

```
In [1]: import os
import cv2
import imageio
import numpy as np
from PIL import Image
from matplotlib import pyplot as plt
from scipy import io
from sklearn.neighbors import kneighbors_graph
from sklearn.cluster import KMeans
from scipy.spatial import distance_matrix
```

```
In [2]: gt_path = 'BSR\\BSDS500\\data\\groundTruth\\test'
pics = os.listdir(gt_path)[0:50]

# create ground truth array

groundTruth = []

for filename in pics:

    data = io.loadmat(os.path.join(gt_path, filename))
    c = data['groundTruth'].shape[1]

    groundTruthPerImage = []
    for n in range(c):
        edge_data = data['groundTruth'][0][n][0][0][0]
        groundTruthPerImage.append(edge_data)

    groundTruthPerImage = np.array(groundTruthPerImage)
    groundTruth.append(groundTruthPerImage)

groundTruth = np.array(groundTruth, dtype=object)

#plt.imshow(groundTruth[0][0])
#plt.show()
```

In [3]:

```
#####
root = "BSR\\BSDS500"
PATH = os.path.join(root, 'data\\groundTruth\\test')

save_pth = os.path.join(root, 'data\\converted_mat_jpg', 'test')
os.makedirs(save_pth, exist_ok=True) #to save gt converted images
pics = os.listdir(PATH)[0:50]

# create converted images for ground truth segmentation
i = 0
for filename in pics:
    data = io.loadmat(os.path.join(PATH, filename))
    c = data['groundTruth'].shape[1]
    for n in range(c):
        edge_data = data['groundTruth'][0][n][0][0][1]
        edge_data_255 = edge_data * 255
        new_img_name = filename.split('.')[0] + '(' + str(n) + ')' + '.jpg'
        imageio.imwrite(os.path.join(save_pth, new_img_name), edge_data_255) #
    pics[i] = filename.split('.')[0] + '.jpg'
    i = i + 1

