



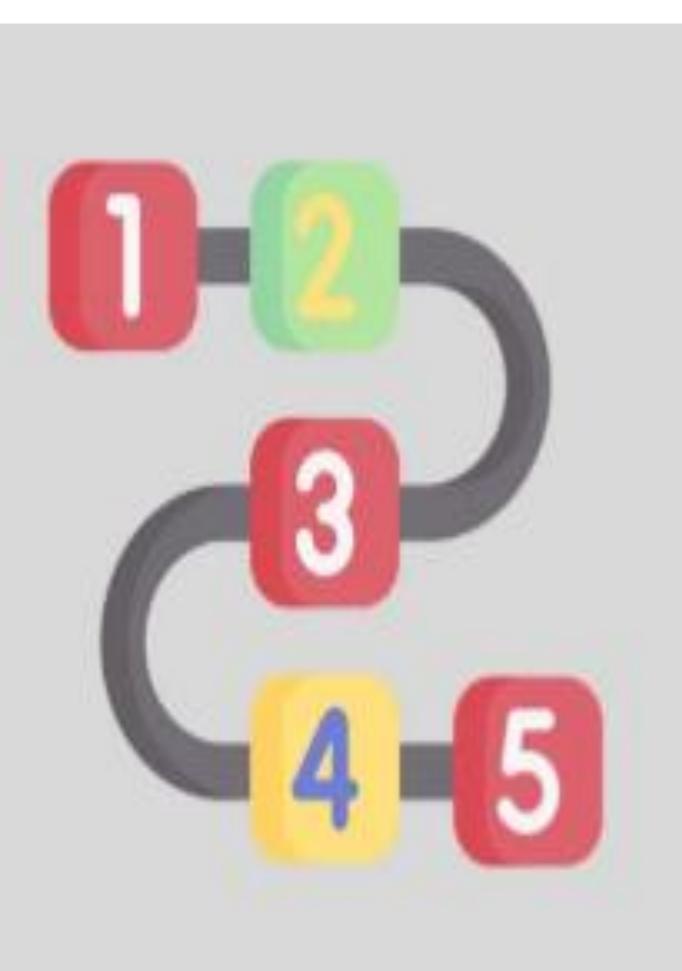




Agenda

- Introduction to Sequential Data
- Limitations of Feedforward Networks
- Introduction to RNNs
- Deep Dive into LSTM
- Common Use Cases of LSTM
- Introduction to GRU
- Comparison: LSTM vs GRU vs RNN





What is Sequential Data?

- Ordered data (sentences, time-series, audio)
- Requires context and memory

Examples:

Text/Sentences:

The sentence "The cat sat on the mat" has a meaning because of word order. Shuffle the words, and the meaning may change.

Time-Series Data:

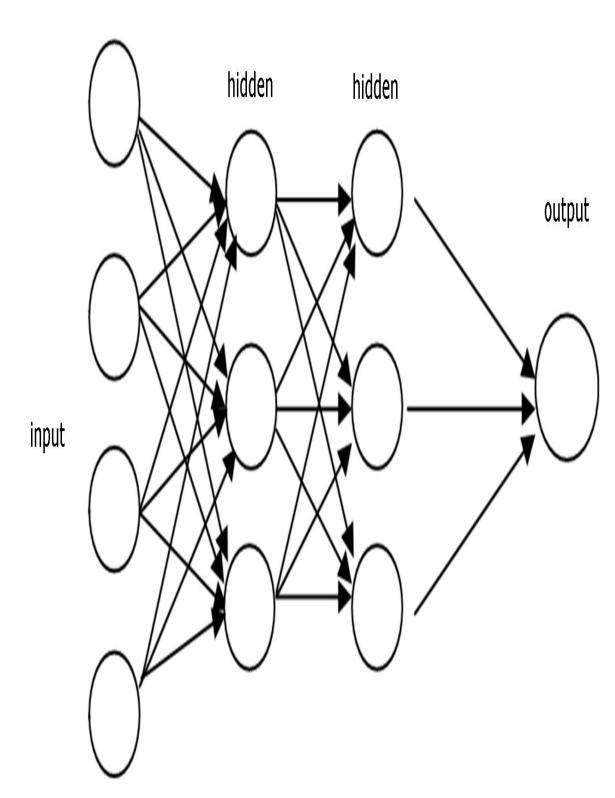
Stock prices, temperature readings — each value depends on the time before it.

Audio Signals:

Speech is made of waveforms that change over time. The order of sound frequencies determines the spoken word.



Why Not Feedforward Networks?



