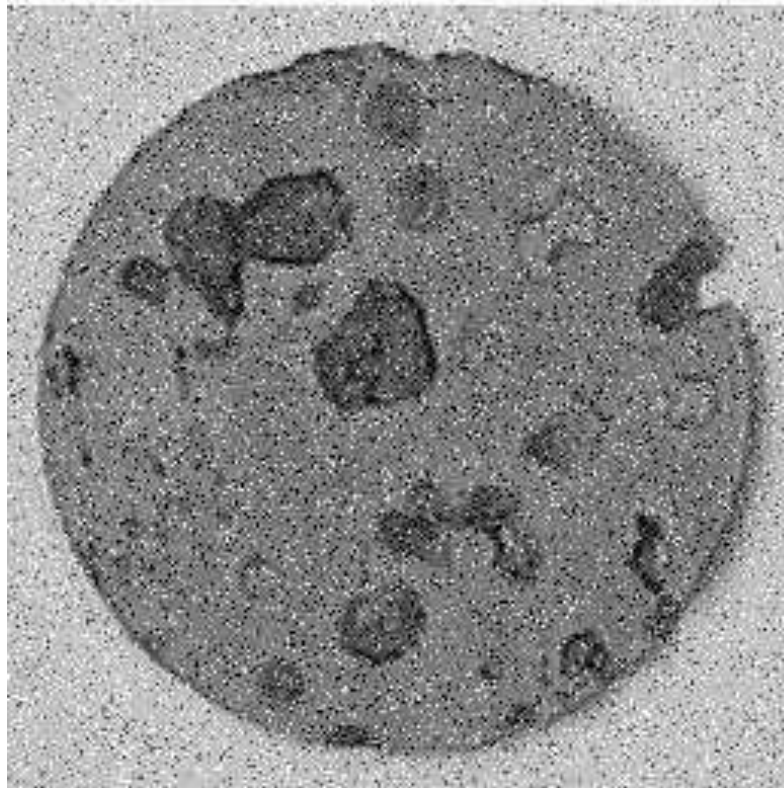


## **Filtrage médian ( Bruit poivre et sel )**

- Robuste
- Non-lineaire
- Chaque pixel est modifié selon la valeur médiane de son voisinage

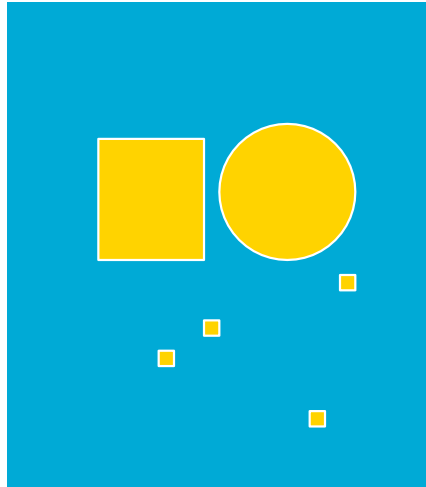
## Filtrage par convolution : Filtre médian

MEDIAN FILTER

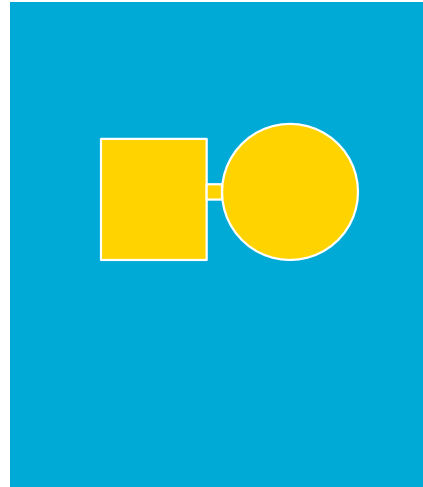


# Binary image filtering: Mathematical morphology

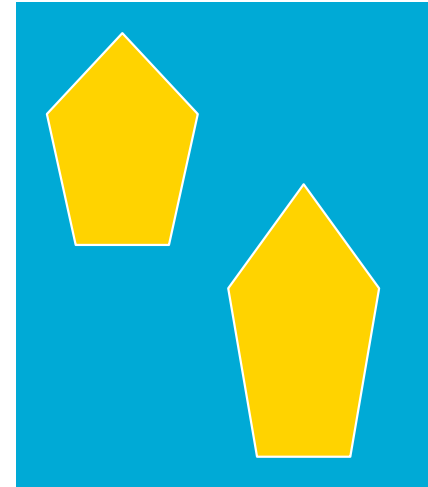
What can we do with MM ?



Remove noise



separate shapes



compare shapes

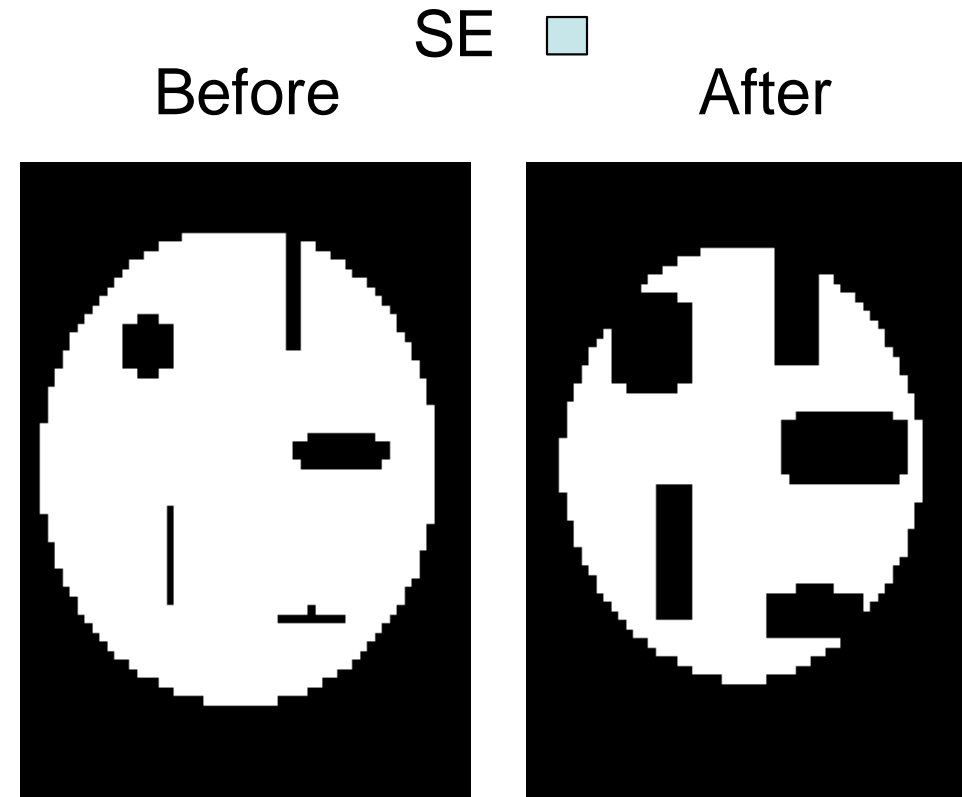
# Binary image filtering:

## Mathematical morphology

- Main idea: probe an image with a simple, pre- defined shape, drawing conclusions on how this shape fits or misses the shapes in the image.
- This simple "probe" is called structuring element, and is itself a binary image (i.e., a subset of the space or grid).

# Binary image filtering: Mathematical morphology

## Basic operators: erosion

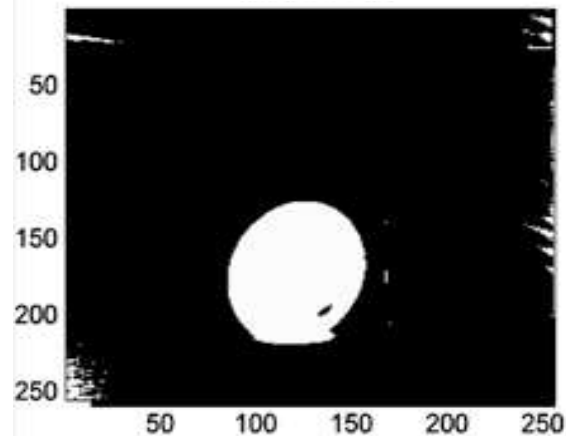




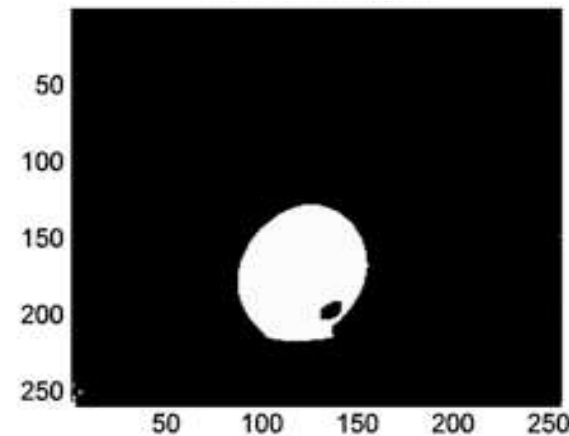
# Binary image filtering: Mathematical morphology