# Visualize the image and the ground truth segmentation

root = "BSR\\BSDS500\\data\\images\\test"
converted = "BSR\\BSDS500\\data\\converted_mat_jpg\\test"

for filename in pics:
    gt = []
    im = Image.open(os.path.join(root, filename))

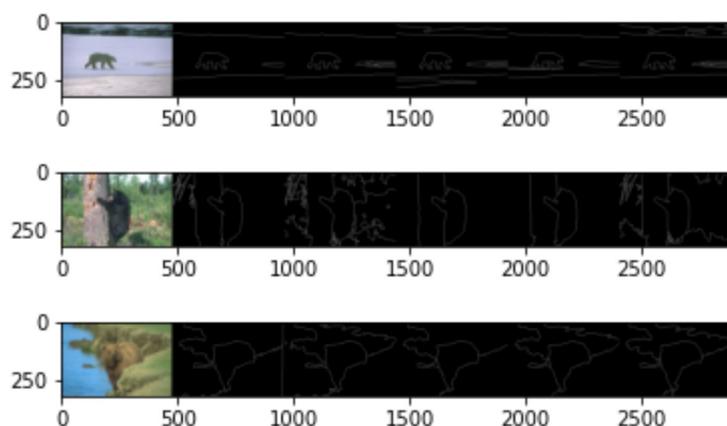
    for file in os.listdir(converted):
        if file.startswith(filename.split('.')[0]):
            gt.append(file)

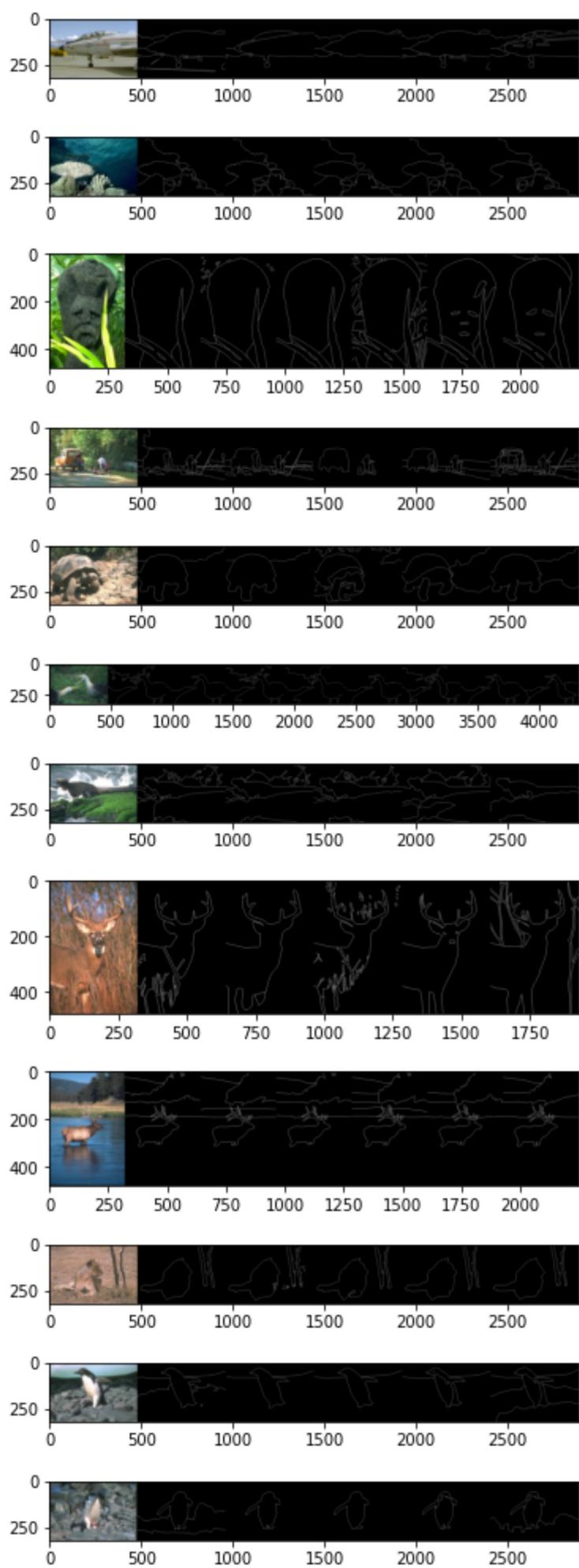
    new_im = Image.new('RGB', (im.width * (len(gt) + 1), im.height)) #HORIZONTAL
    new_im.paste(im, (0, 0))

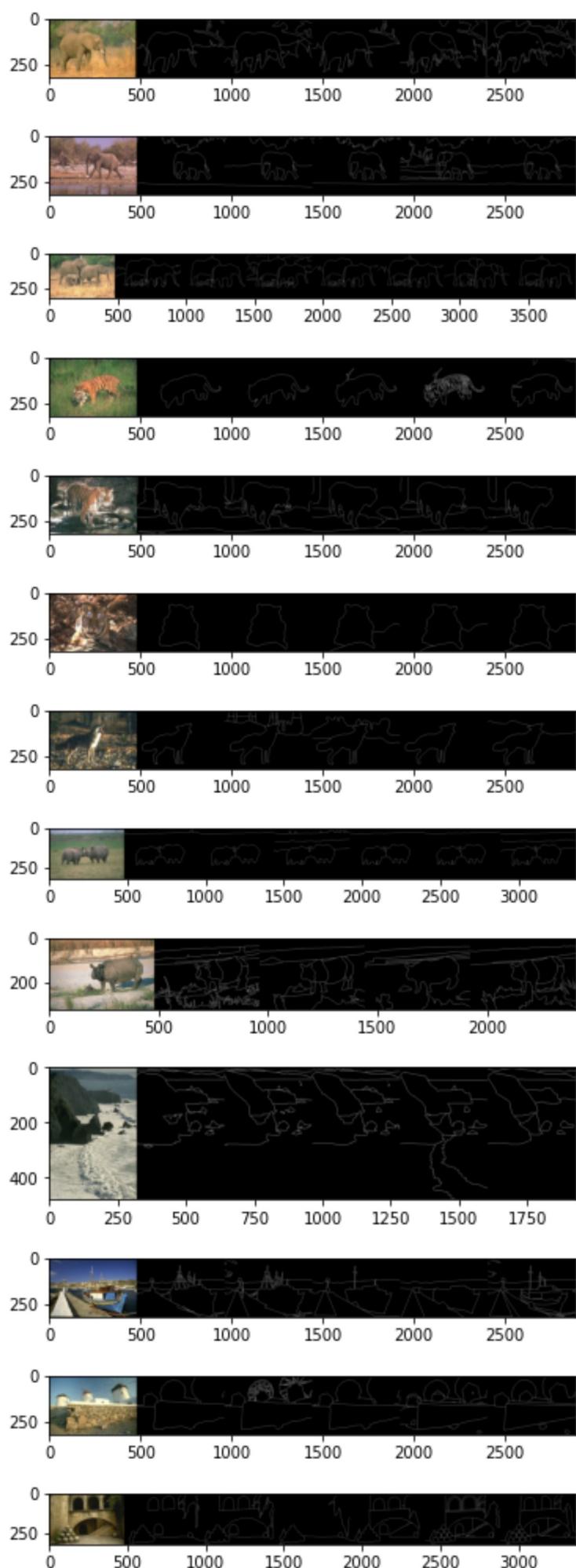
    for i in range(len(gt)):
        im_gt = Image.open(os.path.join(converted, gt[i]))
        new_im.paste(im_gt, (im.width * (i + 1), 0))
# plt.imshow(new_im)
# plt.show()

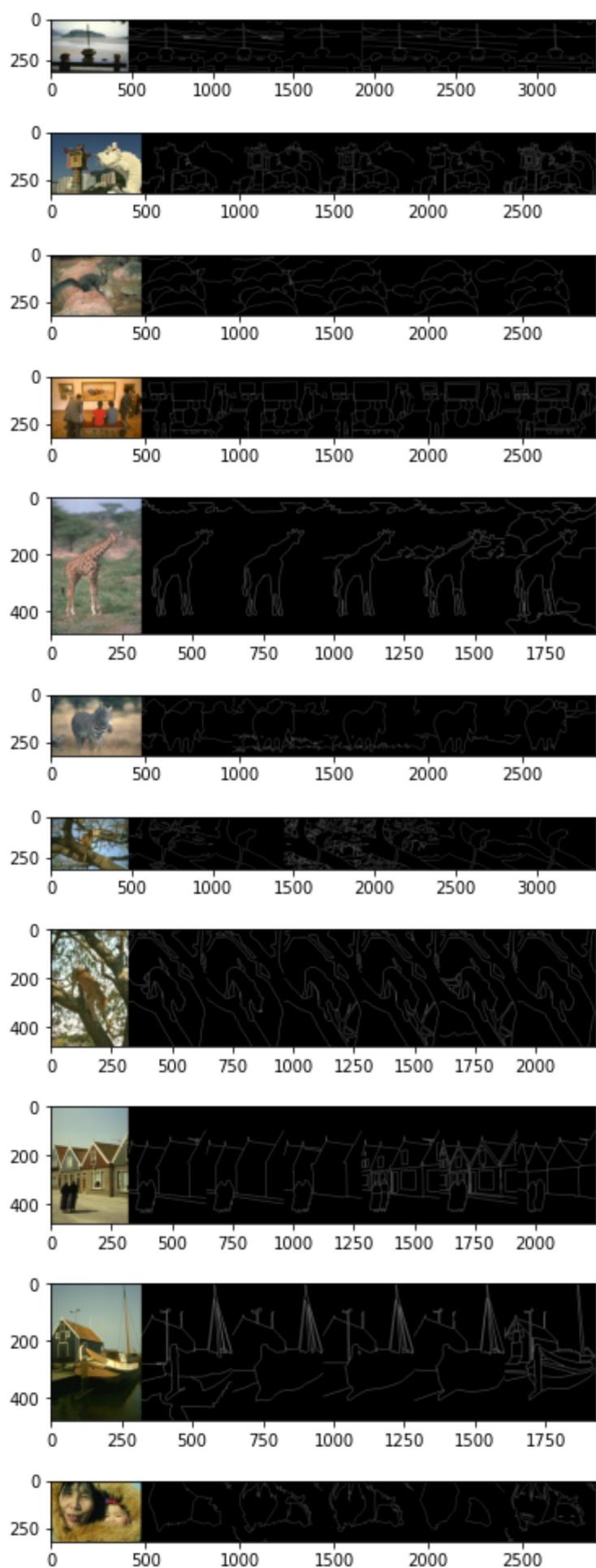
#####

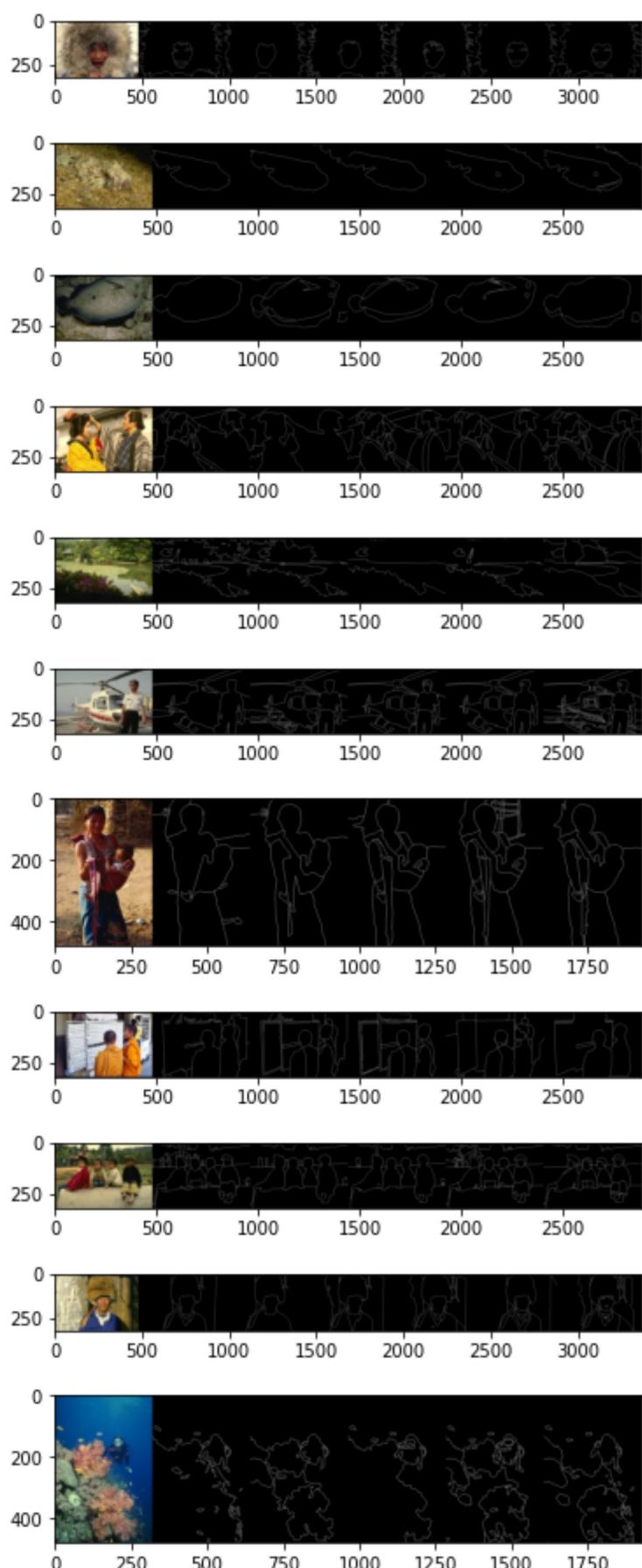
```











