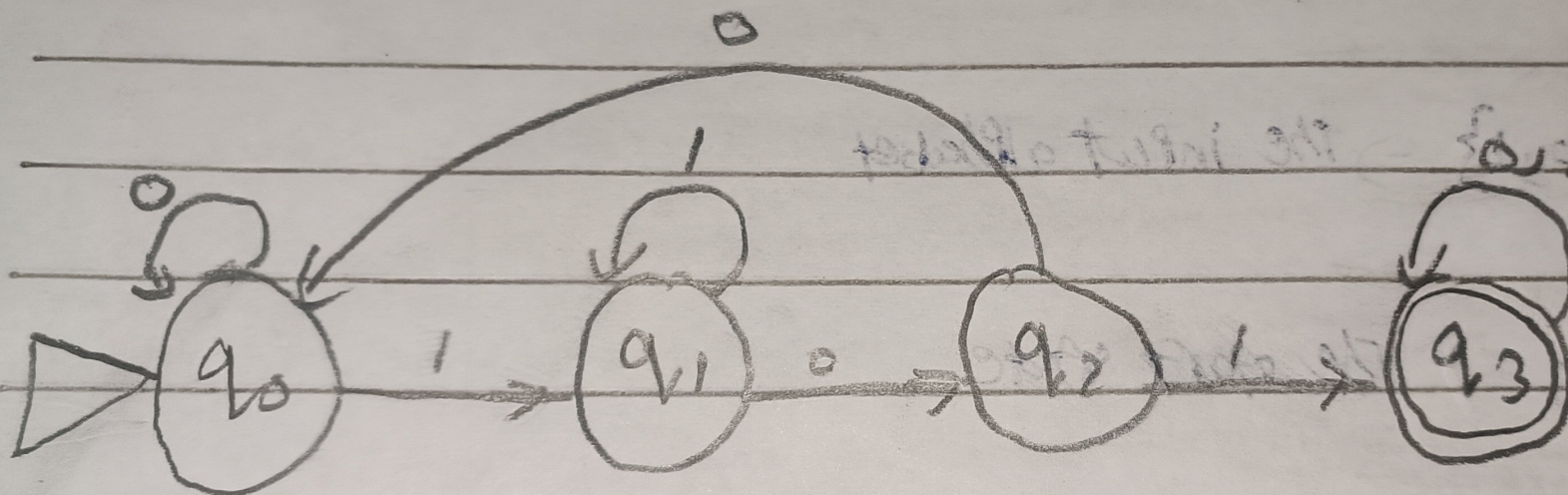


2. State Diagram:





Date

No

Construct a DFA for substring "101"

⇒ The DFA accepts any binary string that contains the substring "101" at least once.

1. Formal Definition:

The DFA is defined as  $M = (Q, \Sigma, \delta, q_0, F)$  where  $q_0$  is the start state.

\*  $Q = \{q_0, q_1, q_2, q_3\}$

$q_0$  is the start state

$q_1, q_2, q_3 \in P$

$q_2 \rightarrow 10$

$q_3 \rightarrow 101$  accept

\*  $\Sigma = \{0, 1\}$  ⇒ The input alphabet

\*  $q_0 = q_0$  ⇒ The start state

\*  $F = \{q_3\}$  ⇒ The set of accept states



\*  $\delta$  (Transition function):

Current state	input 0	input 1	
$q_0$	$q_0$	$q_1$	$\delta(q_0, 0) = q_0$ $\delta(q_0, 1) = q_1$
$q_1$	$q_2$	$q_1$	$\delta(q_1, 0) = q_2$ $\delta(q_1, 1) = q_1$
$q_2$	$q_0$	$q_3$	$\delta(q_2, 0) = q_0$ $\delta(q_2, 1) = q_3$
$q_3$	$q_3$	$q_3$	$\delta(q_3, 0) = q_3$ $\delta(q_3, 1) = q_3$