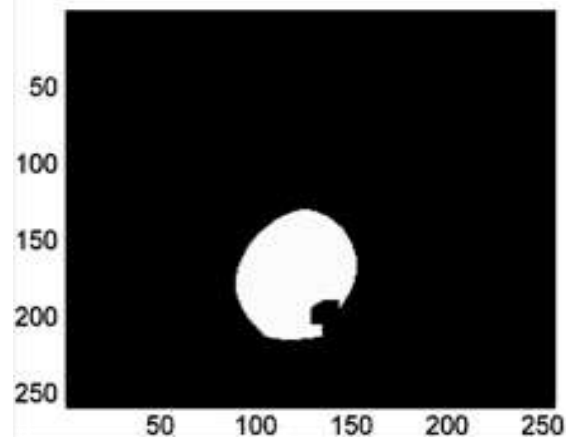
Initial image



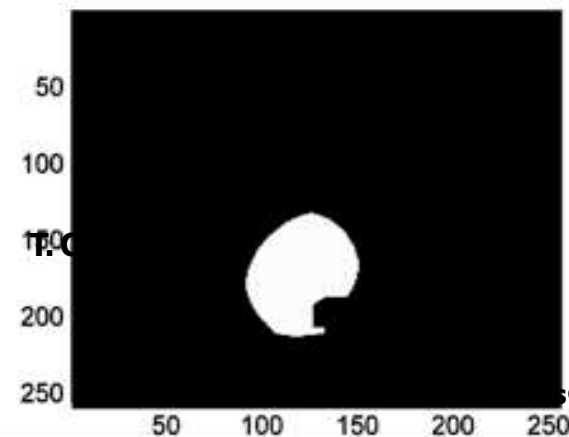
eroded 1 time



eroded 2 times



eroded 3 times



# Binary image filtering: Mathematical morphology

## Basic operators: dilation

SE ■ Before

After

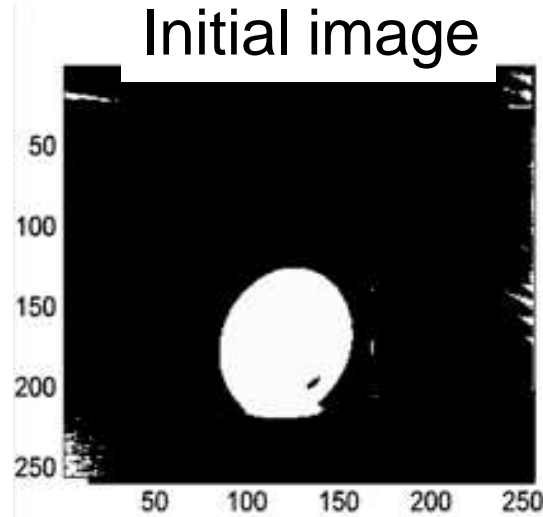


# Binary image filtering: Mathematical morphology

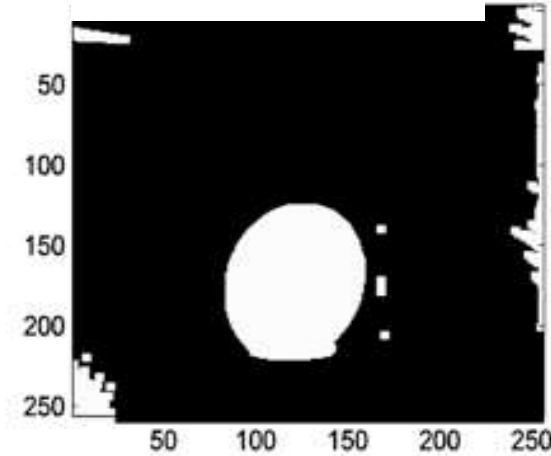
Example



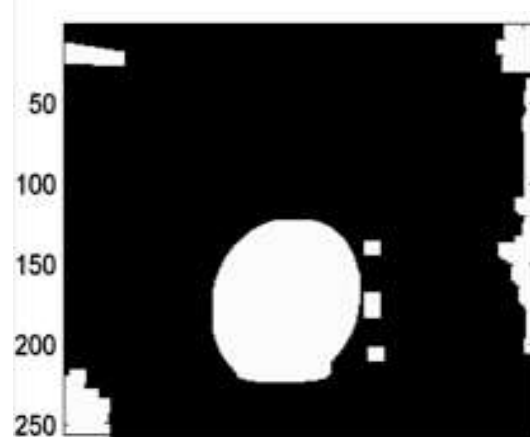
Initial image



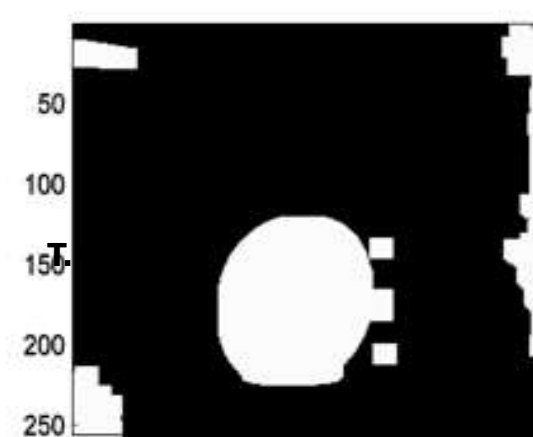
dilated 1 time



dilated 2 times

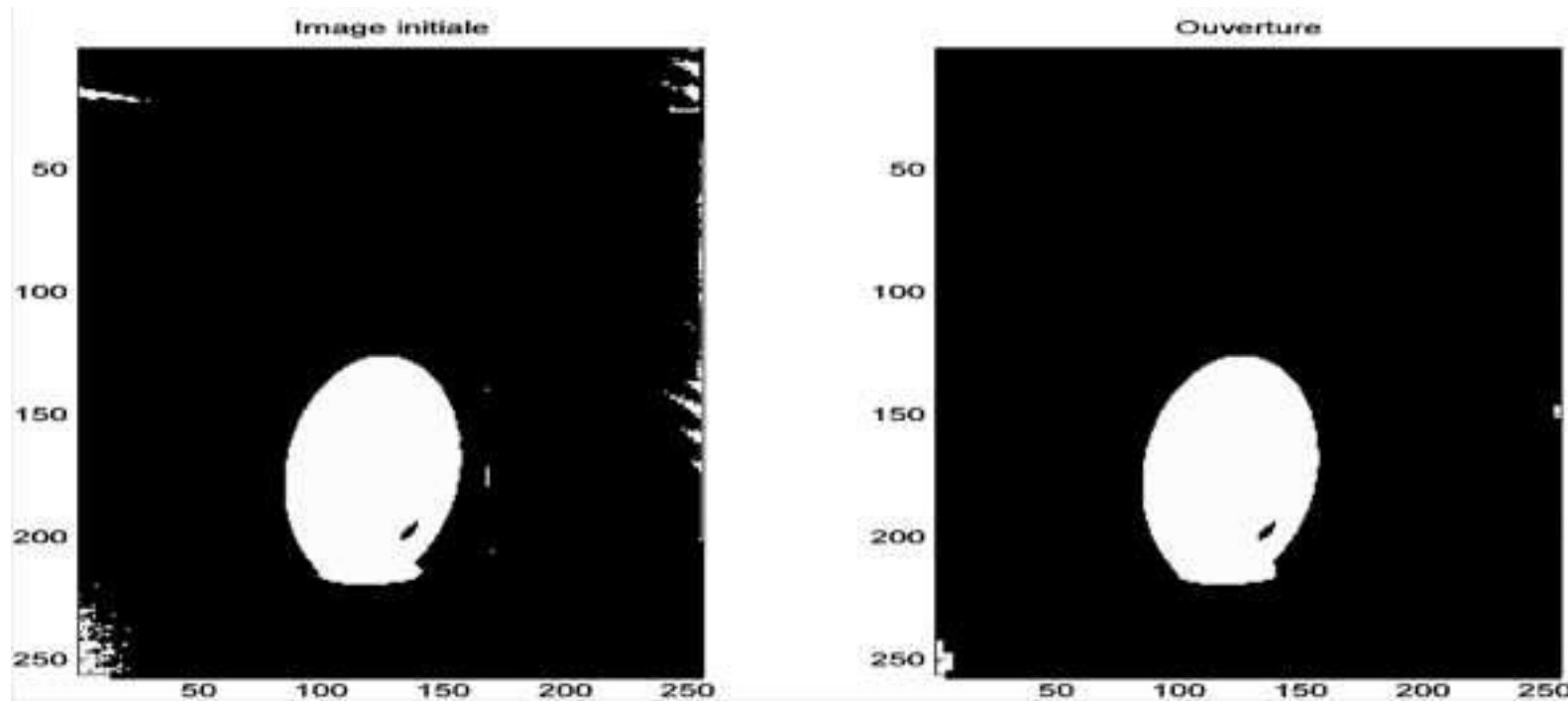


dilated 3 times



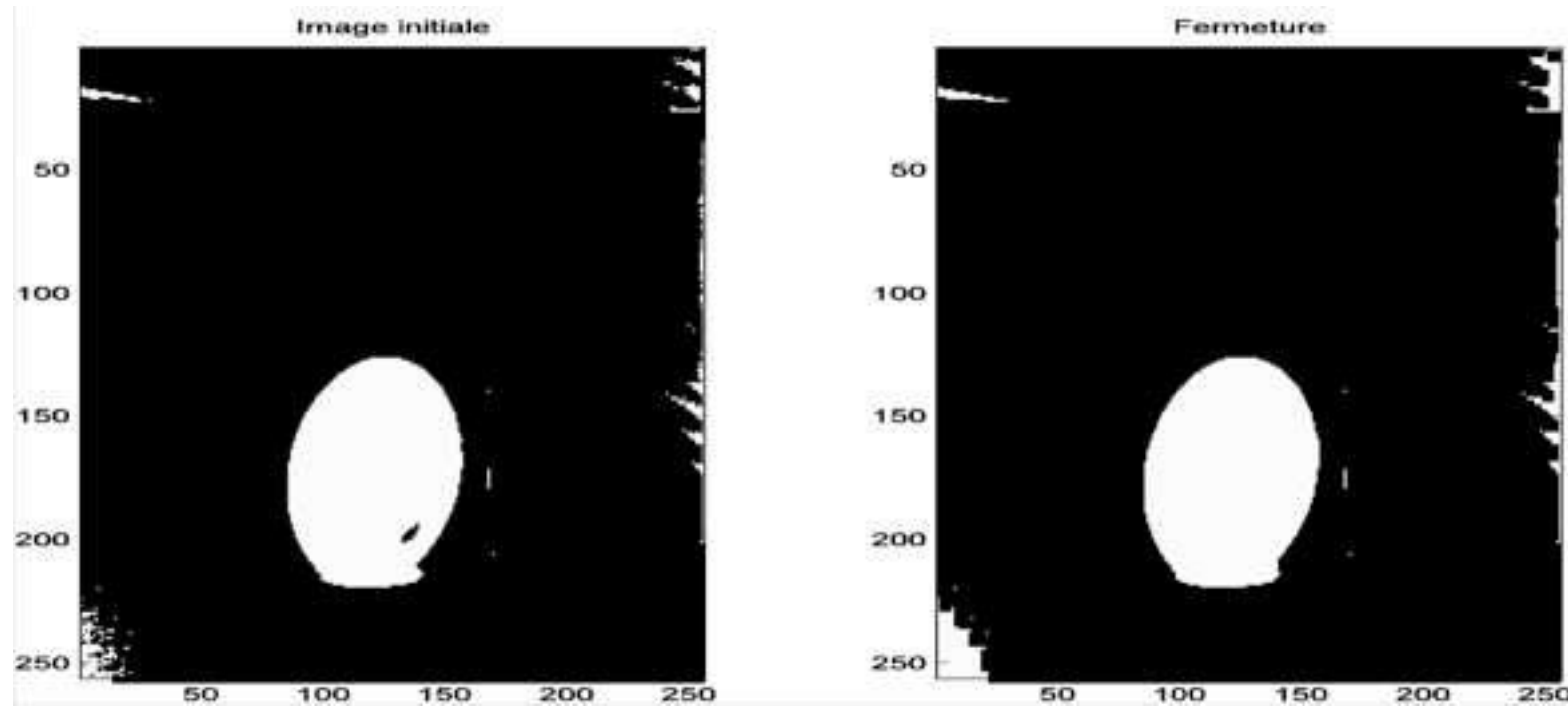