• Feedforward Neural Networks (FNNs) are excellent for many tasks like classification and regression on structured/tabular data, but they fail when it comes to sequential data. Why?

Limitations:

No Memory of the Past:

FNNs process each input independently.

They can't retain information from earlier parts of the input.

For example, if you're translating a sentence, FNNs can't remember what was said earlier.

No Sense of Order:

In sequential data, order matters.

"She is not happy" ≠ "She is happy not"

→ FNNs treat both as unrelated since they lack positional context.

Contextual Dependency is Ignored:

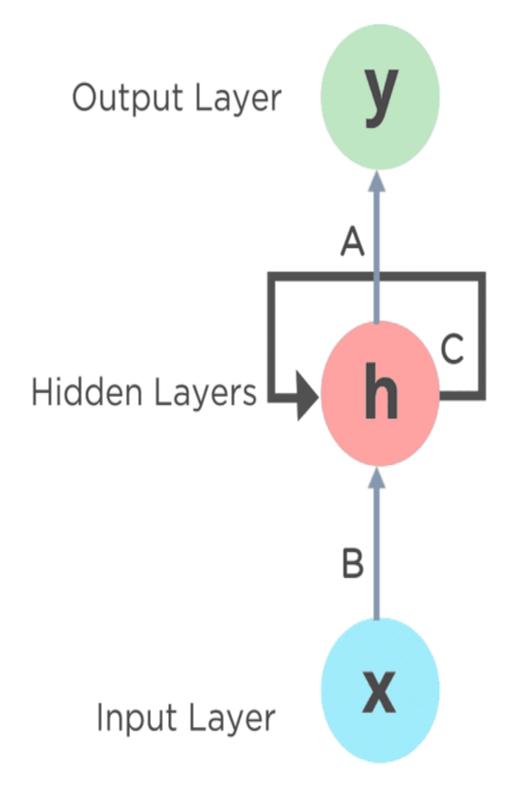
If you're analyzing time-series data like stock prices, the next value heavily depends on the previous ones.

FNNs assume inputs are independent, so they can't model such dependencies.

Fixed Input Size:

FNNs usually require a fixed-size input.





A, B and C are the parameters

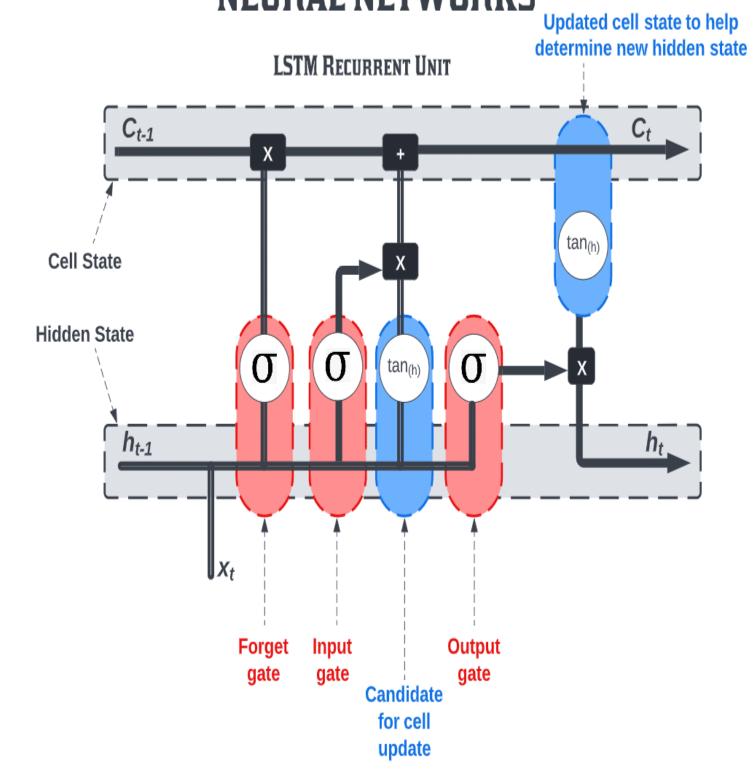
Recurrent Neural Networks (RNN)

- Maintains hidden state
- Designed for sequences
- Struggles with long-term dependencies

(Vanishing Gradient Problem)



LONG SHORT - TERM MEMORY NEURAL NETWORKS



What is LSTM?

LSTM (Long Short-Term Memory) is a special type of Recurrent Neural Network (RNN) architecture designed to **learn long-term dependencies** in sequential data.

Proposed by Hochreiter & Schmidhuber (1997).

