Analyze_ab_test_results_notebook

May 10, 2022

1 Analyze A/B Test Results

This project will assure you have mastered the subjects covered in the statistics lessons. We have organized the current notebook into the following sections:

- Section ??

Specific programming tasks are marked with a **ToDo** tag. ## Introduction

A/B tests are very commonly performed by data analysts and data scientists. For this project, you will be working to understand the results of an A/B test run by an e-commerce website. Your goal is to work through this notebook to help the company understand if they should: - Implement the new webpage, - Keep the old webpage, or - Perhaps run the experiment longer to make their decision.

Each **ToDo** task below has an associated quiz present in the classroom. Though the classroom quizzes are **not necessary** to complete the project, they help ensure you are on the right track as you work through the project, and you can feel more confident in your final submission meeting the **rubric** specification.

Tip: Though it's not a mandate, students can attempt the classroom quizzes to ensure statistical numeric values are calculated correctly in many cases.

```
## Part I - Probability
To get started, let's import our libraries.
```

```
In [1]: import pandas as pd
    import numpy as np
    import random
    import matplotlib.pyplot as plt
    %matplotlib inline
    #We are setting the seed to assure you get the same answers on quizzes as we set up
    random.seed(42)
```

1.0.1 ToDo 1.1
Now, read in the ab_data.csv data. Store it in df. Below is the description of the data, there are a total of 5 columns:

		Valid	
Data columns	Purpose	values	
user_id	Unique ID	Int64	
	•	values	
timestamp	Time stamp when	-	
	the user visited		
	the webpage		
group	In the current	['control',	
	A/B experiment,	'treatment'	
	the users are		
	categorized into		
	two broad groups.		
	The control		
	group users are		
	expected to be		
	served with		
	old_page; and		
	treatment group		
	users are matched		
	with the		
	new_page.		
	However, some		
	inaccurate rows		
	are present in the		
	initial data, such		
	as a control		
	group user is		
	matched with a		
	new_page.		
landing_page	It denotes	['old_page'	
	whether the user	'new_page']	
	visited the old or		
	new webpage.		
converted	It denotes	[0, 1]	
converted	whether the user	10, 11	
	decided to pay for		
	the company's		
	product. Here, 1		
	means yes, the		
	user bought the		
	product.		
	product.		

Use your dataframe to answer the questions in Quiz 1 of the classroom.

Tip: Please save your work regularly.

a. Read in the dataset from the ab_data.csv file and take a look at the top few rows here:

```
In [2]: df = pd.read_csv("ab_data.csv")
       df.head()
Out[2]:
          user_id
                                                   group landing_page
                                    timestamp
                                                                       converted
          851104 2017-01-21 22:11:48.556739
                                                             old_page
                                                                               0
                                                 control
          804228 2017-01-12 08:01:45.159739
                                                             old_page
                                                                               0
       1
                                                 control
          661590 2017-01-11 16:55:06.154213 treatment
                                                                               0
                                                             new_page
       3 853541 2017-01-08 18:28:03.143765
                                               treatment
                                                             new_page
                                                                               0
           864975 2017-01-21 01:52:26.210827
                                                 control
                                                             old_page
                                                                               1
```

b. Use the cell below to find the number of rows in the dataset.

```
In [3]: df.shape[0]
Out[3]: 294478
```

c. The number of unique users in the dataset.

```
In [4]: df['user_id'].nunique()
Out[4]: 290584
```

d. The proportion of users converted.

```
In [5]: df.query('converted == 1').user_id.nunique() / df.user_id.nunique()
Out[5]: 0.12104245244060237
```

e. The number of times when the "group" is treatment but "landing_page" is not a new_page.

```
In [6]: df.query('(group == "treatment" and landing_page != "new_page") or(group != "treatment"
Out[6]: 3893
```

f. Do any of the rows have missing values?

```
In [7]: df.isnull().sum().any()
Out[7]: False
```

1.0.2 ToDo 1.2

In a particular row, the **group** and **landing_page** columns should have either of the following acceptable values:

user_id	timestamp	group	landing_page	converted
XXXX	XXXX	control	old_page	X
XXXX	XXXX	treatment	new_page	Χ

It means, the control group users should match with old_page; and treatment group users should matched with the new_page.