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In [4]: # original images

images = []

images_path = "BSR\\BSDS500\\data\\images\\test\\"

for filename in pics:
    img = cv2.imread(os.path.join(images_path, filename))
    im_rgb = cv2.cvtColor(img, cv2.COLOR_BGR2RGB)
    images.append(im_rgb)

images = np.array(images, dtype=object)
plt.imshow(images[0])
plt.show()

flattened_images = np.empty((0, 3))

for i in range(50):
    flattened_image = images[i].reshape(images[i].shape[0] * images[i].shape[1],
    flattened_images = np.concatenate((flattened_images, flattened_image))
```



In [11]:

```
from sklearn.cluster import KMeans

# k = 3 5 7 9 11
def image_segmentation(k):
    segmented_images = []
    flat_segmented_images = []

    k_means = KMeans(n_clusters=k)
    k_means.fit(flattened_images)

    # build segmented images from clustering labels

    labels = k_means.labels_
    labels.reshape(labels.shape[0], 1)

    index = 0
    for i in range(50):
        size = images[i].shape[0] * images[i].shape[1]
        flat_segmentation = labels[index:size + index]

        segmented_images.append(flat_segmentation.reshape(images[i].shape[0], im

        flat_segmented_images.append(flat_segmentation)
        index += size

    flat_segmented_images = np.array(flat_segmented_images, dtype=object)

    return segmented_images, flat_segmented_images
```

```
In [12]: def recreate_groundTruth(image_index, gt_index, flat_segmented_images, k):  
  
    import sklearn.metrics.cluster as sk  
    from scipy.optimize import linear_sum_assignment  
  
    flattened_gt = np.array(groundTruth[image_index][gt_index]).reshape(  
        images[image_index].shape[0] * images[image_index].shape[1], 1)  
  
    # add dummy classes to match k clusters in case ground truth clusters < k  
    max_gt = flattened_gt.max()  
    if max_gt < k:  
        j = 1  
        for i in range(max_gt, k+1):  
            flattened_gt[i][0] = max_gt + j  
            j+=1  
  
    # add dummy classes to match k clusters in case k_means classes < k  
    max_seg = flat_segmented_images.max()  
    if max_seg < k:  
        j = 1  
        for i in range(max_seg, k+1):  
            flat_segmented_images[i] = max_seg + j  
            j+=1  
  
    contingency_matrix = sk.contingency_matrix(flattened_gt, flat_segmented_images)  
    gt_clusters = contingency_matrix.shape[0]  
  