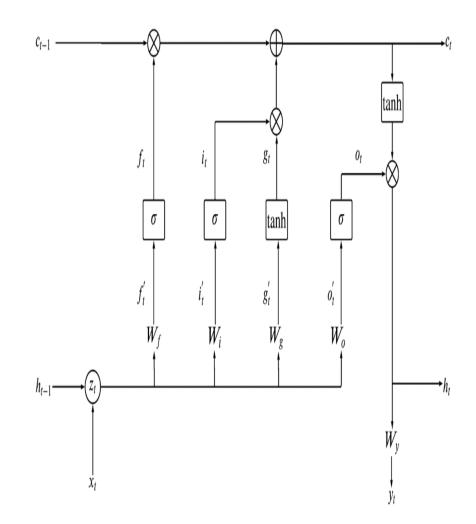
Unlike vanilla RNNs, it has an internal memory (cell state) that can carry information across many time steps.

Uses **gates** (forget, input, output) to control the flow of information.





Long Short-Term Memory Networks



Why "Long" and "Short"-Term?

•The name reflects its ability to manage **short-term memory** (current context) **and long-term memory** (important past context).

For example, in the sentence:

"The cat that was chased by the dog ran under the car,"

The network might need to remember "cat" at the beginning to understand what "ran" refers to at the end.

LSTM Solves:

- Vanishing gradient problem in long sequences
- Maintains memory over time
- Learns complex patterns across long texts, audio, and time-series data





Long Short-Term Memory

LSTM Architecture Overview

Think of LSTM like a smart notebook:

- It writes down important things (input gate).
- It erases unnecessary things (forget gate).
- It decides what to **share with the n1ext layer or step** (output gate).

This makes LSTMs excellent at remembering **context** over long sequences — something vanilla RNNs fail at due to the *vanishing gradient problem*.

Imagine predicting the next word in this sentence:

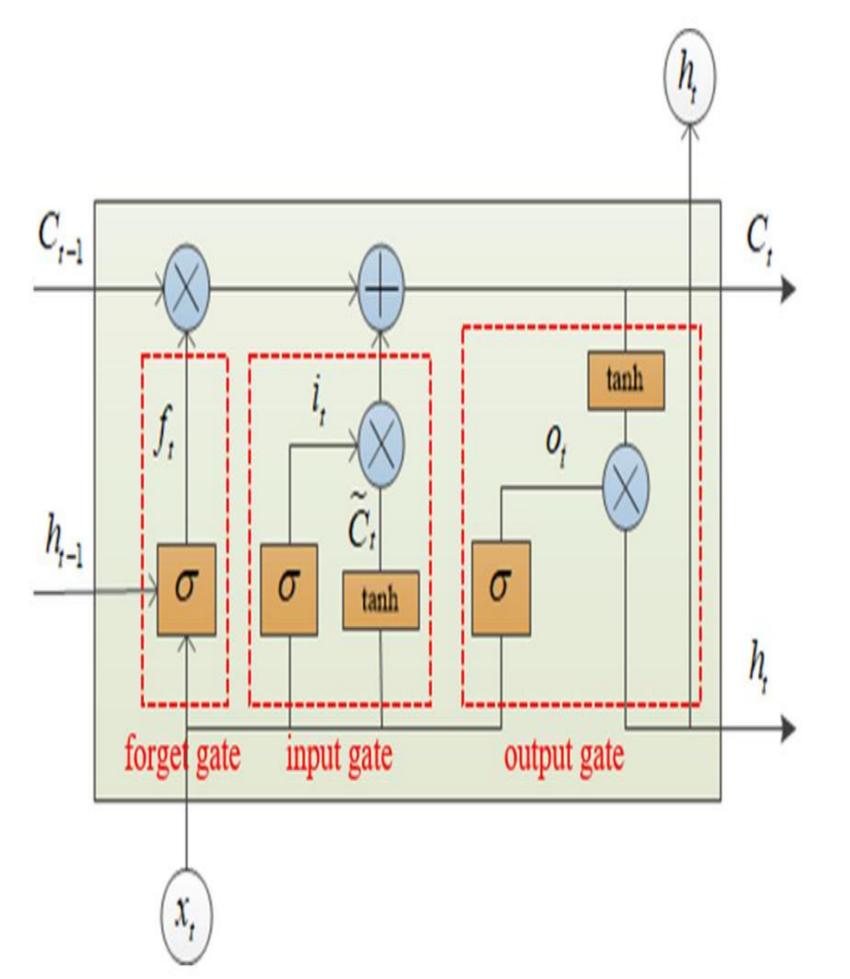
"I grew up in **France**... I speak fluent ____."