However, for the rows where treatment does not match with new_page or control does not match with old_page, we cannot be sure if such rows truly received the new or old wepage.

Use Quiz 2 in the classroom to figure out how should we handle the rows where the group and landing_page columns don't match?

a. Now use the answer to the quiz to create a new dataset that meets the specifications from the quiz. Store your new dataframe in df2.

```
In [8]: # Remove the inaccurate rows, and store the result in a new dataframe df2
       df_control = df.query('group == "control" and landing_page == "old_page"')
       df_treatment = df.query('group == "treatment" and landing_page == "new_page"')
        frame = [df_control , df_treatment]
        df2= pd.concat(frame)
        df2.head()
Out[8]:
          user_id
                                     timestamp
                                                  group landing_page converted
        0 851104 2017-01-21 22:11:48.556739 control
                                                            old_page
        1 804228 2017-01-12 08:01:45.159739 control
                                                            old_page
                                                                              0
        4 864975 2017-01-21 01:52:26.210827 control
                                                            old_page
                                                                              1
          936923 2017-01-10 15:20:49.083499 control
                                                            old_page
                                                                              0
        7
          719014 2017-01-17 01:48:29.539573 control
                                                            old_page
In [9]: # Double Check all of the incorrect rows were removed from df2 -
        # Output of the statement below should be 0
        df2[((df2['group'] == 'treatment') == (df2['landing_page'] == 'new_page')) == False].sha
Out[9]: 0
1.0.3 ToDo 1.3
Use df2 and the cells below to answer questions for Quiz 3 in the classroom.
   a. How many unique user_ids are in df2?
```

```
In [10]: df2['user_id'].nunique()
Out[10]: 290584
   b. There is one user_id repeated in df2. What is it?
In [11]: df2.duplicated(['user_id']).sum()
Out[11]: 1
In [12]: df2[df2.duplicated(['user_id'])].user_id
```

```
Out[12]: 2893
                  773192
         Name: user_id, dtype: int64
   c. Display the rows for the duplicate user_id?
In [13]: df2[df2.duplicated(['user_id'])]
Out[13]:
                                                            group landing_page
                user_id
                                                                                 converted
                                            timestamp
                 773192 2017-01-14 02:55:59.590927 treatment
         2893
   d. Remove one of the rows with a duplicate user_id, from the df2 dataframe.
In [14]: # Remove one of the rows with a duplicate user_id..
         # Hint: The dataframe.drop_duplicates() may not work in this case because the rows with
         df2 = df2.drop_duplicates(['user_id'])
         # Check again if the row with a duplicate user_id is deleted or not
         df2.duplicated(['user_id']).sum()
Out[14]: 0
1.0.4 ToDo 1.4
Use df2 in the cells below to answer the quiz questions related to Quiz 4 in the classroom.
   a. What is the probability of an individual converting regardless of the page they receive?
     Tip: The probability you'll compute represents the overall "converted" success rate in
     the population and you may call it p_{population}.
In [15]: p_population = df2.query('converted == 1').shape[0] / df2['converted'].shape[0]
         p_population
Out[15]: 0.11959708724499628
   b. Given that an individual was in the control group, what is the probability they converted?
In [16]: p_control_converted =df2.query('group =="control" and converted == 1').shape[0] / df2.c
         p_control_converted
Out[16]: 0.1203863045004612
   c. Given that an individual was in the treatment group, what is the probability they con-
verted?
In [17]: p_treatment_converted =df2.query('group =="treatment" and converted == 1').shape[0] / d
         p_treatment_converted
```

Tip: The probabilities you've computed in the points (b). and (c). above can also be treated as conversion rate. Calculate the actual difference (obs_diff) between the conversion rates for the two groups. You will need that later.

Out[17]: 0.11880806551510564

Out[18]: 0.0015782389853555567

d. What is the probability that an individual received the new page?

e. Consider your results from parts (a) through (d) above, and explain below whether the new treatment group users lead to more conversions.

Your answer goes here.

```
## Part II - A/B Test
```

Since a timestamp is associated with each event, you could run a hypothesis test continuously as long as you observe the events.

However, then the hard questions would be: - Do you stop as soon as one page is considered significantly better than another or does it need to happen consistently for a certain amount of time?