# Binary image filtering: Mathematical morphology

## Basic operators: ouverture

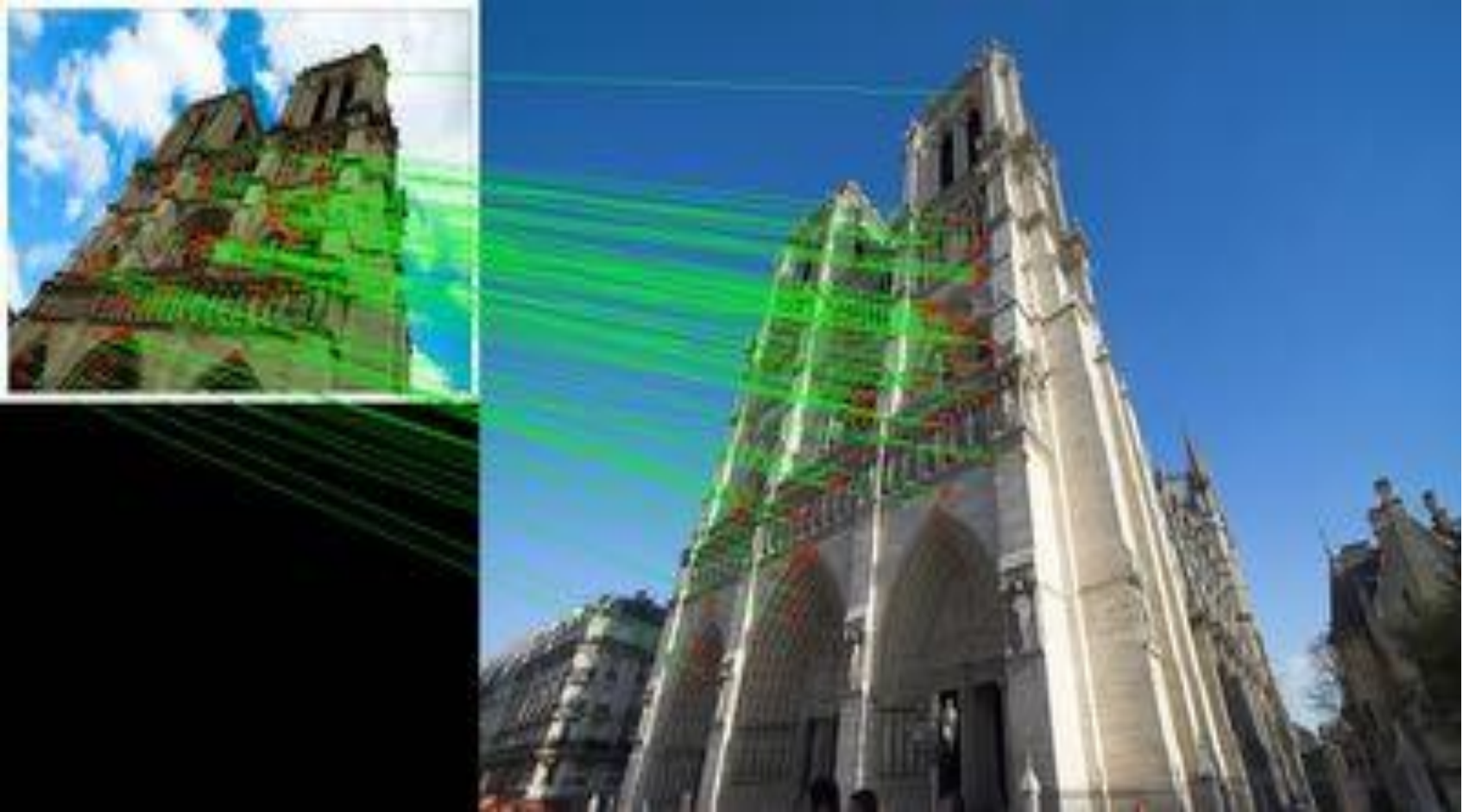


# Binary image filtering: Mathematical morphology

Basic operators:  
fermeture



Un concept important : La  
représentation



- On veut raisonner sur une image
- Il nous faut trouver des descripteurs
- Pour avoir une représentation
  - Identifiables dans plusieurs images
  - Reconnaissables / mouvement caméra
  - Robustes aux changements de d'éclairage
  - Robustes aux déformations liées au mouvement



# Comparaison de points

## Trouver le point le plus similaire

- Hypothèse de décalage en translation

Comment comparer  $I_1(x_1, y_1)$  et  $I_2(x_2, y_2)$  ?