A vanilla RNN might forget "France" after a few steps.

An LSTM remembers the country information across many words and predicts French correctly.

► LSTM = RNN + memory cell + gates → allows learning long-term dependencies in sequential tasks.



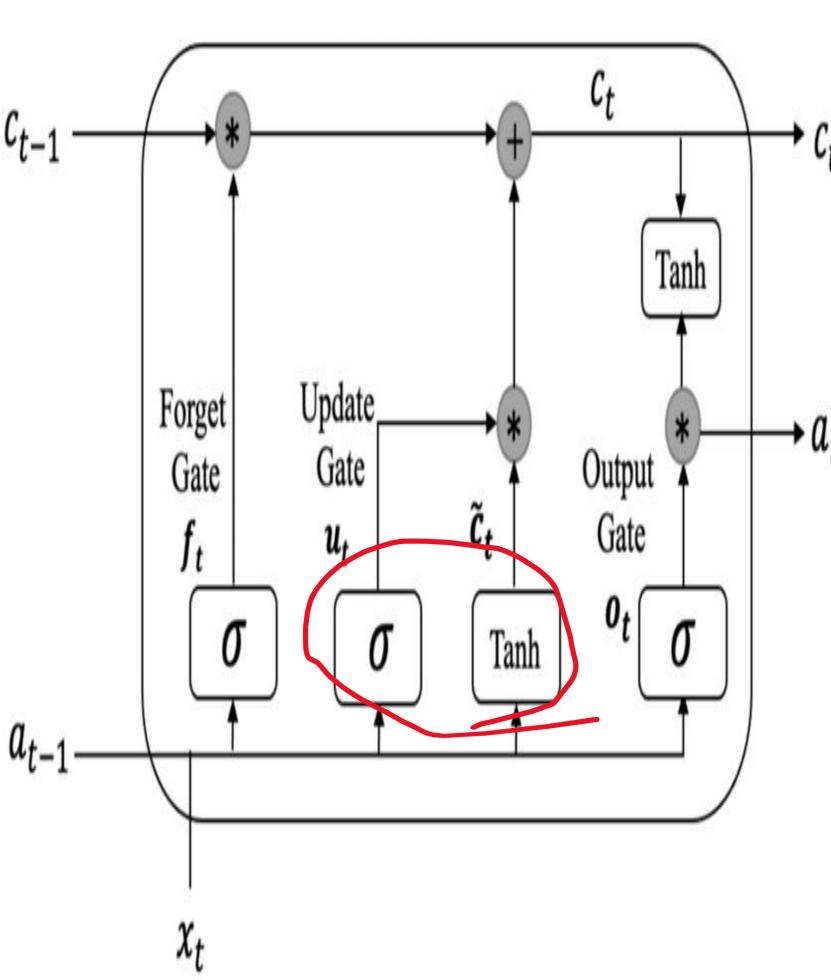


Forget Gate

- The **Forget Gate** is the first decision point inside the LSTM cell.
- Its job is to decide which information from the previous cell state should be removed or kept.
- Sometimes, not all past information is useful for future predictions.
- So, the LSTM needs to "forget" parts of its memory that are no longer relevant.

$$f_t = \sigma\left(W_f \cdot [h_{t-1}, x_t] + b_f\right)$$





Input Gate

After deciding what to forget, the LSTM now asks: "What new information should I store in my memory?"

That's the role of the Input Gate.

The **Input Gate** controls which parts of the current input (and the previous hidden state) are important enough to **add to the cell state (memory)**.

