

Relational Algebra

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1 Introduction

Relational algebra are a set of operation on relations/tables. Recalled that in integer like 1,2,3,4,5, etc., we have operation like $+$, $-$, \times , \div . Similarly, in relations/tables, we have operations; union \cup , intersection \cap , differences, cartesian products \times , join \bowtie . There need to use symbols make it difficult to use ascii-based text editor to write notes.

Given a relation R (a table with data called R), we could use relational algebra operation on the relation R . These operations are union, intersection, differences, cartesian and join.

In the text, it uses these sysmbols;

1. π for rows operation, select certain rows
2. σ for column operation, choose certain attributes

For instance, see example on page 43-47. The relational algebra can be combined to for arbitrary complex expression.

2 Question 2.4.1

Recalled that, there are 4 relations. The common attributes in all relations/tables are model. We would use ra, mysql/sqlite3 for answers.

(a) Choose *maker* that sell *printer*, but not *pc*. We need *maker*, thus it is a projection. We only need *printer* but not *pc*, thus a selection. The relation we would use is *Product*.

Let R_i where $i = 1, 2, 3, \dots$ be a temporary relation/table in our computation.

$$R1 := (\pi_{maker})(\sigma_{type=printer})(Product) \quad (1)$$

$$R2 := (\pi_{maker})(\sigma_{type=pc})(Product) \quad (2)$$

$$R3 := (\pi_{maker})(R1 - R2) \quad (3)$$

$R1$ find all maker that sell printer (D,E, H), $R2$ find all maker that sell pc (A, B, C, D, E). Therefore, those who sell printer, but not pc is $(R1-R2)$ which is (H).

SQL:

```

CREATE VIEW [ U ] AS
select distinct maker from Product where type="pc";

CREATE VIEW [ V ] AS
select distinct maker from Product where type="printer";

select maker from V where maker not in ( select maker from U );

```

(b) what pc model have speed at least 2.5? (1001,1004,1005,1006,1010,1012,1013)

$$R1 := (\sigma_{speed \geq 2.5})(PC) \quad (4)$$

$$R2 := (\pi_{maker})(R1) \quad (5)$$

SQL: SELECT maker from PC where speed >= 2.5

(c) What maker produced laptop with hd atleast 120GB? (A,B,E,G)

$$R1 := (\sigma_{hd > 120})(LapTop) \quad (6)$$

$$R2 := (\pi_{maker})(R1) \quad (7)$$

$$R3 := (Product) \bowtie (R2) \quad (8)$$

SQL;

```

select maker from Product where model in
(select model from LapTop where hd >= 120)

```

```

select Product.maker from Product, LapTop where
Product.model=LapTop.model AND LapTop.hd >= 120;

```

(d) Find the model and price for all product by maker C. (1007, 510)

$$R1 := (\sigma_{maker=C})(Product \bowtie PC) \quad (9)$$

$$R2 := (\sigma_{maker=C})(Product \bowtie LapTop) \quad (10)$$

$$R3 := (\sigma_{maker=C})(Product \bowtie Printer) \quad (11)$$

$$R4 := (\pi_{model,price})(R1) \quad (12)$$

$$R5 := (\pi_{model,price})(R2) \quad (13)$$

$$R6 := (\pi_{model,price})(R3) \quad (14)$$

$$R7 := R4 \cup R5 \cup R6 \quad (15)$$

SQL:

```

select maker, Product.model from Product JOIN
LapTop on Product.model = LapTop.model
where Product.maker="C";
select maker, Product.model from Product JOIN
PC on Product.model = LapTop.model
where Product.maker="C";

```

```
select maker, Product.model from Product JOIN
Printer on Product.model = LapTop.model
where Product.maker="C";
```

```
select model, price from LapTop where model in
(select model from Product where maker="C") UNION
select model, price from PC where model in
(select model from Product where maker = "C" )
```

(e) find model of black-and-white printer. (3002, 3005)

$$R1 := (\sigma_{color=0})(Printer) \quad (16)$$

$$R2 := (\pi_{model})(R1) \quad (17)$$

SQL:

```
select model from Printer where color=0;
```

(f) find hd sizes that occur in 2 or more PC.(80(2),160(2),250(6))

SQL:

```
CREATE VIEW W SELECT hd, count (hd) as hdc from PC group by hd
select * from W where hdc >= 2
```

```
select * from (select hd, count (*) as hdc from PC group by hd )
where hdc >=2
```

(g) find pairs of PC that have same speed and RAM. (1004,1012)

$$R1 := (\sigma_{speed_a=speed_b, ram_a=ram_b, model_a < model_b})(PC_a \bowtie PC_b) \quad (18)$$

```
select A.model, B.model, A.speed, A.ram, B.speed, B.ram from
PC as A join PC as B on A.speed = B.speed AND A.ram = B.ram
AND A.model < B.model
```

(h) find makers of atleast 2 different pc or laptop with atleast speed 2.2. (B, E)

SQL:

```
create view X as select model, speed from PC where
speed >=2.2 UNION select model, speed
from LapTop where speed >= 2.2
```

```
select maker from ( select maker, count (*) as mkc
from X group by maker)
where mkc >=2
```

(k) Find makers with exactly 3 different models PC. (A,B,D,E)

```

select maker from ( select maker, count(*) as mkc
                    from ( Product JOIN PC on Product.model = PC.model )
                    group by maker )
                    where mkc =3

```

(j) find makers with the highest speed for PC and LapTop. (maker=B, model=1005,1006).

```

select maker, model from Product where model in
(select model from PC where speed in
(select max(speed) from
( select model, speed from PC UNION
select model, speed from LapTop )))

```

(l) makers with atleast 3 different speeds. (A(1.42,2.1,2.66), D(2,2,2,2.8), E(1.86,2.8,3.06))

```

create view Ri as select Product.maker, PC.model, PC.speed from
PC JOIN Product on Product.model = PC.model
# note i = 1, 2, 3
select R1.maker, R1.speed, R2.speed, R3.speed from R1, R2, R3
where R1.maker=R2.maker and R1.maker = R3.maker and
R1.speed < R2.speed and R1.speed < R3.speed and
R2.speed < R3.speed

```