Robustesse changement luminosité / contraste ?

# Comparaison de points

## Sum of Squared Differences

$$SSD(I_1, x_1, y_1, I_2, x_2, y_2) = \sum_{i=-n}^n \sum_{j=-p}^p (I_1(x_1 + i, y_1 + j) - I_2(x_2 + i, y_2 + j))^2$$

## Cross corrélation

– Invariance / luminosité et contraste

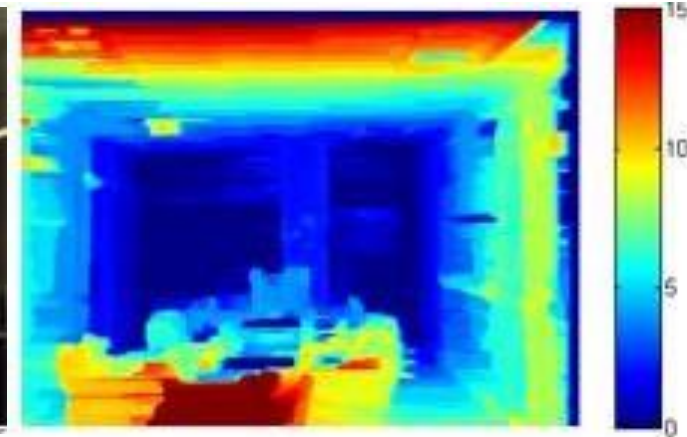
$$NCC(I_1, x_1, y_1, I_2, x_2, y_2) = \frac{\sum_{i,j} (I_1(x_1 + i, y_1 + j) - \overline{I_1(x_1, y_1)}) (I_2(x_2 + i, y_2 + j) - \overline{I_2(x_2, y_2)})}{\sqrt{\sum_{i,j} (I_1(x_1 + i, y_1 + j) - \overline{I_1(x_1, y_1)})^2 \sum_{i,j} (I_2(x_2 + i, y_2 + j) - \overline{I_2(x_2, y_2)})^2}}$$

# Application : stéréo-vision

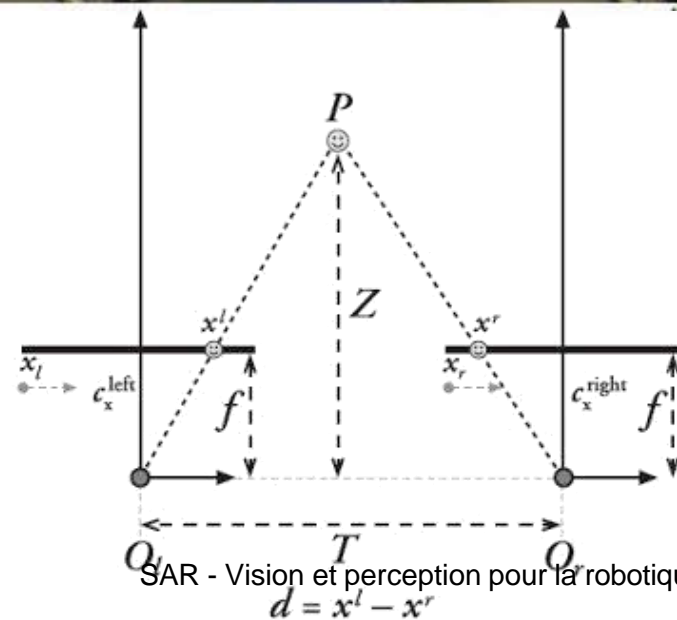
Gauche

Droite

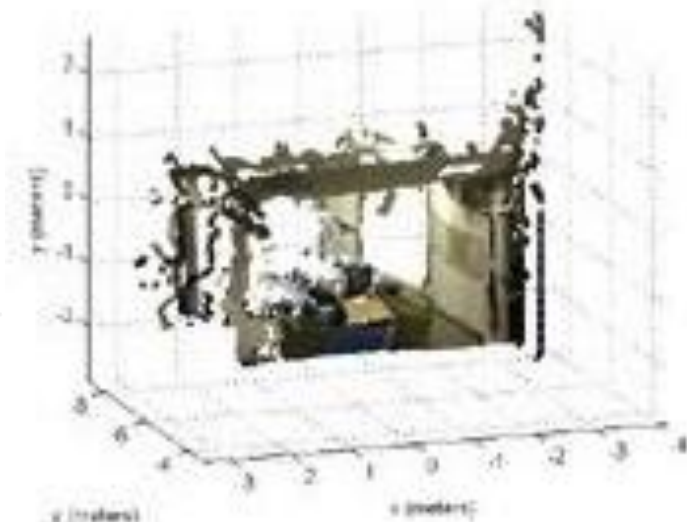
Disparité



Validité ?



SAR - Vision et perception pour la robotique



# Comparaison de points

Trouver le point le plus similaire

– Translation -> SSD

Comment reconnaître un point après rotation ?

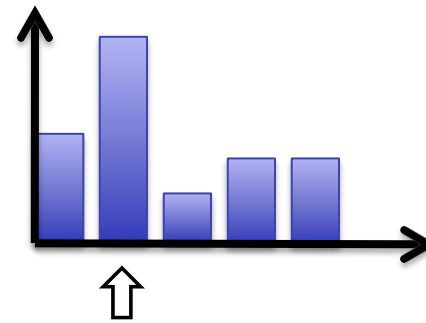
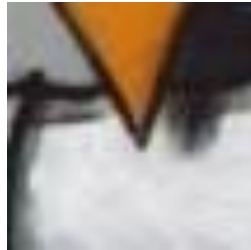




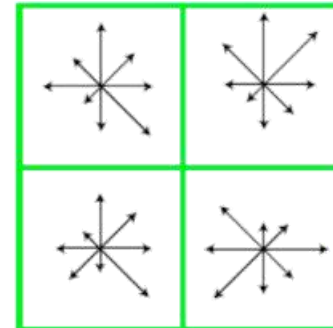
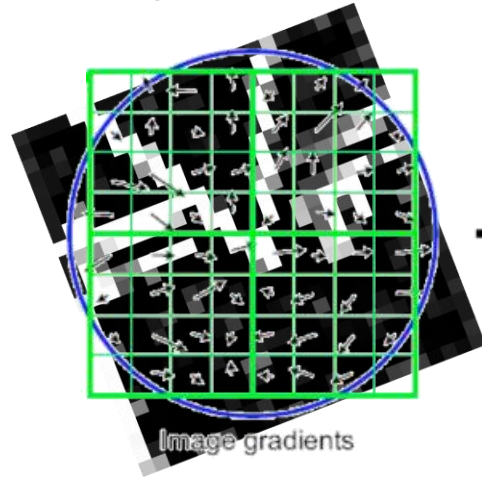
# Descripteurs SIFT [Lowe99]

## Histogramme d'orientation du gradient

- Orientation de référence



- Histogramme des orientations

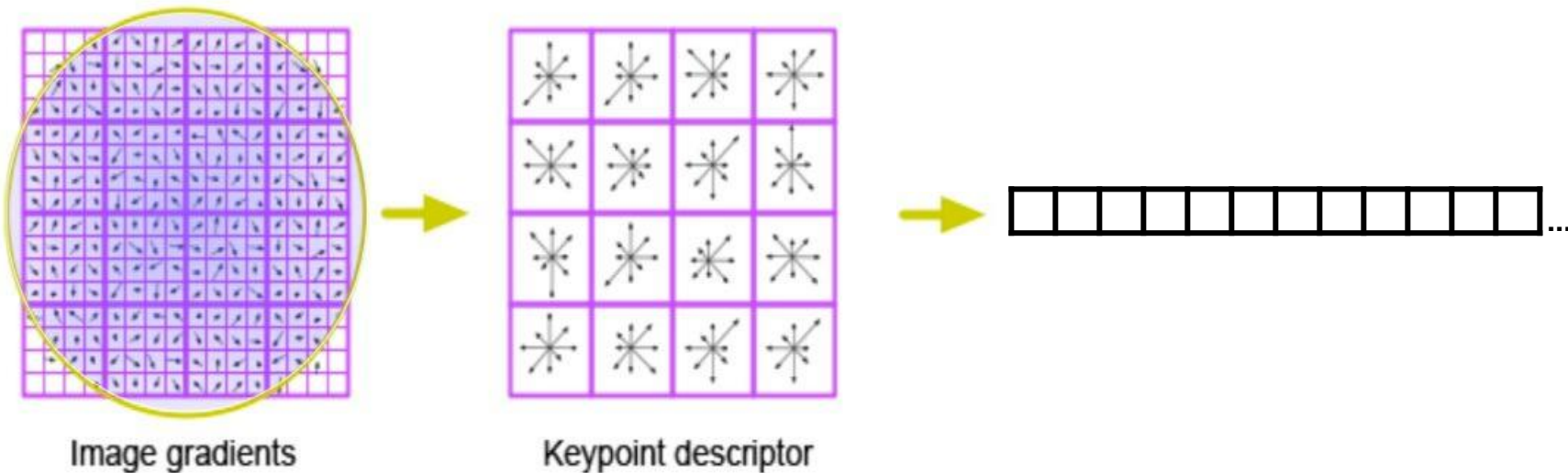


Keypoint descriptor

# Descripteurs SIFT [Lowe99]

## Histogramme d'orientation du gradient

- 4x4 fenêtres
- Histogrammes sur 8 directions
- Pondération gaussienne autour du centre
- Dimension 128