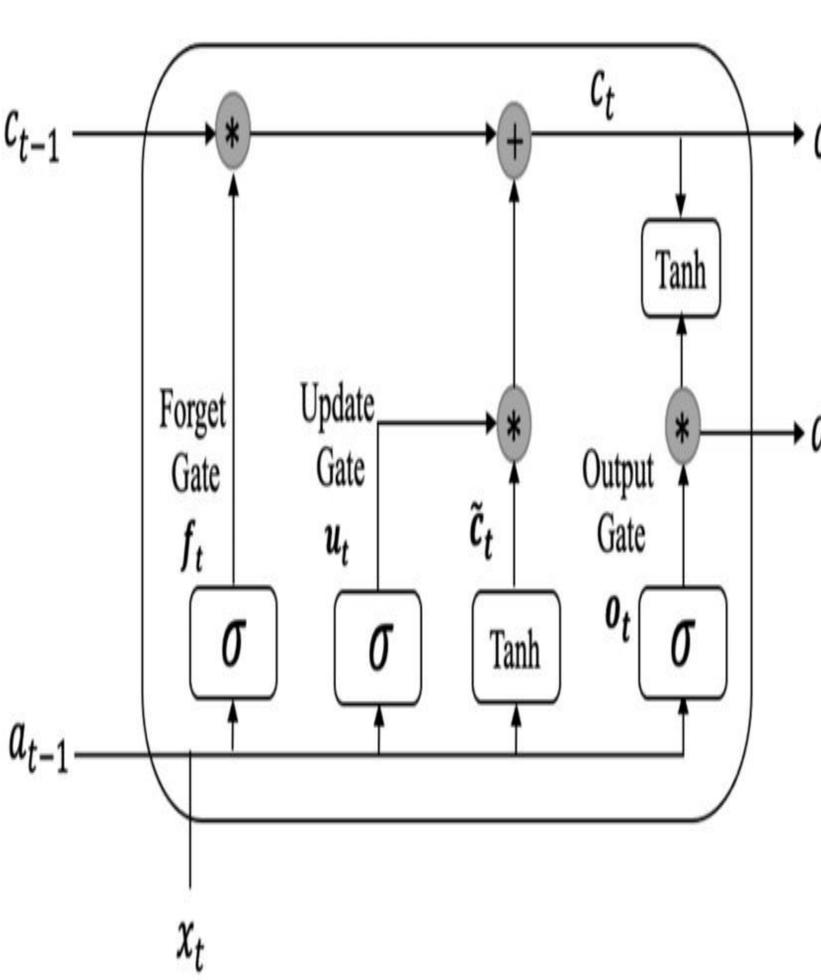
Gate Activation:

$$i_t = \sigma \left(W_i \cdot [h_{t-1}, x_t] + b_i \right)$$

Candidate Memory:

$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$





Update Gate

Now that we know what to forget (Forget Gate) and what new information to add (Input Gate),

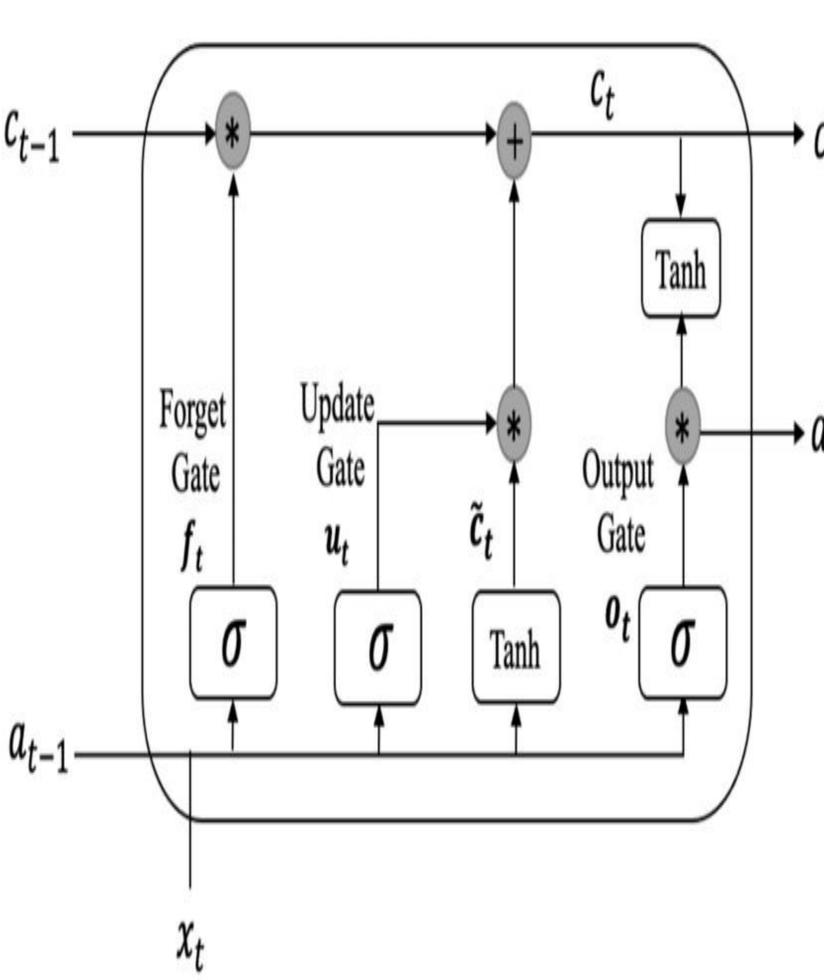
 $m{+} \mathfrak{a}_t$ it's time to **actually update the memory** — this happens in the **Cell State**.