- How long do you run to render a decision that neither page is better than another? These questions are the difficult parts associated with A/B tests in general.

1.0.5 ToDo 2.1

For now, consider you need to make the decision just based on all the data provided.

Recall that you just calculated that the "converted" probability (or rate) for the old page is *slightly* higher than that of the new page (ToDo 1.4.c).

If you want to assume that the old page is better unless the new page proves to be definitely better at a Type I error rate of 5%, what should be your null and alternative hypotheses (H_0 and H_1)?

You can state your hypothesis in terms of words or in terms of p_{old} and p_{new} , which are the "converted" probability (or rate) for the old and new pages respectively.

```
H0: P_old_page >= P_new_page , H1: P_new_page > P_old_page.
```

1.0.6 ToDo **2.2** - Null Hypothesis H_0 Testing

Under the null hypothesis H_0 , assume that p_{new} and p_{old} are equal. Furthermore, assume that p_{new} and p_{old} both are equal to the **converted** success rate in the df2 data regardless of the page. So, our assumption is:

```
p_{new} = p_{old} = p_{population}
In this section, you will:
```

- Simulate (bootstrap) sample data set for both groups, and compute the "converted" probability *p* for those samples.
- Use a sample size for each group equal to the ones in the df2 data.
- Compute the difference in the "converted" probability for the two samples above.
- Perform the sampling distribution for the "difference in the converted probability" between the two simulated-samples over 10,000 iterations; and calculate an estimate.

Use the cells below to provide the necessary parts of this simulation. You can use **Quiz 5** in the classroom to make sure you are on the right track.

a. What is the **conversion rate** for p_{new} under the null hypothesis?

b. What is the **conversion rate** for p_{old} under the null hypothesis?

c. What is n_{new} , the number of individuals in the treatment group? *Hint*: The treatment group users are shown the new page.

d. What is n_{old} , the number of individuals in the control group?

e. Simulate Sample for the treatment Group Simulate n_{new} transactions with a conversion rate of p_{new} under the null hypothesis. *Hint*: Use numpy.random.choice() method to randomly generate n_{new} number of values. Store these n_{new} 1's and 0's in the new_page_converted numpy array.

f. Simulate Sample for the control **Group** Simulate n_{old} transactions with a conversion rate of p_{old} under the null hypothesis. Store these n_{old} 1's and 0's in the old_page_converted numpy array.

g. Find the difference in the "converted" probability $(p'_{new} - p'_{old})$ for your simulated samples from the parts (e) and (f) above.

```
In [27]: new_page_converted.mean() - old_page_converted.mean()
Out[27]: -0.0030937697877378018
```

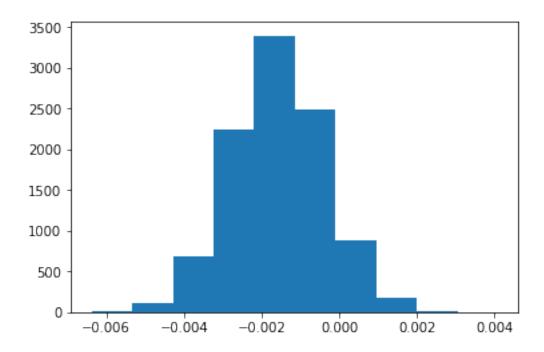
h. Sampling distribution Re-create new_page_converted and old_page_converted and find the $(p'_{new} - p'_{old})$ value 10,000 times using the same simulation process you used in parts (a) through (g) above.

Store all $(p'_{new} - p'_{old})$ values in a NumPy array called p_diffs.

```
In [28]: # Sampling distribution
    p_diffs = []
    size = df2.shape[0]
    for _ in range(10000):
        bootstrap = df2.sample( size ,replace = True)
        new_page_converted = bootstrap.query('group =="treatment"')
        old_page_converted = bootstrap.query('group == "control"')
        P_new = new_page_converted.query('converted == 1').shape[0] / new_page_converted.sh
        P_old = old_page_converted.query('converted == 1').shape[0] / old_page_converted.sh
        p_diffs.append(P_new - P_old)
In [29]: plt.hist(p_diffs)
```

