Exercise 2:. Part a) $S_{ij} = \begin{cases} 1 & i = j \\ i & i = j \end{cases}$ to Shaw P is a Markov Chairi-Vi $\sum_{j=1}^{M} \tilde{P}_{ij} = 1$ we split the Sum into 2 Part i=j & i + j $\sum_{i=1}^{n} \tilde{p}_{i,j} = \sum_{i=1}^{n} \left[(1-c_{\hat{j}}) \delta_{i,j} + d_{i,j} P_{i,j} \right]$ = \(\lambda_{ij} P_{ij} + (1-C_j) + d_{ij} P_{ij} \) Since di = 1 N (Pi) = 1 M = 1 D di * Pii = Pii 2 C: = Substitute in () Vi, & Pii = \ (1-(i) + \ di, Pii + Pii = 1 - C(+ 1 - P/1 + P/1 2-C: ->2) $C_i = \sum_{i=1}^{N} d_{ij} P_{ij} = \sum_{i=1}^{N} \widetilde{P}_{ij} = (1-C_i) + C_i = 1$ 8. Ai, ≤ Pi; = 1

herle, Pis Me a valid Marker Chain.

Pout b) Case 1: i + j = Si; = 0 Pis = XisPis & Pis = X si-Psi So: Pi, Pi = 4, Pi, Pi & Pi, Pi = 4, Pi, Pi Since P is symmetric $\Rightarrow P_{ij} = P_{ji}$ $\forall ij = Min(1, \frac{P_i^*}{P_j^*})$ di=min (1, Pot) $\square : F \xrightarrow{P_i} \not\in 1 \implies \alpha_{i,j} = \frac{P_i}{P_i^*}, \alpha_{j,j} = 1$ $\hat{P}_{ij} P_{i}^{\dagger} = \frac{P_{i}^{\dagger}}{P_{i}^{\dagger}} P_{ij} P_{j}^{\dagger} = P_{ij} P_{i}^{\dagger} P_{i}^{\dagger}$ $\hat{P}_{ij} P_{i}^{\dagger} = 1 \cdot P_{ij} P_{i}^{\dagger} = P_{ij} P_{i}^{\dagger}$ 2) if Pi > 1 -> di; = 1, di; = Pi $\tilde{P}_{ij}P_{j}^{\dagger} = \frac{1.P_{ij}.P_{j}^{\dagger}}{P_{i}} = \frac{P_{ij}.P_{j}^{\dagger}}{P_{i}} = \frac{P_{ij}.P_{ij}}{P_{i}} = \frac{P_{ij}.P_{ij}}{P_{ij}} = \frac{P_{ij}.P_{ij}}{P_{i}} = \frac{P_{ij}.P_{ij}}{P_{i}} = \frac{P_{ij}.P_{ij}}{P_{i}} = \frac{P_{ij}.P_{ij}}{P_{i}} = \frac{P_{ij}.P_{ij}}{P_{ij}} = \frac{P$

Gux 2: i = j => Sij = 1 => Pi = 1 - Ci + di Pi = Pipi trivially " P satis fired delailed balance Viji