The **cell state** is the internal memory of the LSTM.

It flows through time, carrying important information forward — updated at every step.

$$C_t = \sigmaig(f_t * C_{t-1} + i_t * ilde{C}_tig)$$





Output Gate

After updating the memory (cell state), the LSTM now decides:

What should be output at this time step?

That's the job of the **Output Gate**.

The **Output Gate** controls what information from the updated cell state should become the **hidden state**, which will be:

Passed to the next LSTM unit

Used to produce any final output (e.g., predictions)

$$h_t = \tanh(C_t) * o_t$$



Advantages of LSTM

1. Solves the Vanishing Gradient Problem

- •Can preserve information over long sequences.
- •Unlike vanilla RNNs, LSTM doesn't "forget" quickly.

2. Captures Long-Term Dependencies

- Keeps track of context across many time steps.
- •Useful in tasks where earlier input influences much later output (e.g., machine translation).

3. Selective Memory with Gates

- •Forget, input, and output gates act as filters.
- The network decides what to keep, update, or discard.

4. Better Accuracy in Sequence Tasks

•Proven to outperform vanilla RNNs in **NLP**, **speech recognition**, **and time-series forecasting**.

5. Flexible for Different Data Types

•Works with text, speech, video, stock prices, sensor data, etc.

6. Well-Researched & Widely Used

•Huge community support, tutorials, and pre-trained models available.



Limitations of LSTM

1. High Computational Cost

- More complex than vanilla RNNs.
- •Each LSTM cell has **multiple gates** → more matrix multiplications per step.

2. Slower Training

Requires more resources and longer training time compared to simpler RNNs or GRUs.

3. Large Memory Usage

- Storing gate activations and gradients consumes a lot of memory.
- Not ideal for very long sequences on limited hardware.

4. Difficult to Tune

- Many hyperparameters: number of layers, hidden units, dropout, learning rate.
- Sensitive to initialization and optimization choices.

5. Overkill for Short Sequences

- •When the sequence length is short, LSTMs may be unnecessarily heavy.
- Simpler models (GRU, even vanilla RNN) may work just as well.

6. Interpretability

•Internal working (gates + cell state) is hard to interpret compared to simpler models.





Motivation for GRU

- •We've seen how LSTMs solve the vanishing gradient problem using gates and memory cells.
- •But... LSTMs are computationally heavy:
 - Multiple gates (forget, input, output).
 - Large number of parameters.
 - Slower training and inference.

Researchers asked:

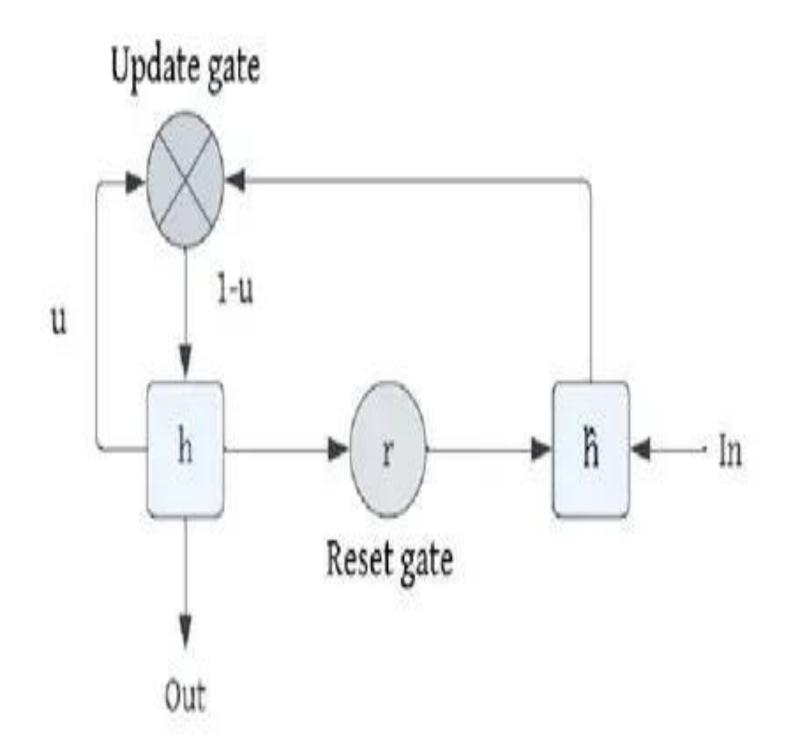
? "Can we design a simpler architecture that works almost as well as LSTM, but is faster and lighter?"
Answer: GRU (Gated Recurrent Unit) → introduced in 2014 (Cho et al.).