# Invariance au changement d'échelle

Trouver des point similaires quelque soit l'échelle

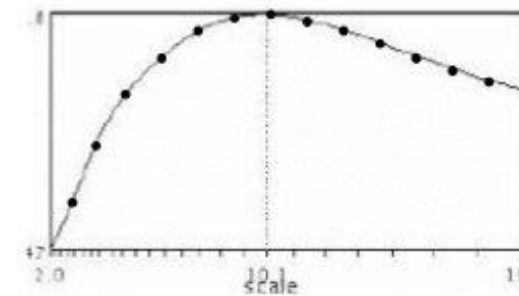
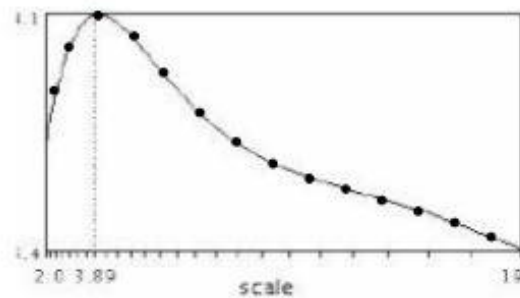
- Translation -> SSD
- Rotation -> orientation de référence

Comment comparer des points à des échelles différentes ?



# Détection d'échelle de référence

Analyse par fonction de signature

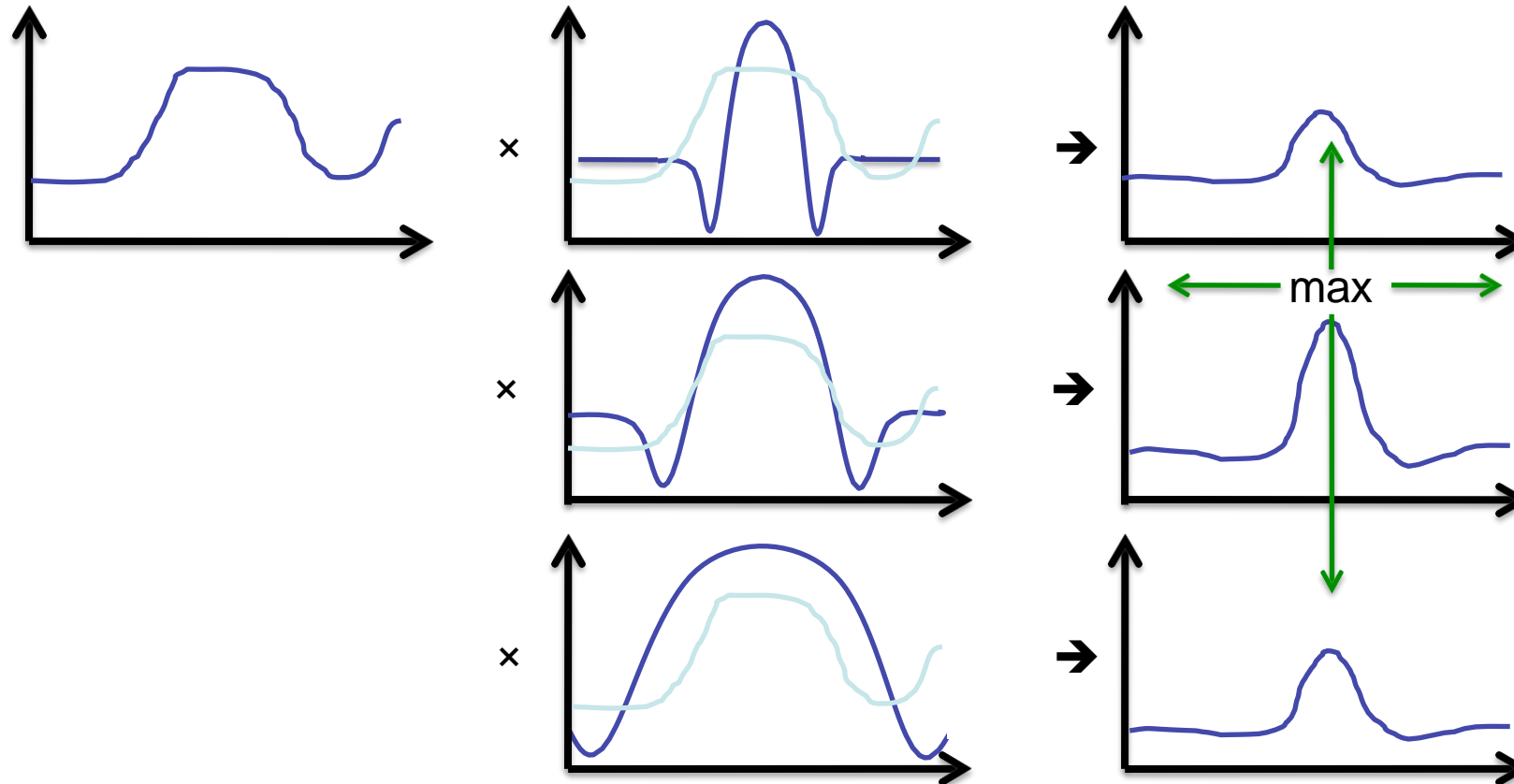




# Détection de « blobs »

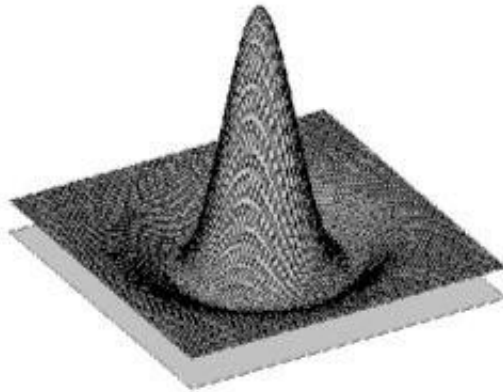
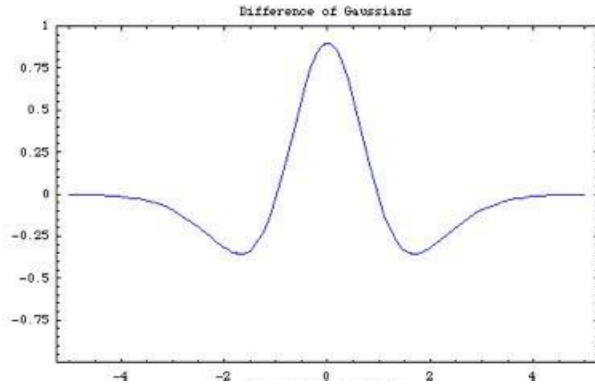
## Détection d'échelle avec fonction en « cloche »

- Recherche de points au centre de « blobs »