Out[29]: []

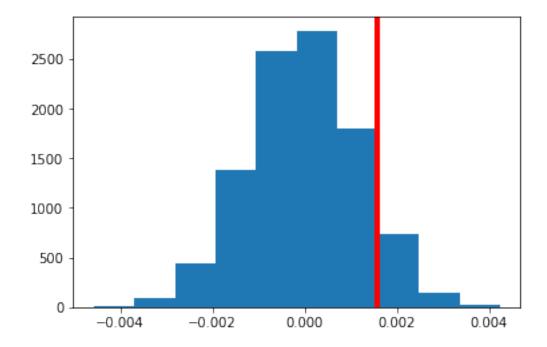
plt.plot()



i. Histogram Plot a histogram of the **p_diffs**. Does this plot look like what you expected? Use the matching problem in the classroom to assure you fully understand what was computed here.

Also, use plt.axvline() method to mark the actual difference observed in the df2 data (recall obs_diff), in the chart.

Tip: Display title, x-label, and y-label in the chart.



j. What proportion of the **p_diffs** are greater than the actual difference observed in the df2 data?

```
In [31]: (null_vals > obs_diff).mean()
Out[31]: 0.09310000000000000
```

k. Please explain in words what you have just computed in part **j** above.

- What is this value called in scientific studies?
- What does this value signify in terms of whether or not there is a difference between the new and old pages? *Hint*: Compare the value above with the "Type I error rate (0.05)".

It's called the p-value which is the probability of observing our statistics, We compare it with the alpha which is the Type one error rate, if the p-value is small we choose H1 and if its large we choose H0

I. Using Built-in Methods for Hypothesis Testing We could also use a built-in to achieve similar results. Though using the built-in might be easier to code, the above portions are a walk-through of the ideas that are critical to correctly thinking about statistical significance.

Fill in the statements below to calculate the: - convert_old: number of conversions with the old_page - convert_new: number of conversions with the new_page - n_old: number of individuals who were shown the old_page - n_new: number of individuals who were shown the new_page

```
In [32]: import statsmodels.api as sm
    # number of conversions with the old_page
    convert_old = df2.query('converted =="0"')
# number of conversions with the new_page
```

```
convert_new =df2.query('converted ==1')

# number of individuals who were shown the old_page
n_old = df2.query('converted =="0"').shape[0]

# number of individuals who received new_page
n_new = df2.query('converted ==1').shape[0]
```

/opt/conda/lib/python3.6/site-packages/statsmodels/compat/pandas.py:56: FutureWarning: The panda from pandas.core import datetools

m. Now use sm.stats.proportions_ztest() to compute your test statistic and p-value. Here is a helpful link on using the built in.

The syntax is:

```
proportions_ztest(count_array, nobs_array, alternative='larger')
```

where, - count_array = represents the number of "converted" for each group - nobs_array = represents the total number of observations (rows) in each group - alternative = choose one of the values from [two-sided, smaller, larger] depending upon two-tailed, left-tailed, or right-tailed respectively. >Hint: It's a two-tailed if you defined H_1 as $(p_{new} = p_{old})$. It's a left-tailed if you defined H_1 as $(p_{new} > p_{old})$.

The built-in function above will return the z_score, p_value.

Tip: You don't have to dive deeper into z-test for this exercise. Try having an overview of what does z-score signify in general.

n. What do the z-score and p-value you computed in the previous question mean for the conversion rates of the old and new pages? Do they agree with the findings in parts **j.** and **k.**?

Tip: Notice whether the p-value is similar to the one computed earlier. Accordingly, can you reject/fail to reject the null hypothesis? It is important to correctly interpret the test statistic and p-value.

p_value>0.05 we will reject null values

Part III - A regression approach

1.0.7 ToDo 3.1

In this final part, you will see that the result you achieved in the A/B test in Part II above can also be achieved by performing regression.

a. Since each row in the df2 data is either a conversion or no conversion, what type of regression should you be performing in this case?

we should use logistic regression

b. The goal is to use **statsmodels** library to fit the regression model you specified in part **a.** above to see if there is a significant difference in conversion based on the page-type a customer receives. However, you first need to create the following two columns in the df2 dataframe: 1. intercept - It should be 1 in the entire column. 2. ab_page - It's a dummy variable column, having a value 1 when an individual receives the **treatment**, otherwise 0.