GRU simplifies the LSTM by:

Combining forget & input gate → update gate.

Removing the **separate cell state** \rightarrow only hidden state.





What is GRU?

- •GRU is a gated architecture like LSTM.
- •It controls information flow with fewer gates.
- •Unlike LSTM, it has **no separate cell state** → only maintains a **hidden state**.

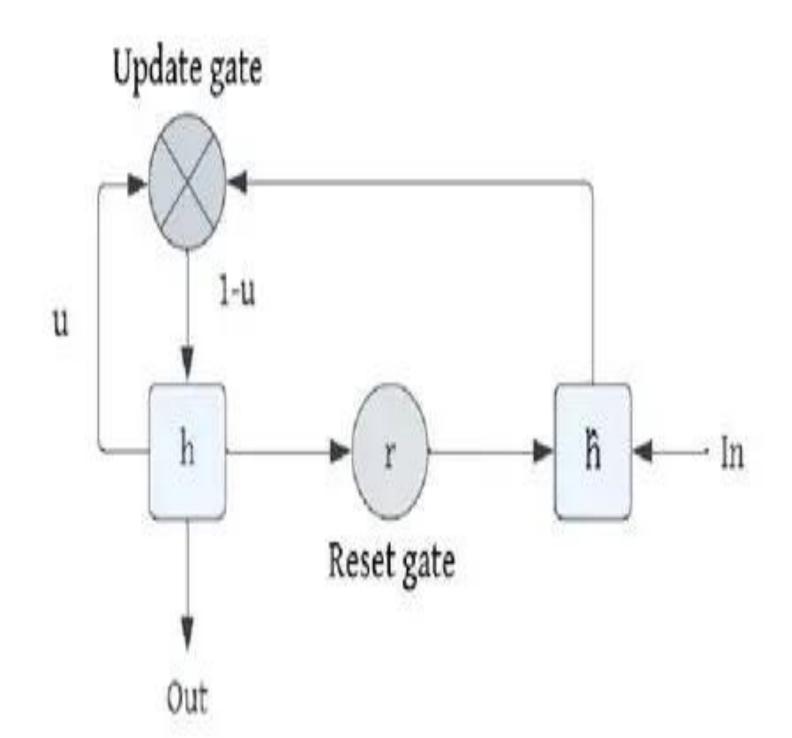
GRU was designed to:

- Be faster and simpler than LSTM
- Use fewer gates (only 2 instead of 3)
- Have fewer parameters, which helps it train quicker

GRU Has Two Gates:

- Update Gate
- > Reset Gate



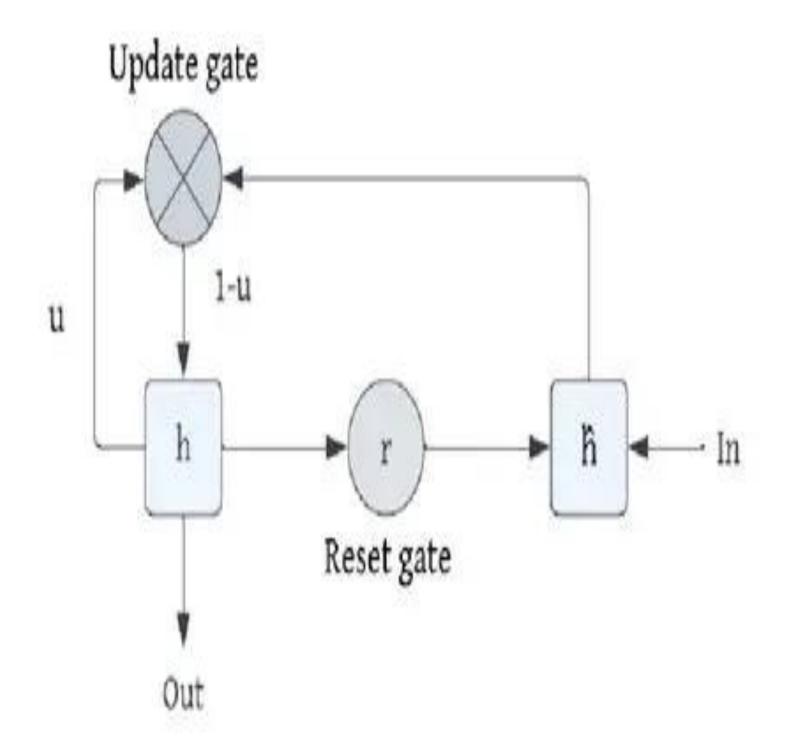


Update Gate

In GRU, the **Update Gate** is responsible for controlling how much of the past information should be **carried**forward and how much of the new information should be used to update the current hidden state.