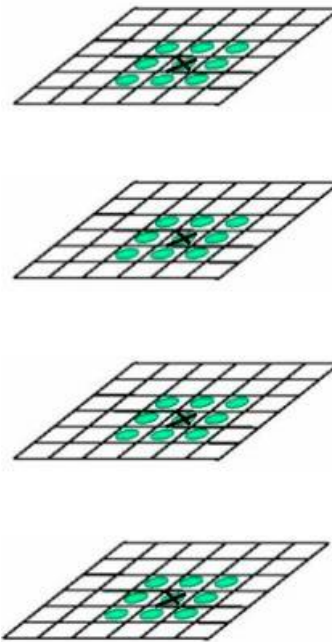


# Détecteur SIFT

Détection par différence de gaussiennes



Convolution

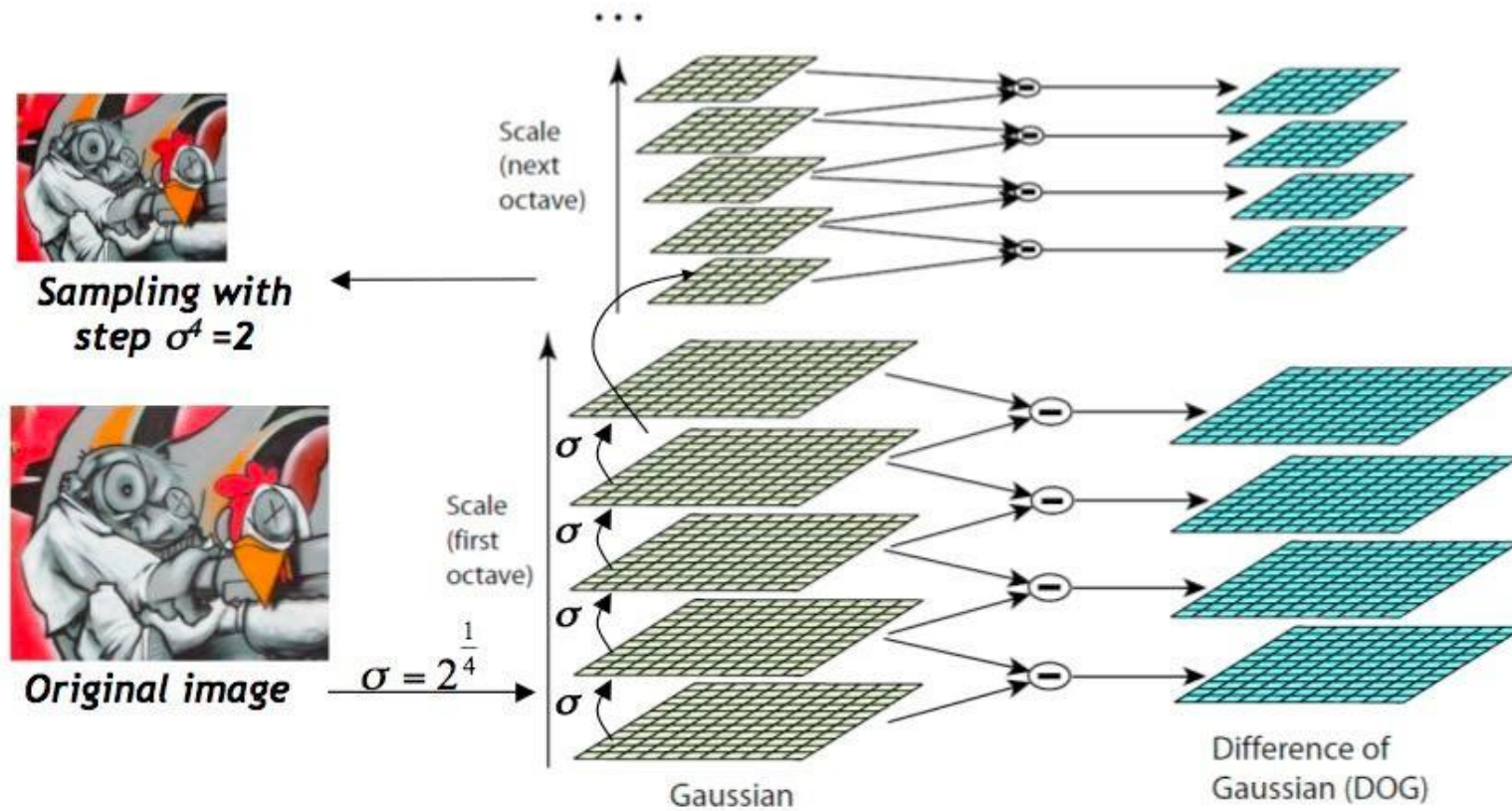


Max échelle/espace



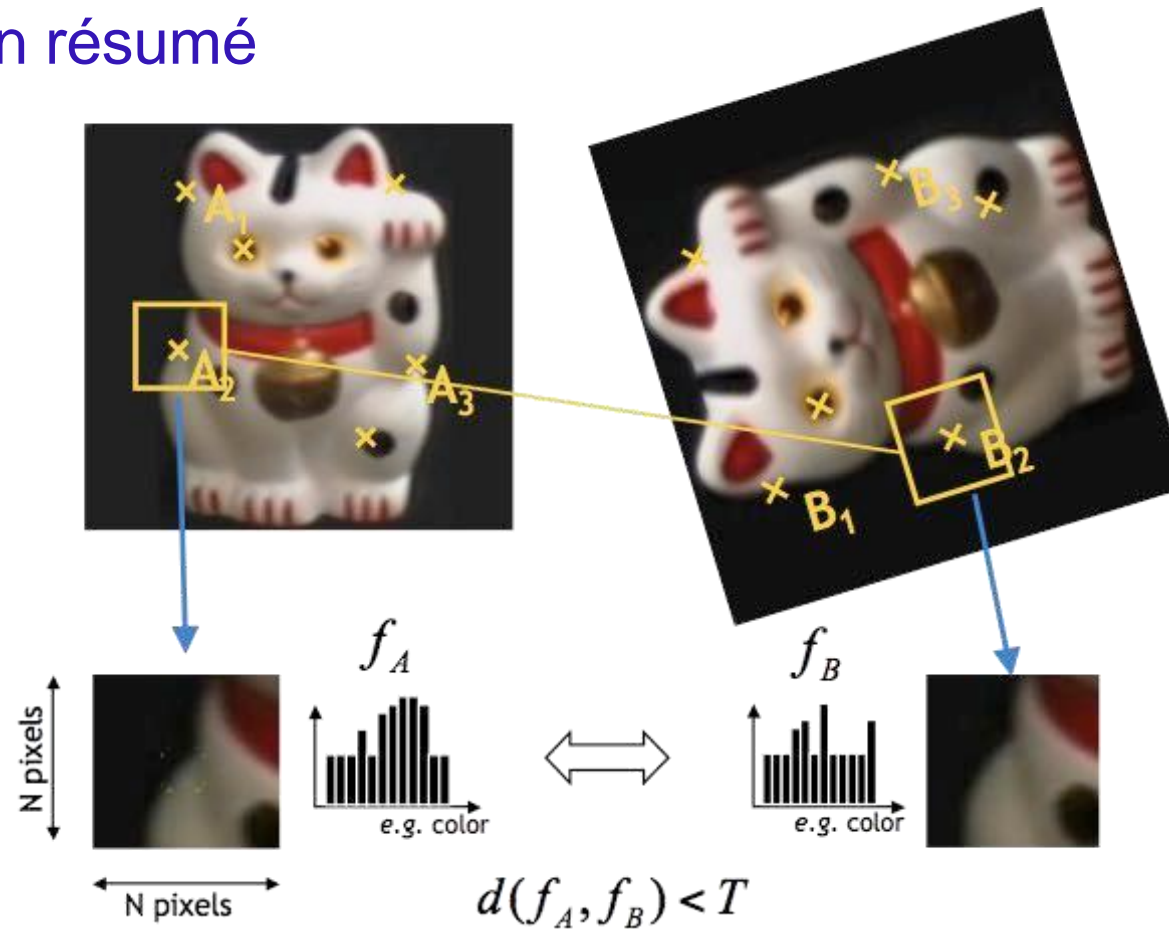
# Détecteur SIFT

## Implémentation optimisée



# Détecteur SIFT

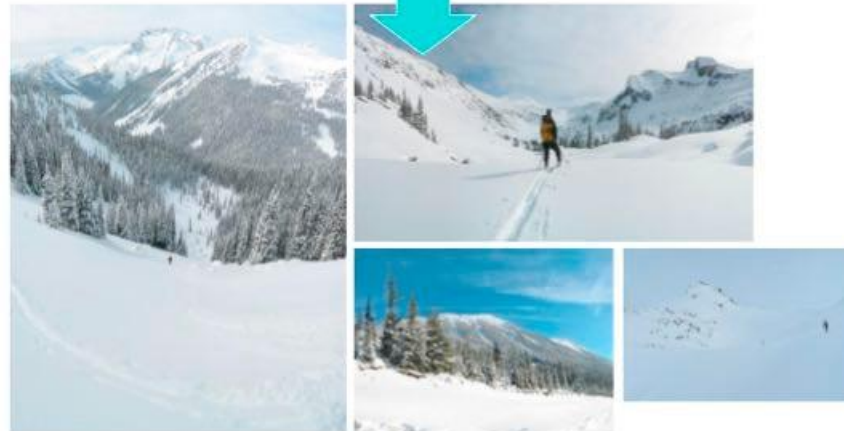
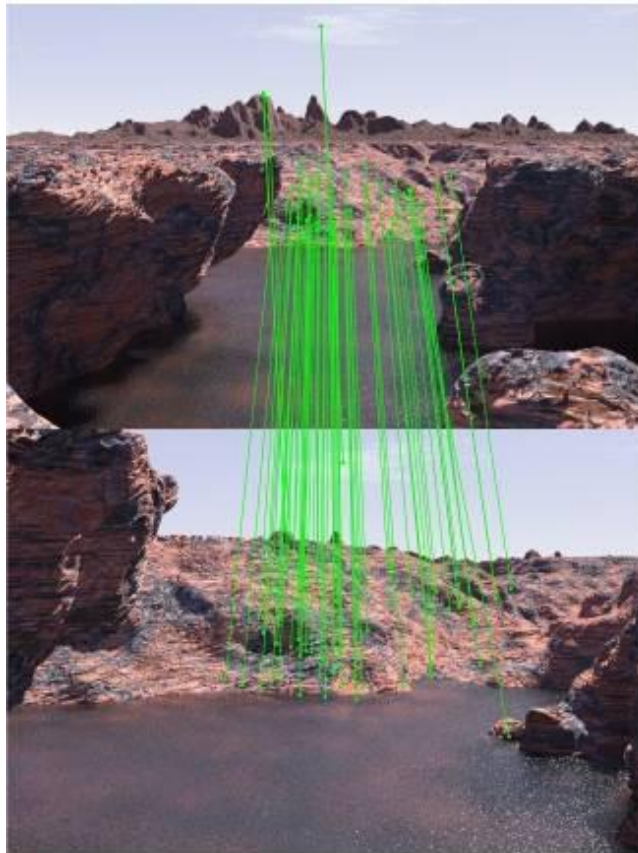
En résumé