c. Use **statsmodels** to instantiate your regression model on the two columns you created in part (b). above, then fit the model to predict whether or not an individual converts.

d. Provide the summary of your model below, and use it as necessary to answer the following questions.

```
In [37]: results.summary2()
Out[37]: <class 'statsmodels.iolib.summary2.Summary'>
                         Results: Logit
      ______
                                No. Iterations:
                                               6.0000
                     Logit
      Dependent Variable: converted Pseudo R-squared: 0.000
                    2022-05-10 21:58 AIC:
      Date:
                                              212780.3502
      No. Observations: 290584
                                BIC:
                                              212801.5095
      Df Model:
                    1
                                Log-Likelihood: -1.0639e+05
                             LL-Null: -1.0639e+05
      Df Residuals: 290582
```

Converged:	1.0000		Scale:		1.0000	
	Coef.	Std.Err.	z	P> z	[0.025	0.975]
intercept	-1.9888	0.0081	-246.6690	0.0000	-2.0046	-1.9730
treatment	-0.0150	0.0114	-1.3109	0.1899	-0.0374	0.0074
========	=======	:=======	:=======	:======	:======	======
11 11 11						

e. What is the p-value associated with **ab_page**? Why does it differ from the value you found in **Part II**?

Hints: - What are the null and alternative hypotheses associated with your regression model, and how do they compare to the null and alternative hypotheses in **Part II**? - You may comment on if these hypothesis (Part II vs. Part III) are one-sided or two-sided. - You may also compare the current p-value with the Type I error rate (0.05).

in partII p_value is equal 0.9 and in partIII p_value is equal 0.18, as p-value partII > p-value partIII, but both of them is larger than the alpha. so we reject null hypothesis

f. Now, you are considering other things that might influence whether or not an individual converts. Discuss why it is a good idea to consider other factors to add into your regression model. Are there any disadvantages to adding additional terms into your regression model?

Adding other factors helps precision the model

- **g.** Adding countries Now along with testing if the conversion rate changes for different pages, also add an effect based on which country a user lives in.
 - 1. You will need to read in the **countries.csv** dataset and merge together your df2 datasets on the appropriate rows. You call the resulting dataframe df_merged. Here are the docs for joining tables.
 - 2. Does it appear that country had an impact on conversion? To answer this question, consider the three unique values, ['UK', 'US', 'CA'], in the country column. Create dummy variables for these country columns. >Hint: Use pandas.get_dummies() to create dummy variables. You will utilize two columns for the three dummy variables.

Provide the statistical output as well as a written response to answer this question.

```
In [38]: # Read the countries.csv
         df3 = pd.read_csv('countries.csv')
         df3.head()
Out[38]:
            user_id country
         0
             834778
         1
             928468
                          US
         2
             822059
                          IJK
             711597
         3
                          IJK
             710616
                          IJK
```

```
In [39]: # Join with the df2 dataframe
         df_merge = pd.merge(df2,df3)
         df_merge.head()
Out [39]:
            user_id
                                       timestamp
                                                     group landing_page
                                                                          converted
             851104 2017-01-21 22:11:48.556739
                                                  control
                                                               old_page
                                                                                  0
         1
             804228 2017-01-12 08:01:45.159739 control
                                                               old_page
                                                                                  0
         2
             864975 2017-01-21 01:52:26.210827
                                                   control
                                                               old_page
                                                                                  1
         3
             936923 2017-01-10 15:20:49.083499
                                                               old_page
                                                                                  0
                                                   control
             719014 2017-01-17 01:48:29.539573
                                                               old_page
                                                                                  0
                                                   control
            intercept
                       control
                                treatment country
         0
                    1
                                         0
                                                 US
                              1
         1
                    1
                                         0
                                                 US
                              1
         2
                    1
                                                 US
                              1
                                         0
         3
                    1
                              1
                                         0
                                                 US
                     1
                              1
                                                 US
In [40]: # Create the necessary dummy variables
         df_merge[['UK', 'US', 'CA']] = pd.get_dummies(df_merge['country'])
         df_merge = df_merge.drop(columns=['CA'])
         df_merge.head()
Out [40]:
            user_id
                                       timestamp
                                                     group landing_page
                                                                          converted
             851104 2017-01-21 22:11:48.556739
                                                  control
                                                               old_page
                                                                                  0
             804228 2017-01-12 08:01:45.159739 control
                                                                                  0
         1
                                                               old_page
         2
             864975 2017-01-21 01:52:26.210827
                                                   control
                                                               old_page
                                                                                  1
             936923 2017-01-10 15:20:49.083499
                                                               old_page
                                                                                  0
         3
                                                  control
         4
             719014 2017-01-17 01:48:29.539573
                                                   control
                                                               old_page
                                                                                  0
                                 treatment country
                                                     UK
                                                         US
            intercept
                       control
         0
                                                      0
                                                          0
                    1
                              1
                                         0
                                                 US
         1
                    1
                              1
                                         0
                                                 US
                                                      0
                                                          0
         2
                    1
                              1
                                         0
                                                 US
                                                      0
                                                          0
         3
                    1
                              1
                                         0
                                                      0
                                                          0
                                                 US
                              1
                                         0
                                                      0
                                                          0
                                                 US
```