$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$





Reset Gate

In the GRU, the **Reset Gate** decides how much of the past hidden state should be forgotten **when computing the new memory**.

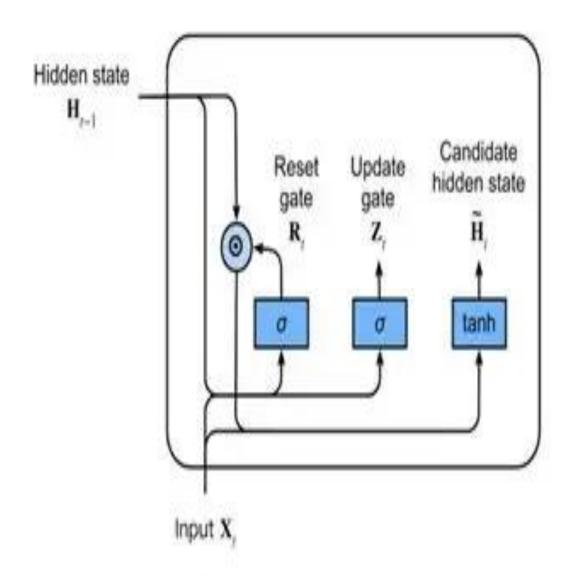
It helps the model to reset or ignore irrelevant past information.

$$r_t = \sigma\left(W_r \cdot [h_{t-1}, x_t]\right)$$



Candidate hidden state update

$$\tilde{H}_t = \tanh(X_t W_{xh} + (R_t \odot H_{t-1}) W_{hh} + b_h)$$



In a GRU, before updating the hidden state, we compute a candidate hidden state ($h_{_{\it f}}$ (that represents the new information the network might want to add.

How it works:

Reset gate r_t decides how much of the **past memory** to use.

If $r_t \approx 0 \rightarrow$ ignore most of the past (focus on new input).

If $r_t \approx 1 \rightarrow$ keep past information.

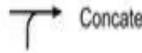
The network combines **filtered past info + current** input.

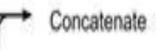
Passes them through a tanh activation → candidate hidden state.

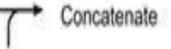








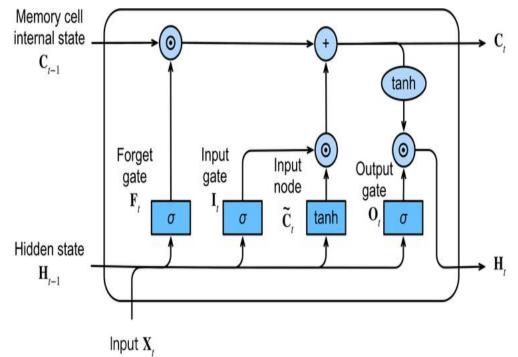


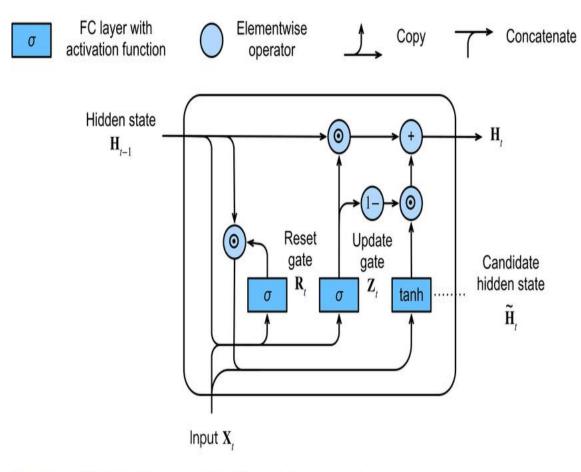


Comparison Table

Feature	LSTM	GRU
Long-term Memory	True	True
Training Speed	Slow	Fast
Complexity	High	Low







When to choose GRU over LSTM

1. When speed matters

- •GRUs are **faster to train** (fewer gates → fewer parameters).
- •Better for **real-time applications** like chatbots or online recommendation.

2. When resources are limited

- •GRUs use less memory & computation.
- •Good for mobile/embedded devices or when using smaller GPUs.

3. When data is small or moderate

- •GRUs have lower risk of overfitting due to simpler architecture.
- More suitable for tasks with limited training data.

4. When sequences are not very long

•For short/medium sequences, GRUs perform as well as LSTMs, but more efficiently.

5. When experimenting quickly

•Faster training allows **rapid prototyping** and trying different architectures.