# Détecteur SIFT

## Exemples de correspondances

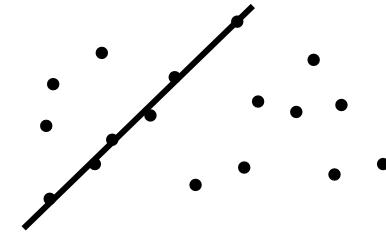


Brown, ICCV 2003

# Hough Transform

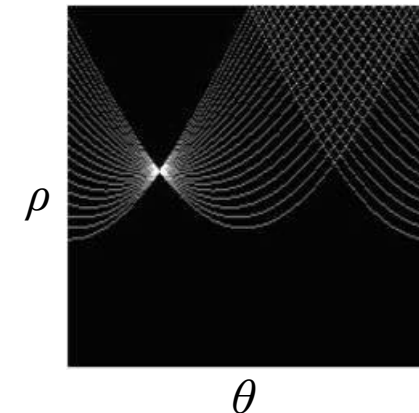
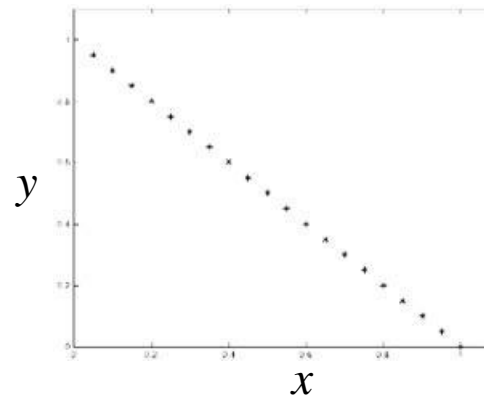
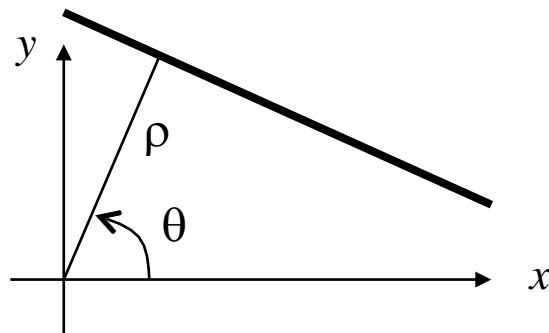
- **Origin: Detection of straight lines in clutter**

- Basic idea: each candidate point votes for all lines that it is consistent with.
- Votes are accumulated in quantized array
- Local maxima correspond to candidate lines

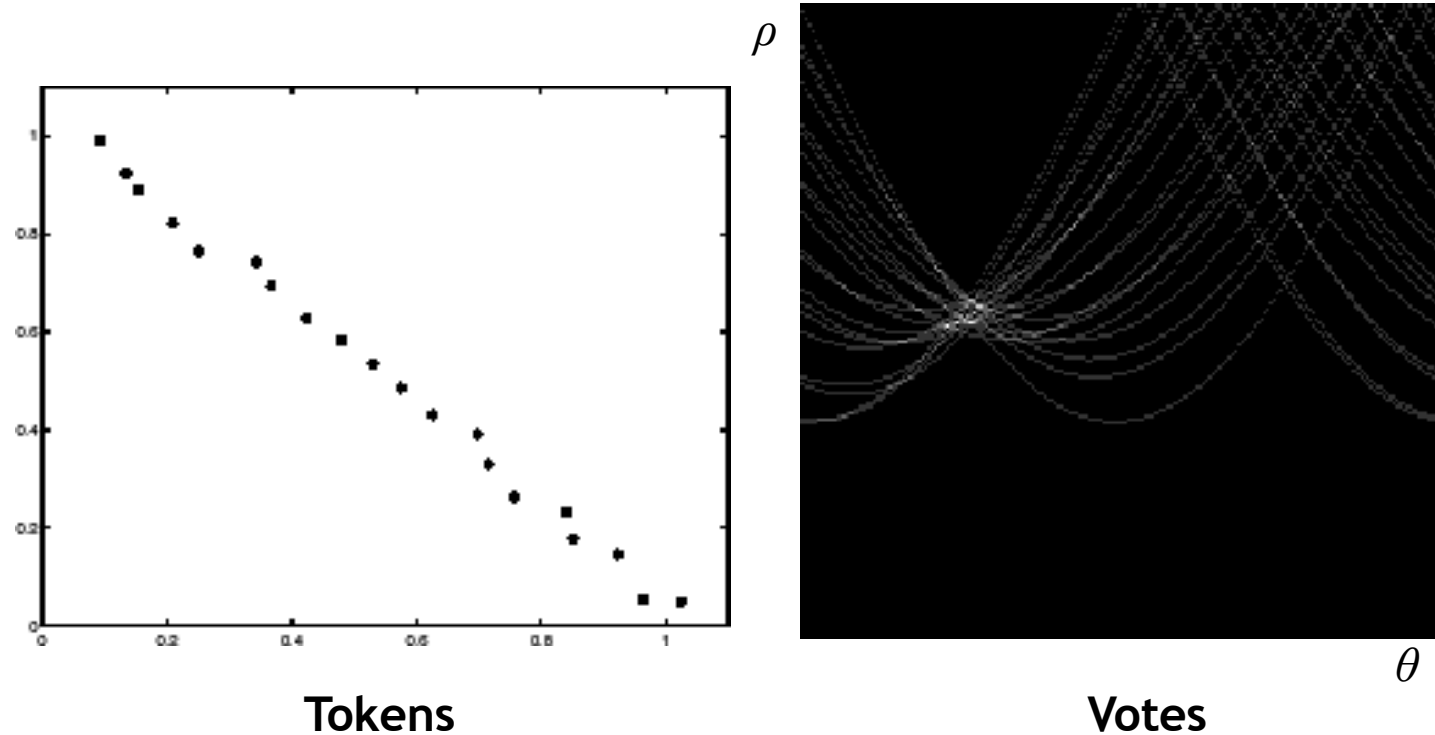


- **Representation of a line**

- Usual form  $y = ax + b$  has a singularity around  $90^\circ$ .
- **Better parameterization:**  $x \cos(\theta) + y \sin(\theta) = \rho$