h. Fit your model and obtain the results Though you have now looked at the individual factors of country and page on conversion, we would now like to look at an interaction between page and country to see if are there significant effects on conversion. Create the necessary additional columns, and fit the new model.

Provide the summary results (statistical output), and your conclusions (written response) based on the results.

Tip: Conclusions should include both statistical reasoning, and practical reasoning for the situation.

Hints: - Look at all of p-values in the summary, and compare against the Type I error rate (0.05). - Can you reject/fail to reject the null hypotheses (regression model)? - Comment on the effect of page and country to predict the conversion.

```
In [42]: # Fit your model, and summarize the results
        df2['intercept'] = 1
        lr = sm.Logit(df2['converted'], df2[['intercept', 'treatment']])
        result = lr.fit()
        #results.pvalues
        result.summary2()
Optimization terminated successfully.
        Current function value: 0.366118
        Iterations 6
Out[42]: <class 'statsmodels.iolib.summary2.Summary'>
                               Results: Logit
        _____
        Model: Logit No. Iterations: 6.0000 Dependent Variable: converted Pseudo R-squared: 0.000

      Date:
      2022-05-10 21:58 AIC:
      212780.3502

      No. Observations:
      290584 BIC:
      212801.5095

      Df Model:
      1 Log-Likelihood:
      -1.0639e+05

      Df Residuals:
      290582 LL-Null:
      -1.0639e+05

        Converged: 1.0000 Scale: 1.0000
        -----
                    Coef. Std.Err. z P>|z| [0.025 0.975]
        _____
        intercept -1.9888 0.0081 -246.6690 0.0000 -2.0046 -1.9730
        treatment -0.0150 0.0114 -1.3109 0.1899 -0.0374 0.0074
        _____
```

Hypothesis is helping to draw conclusion from sample data. in the first we assume null hypothesis is true but after testing p_value we reject null hypothesis if it is larger than alpha ## Final Check!

Congratulations! You have reached the end of the A/B Test Results project! You should be very proud of all you have accomplished!

Tip: Once you are satisfied with your work here, check over your notebook to make sure that it satisfies all the specifications mentioned in the rubric. You should also probably remove all of the "Hints" and "Tips" like this one so that the presentation is as polished as possible.

Submission You may either submit your notebook through the "SUBMIT PROJECT" button at the bottom of this workspace, or you may work from your local machine and submit on the last page of this project lesson.

1. Before you submit your project, you need to create a .html or .pdf version of this notebook in the workspace here. To do that, run the code cell below. If it worked correctly, you should

- get a return code of 0, and you should see the generated .html file in the workspace directory (click on the orange Jupyter icon in the upper left).
- 2. Alternatively, you can download this report as .html via the **File > Download as** submenu, and then manually upload it into the workspace directory by clicking on the orange Jupyter icon in the upper left, then using the Upload button.
- 3. Once you've done this, you can submit your project by clicking on the "Submit Project" button in the lower right here. This will create and submit a zip file with this .ipynb doc and the .html or .pdf version you created. Congratulations!