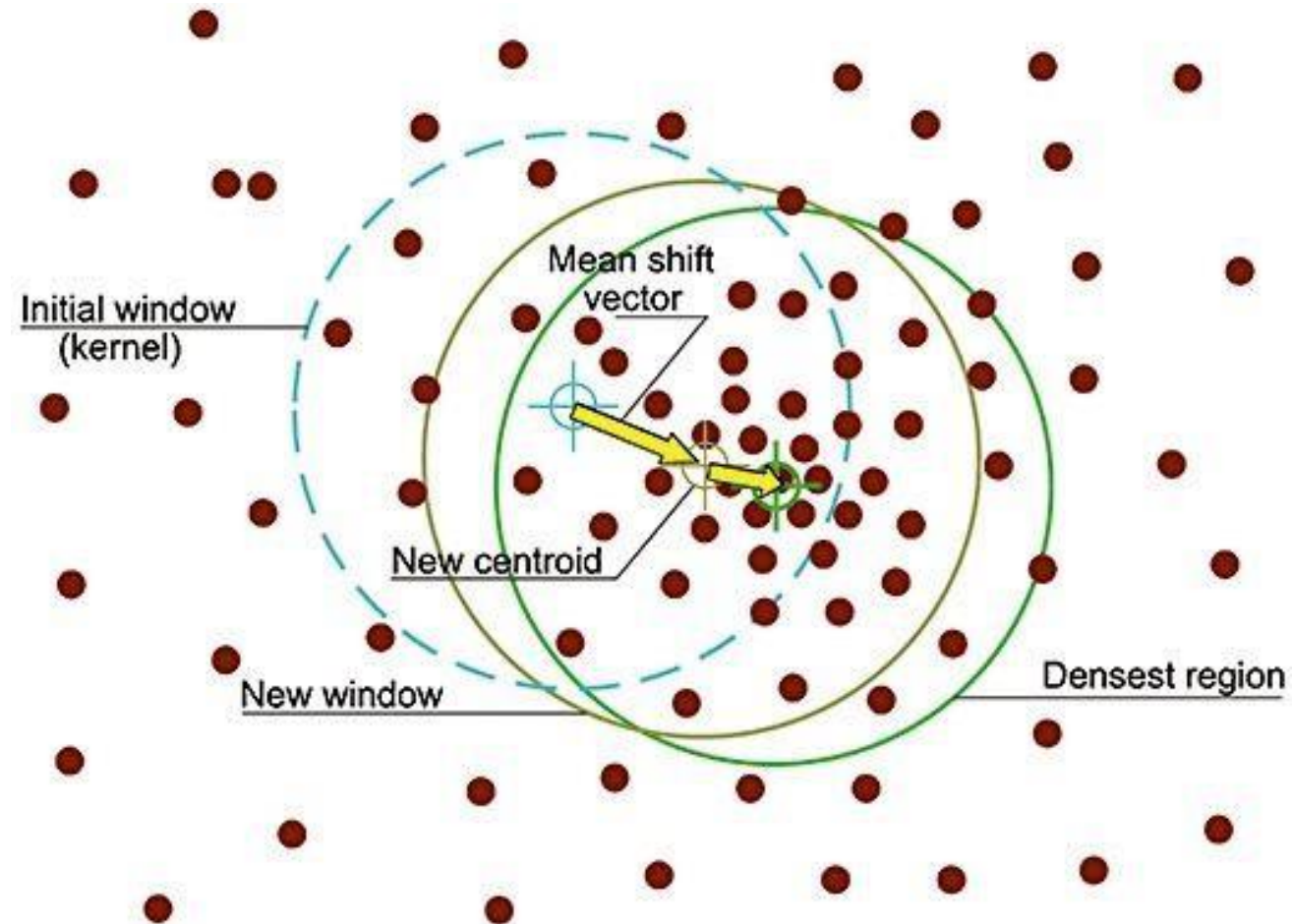
# Hough Transform: Noisy Line



- Possible problem: Finding the true maximum
  - Mean-shift, Gaussian convolution...

# Mean-Shift

Recherche de max local itératif

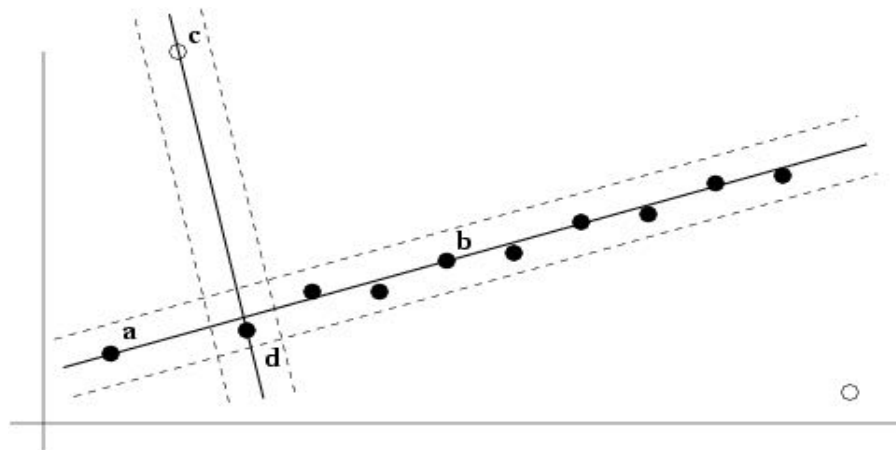




# RANSAC (RANdom SAmple Consensus)

[Fischler81]

- Randomly choose a minimal subset of data points necessary to fit a model (a *sample*)
- Points within some distance threshold  $t$  of model are a *consensus set*. Size of consensus set is model's *support*.
- Repeat for  $N$  samples; model with biggest support is most robust fit
  - Points within distance  $t$  of best model are inliers
  - Fit final model to all inliers



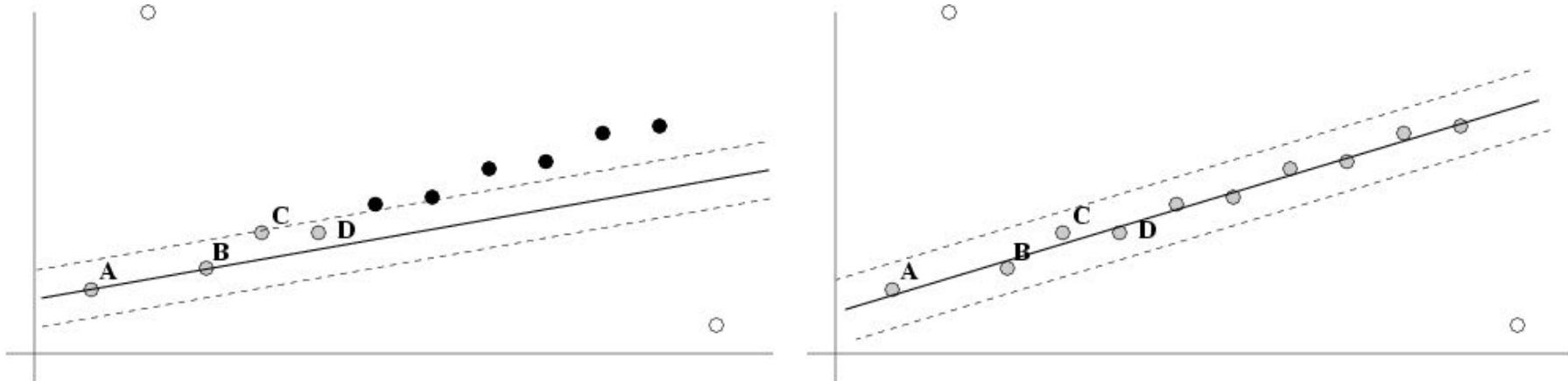
- **RANSAC: How many samples?**
    - How many samples are needed?
      - Suppose  $w$  is fraction of inliers (points from line).
      - $n$  points needed to define hypothesis (2 for lines)
      - $k$  samples chosen.
    - Prob. that a single sample of  $n$  points is correct:  $w^n$
    - Prob. that all samples fail is:  $(1 - w^n)^k$
- ⇒ Choose  $k$  high enough to keep this below desired failure rate.

## RANSAC: Computed $k$ ( $p=0.99$ )

Sample size $n$	Proportion of outliers						
	5%	10%	20%	25%	30%	40%	50%
2	2	3	5	6	7	11	17
3	3	4	7	9	11	19	35
4	3	5	9	13	17	34	72
5	4	6	12	17	26	57	146
6	4	7	16	24	37	97	293
7	4	8	20	33	54	163	588
8	5	9	26	44	78	272	1177

## After RANSAC

- RANSAC divides data into inliers and outliers and yields estimate computed from minimal set of inliers
- Improve this initial estimate with estimation over all inliers (e.g. with standard least-squares minimization)
- But this may change inliers, so alternate fitting with re-classification as inlier/outlier



# Comparison

## Gen. Hough Transform

- **Advantages**
  - Very effective for recognizing arbitrary shapes or objects
  - Can handle high percentage of outliers (>95%)
  - Extracts groupings from clutter in linear time
- **Disadvantages**
  - Quantization issues
  - Only practical for small number of dimensions (up to 4)
- **Improvements available**
  - Probabilistic Extensions
  - Continuous Voting Space } [Leibe08]

## RANSAC

- **Advantages**
  - General method suited to large range of problems
  - Easy to implement
  - Independent of number of dimensions
- **Disadvantages**
  - Only handles moderate number of outliers (<50%)
- **Many variants available, e.g.**
  - PROSAC: Progressive RANSAC [Chum05]
  - Preemptive RANSAC [Nister05]

# Segmentation et detection d'objets

- Ligne de partage des eaux
- Cascade de Haar ( Viola Jones detector)

# En pratique

- Non trivial de faire des opérations basiques de vision
- Problème de robustesse
- Avantage de la compréhension
- Bienvenue dans l'ère du Deep learning ( 2012 )

Quelle heure est t'il ?

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# Et maintenant ! TP A vous de jouer?