    # max matching  
  
    idx = linear_sum_assignment(-contingency_matrix.T)[1]  
    for i in range(k):  
        contingency_matrix[[idx[i], i]] = contingency_matrix[[i, idx[i]]]  
        replaced_index = np.argwhere(flattened_gt == (idx[i]+1))  
        # give the major k clusters new values  
        flattened_gt[replaced_index] = gt_clusters + i + 1  
  
    # give the minor clusters (which will be merged into the major clusters) new  
    # values_gt = np.unique(flattened_gt)  
    for i in range(gt_clusters - k):  
        replaced_index = np.argwhere(flattened_gt == (values_gt[i]))  
        flattened_gt[replaced_index] = gt_clusters + k + i + 1  
  
    # merge the minor clusters into the major clusters  
    contingency_matrix = sk.contingency_matrix(flattened_gt, flat_segmented_images)  
    for i in range(k, gt_clusters):  
        replaced_index = np.argwhere(flattened_gt == (gt_clusters + i + 1))  
        flattened_gt[replaced_index] = gt_clusters + np.argmax(contingency_matrix[i])  
        contingency_matrix[np.argmax(contingency_matrix[i])] += contingency_matrix[i]  
    contingency_matrix = contingency_matrix[:k,:]  
  
    new_gt = flattened_gt.reshape((images[image_index].shape[0], images[image_index].shape[1]))  
  
    return new_gt, contingency_matrix
```

```
In [13]: def evaluate_segmentation(image_index, gt_index, flat_segmented_images, k):  
    new_gt,contingency_matrix = recreate_groundTruth(image_index,gt_index,flat_s  
    # calculate F-score  
  
    precision = np.zeros((k, 1))  
    recall = np.zeros((k, 1))  
    f_score = np.zeros((k, 1))  
  
    for i in range(k):  
        TP = np.amax(contingency_matrix[:, i])  
        precision[i] = TP / np.sum(contingency_matrix[:, i])  
        recall[i] = TP / np.sum(contingency_matrix[i])  
  
        f_score[i] = (2 * precision[i] * recall[i]) / (precision[i] + recall[i])  
  
    f_score_avg = np.mean(f_score)  
  
    #####  
    # calculate conditional Entropy  
  
    pixels_count = images[image_index].shape[0] * images[image_index].shape[1]  
    entropy = 0  
    for i in range(k):  
        sum_cluster = np.sum(contingency_matrix[:, i])  
  
        H_cluster = 0  
        for j in range(k):  
            n_ij = contingency_matrix[i][j]  
            if n_ij != 0:  
                H_cluster += (n_ij / pixels_count) * np.log10(n_ij / sum_cluster)  
  
        entropy -= H_cluster  
  
    #####  
    return f_score_avg, entropy , new_gt
```

```
In [8]: k_clusters = [3,5,7,9,11]

fig, ax = plt.subplots(1, 5, figsize=(35, 10))
seg_fig, seg_axs = plt.subplots(50, 5, figsize=(70, 500))

for k in k_clusters:

    plot = k_clusters.index(k)

    F_score_entropy_list = np.zeros((50, 2))
    segmented_imgs, flat_segmented_imgs = image_segmentation(k=k)

    for img_index in range(50):
        seg_axs[img_index][plot].imshow(segmented_imgs[img_index])

        seg_f_score_avg = 0
        seg_entropy_avg = 0
        gt_count = len(groundTruth[img_index])

        for gt_img_index in range(gt_count):
            F_score, Entropy, _ = evaluate_segmentation(img_index, gt_img_index,
                seg_f_score_avg += F_score
                seg_entropy_avg += Entropy

        seg_f_score_avg /= gt_count
        seg_entropy_avg /= gt_count

        F_score_entropy_list[img_index][0] = seg_f_score_avg
        F_score_entropy_list[img_index][1] = seg_entropy_avg

    print("for k = {} : F-score per dataset: {}    Entropy per dataset: {}".format(
        F_score_entropy_list[:, 0]) / 50, np.sum(F_score_entropy_list[:, 1]) / 5

    ax[plot].set_axis_off()
    table = ax[plot].table(
        cellText=F_score_entropy_list,
        rowLabels=[r + 1 for r in range(50)],
        colLabels=["Average F-score", "Average Conditional Entropy"],
        cellLoc='center',
        loc='upper left')
    table.scale(1, 5)
    ax[plot].set_title('for k = {}'.format(k))

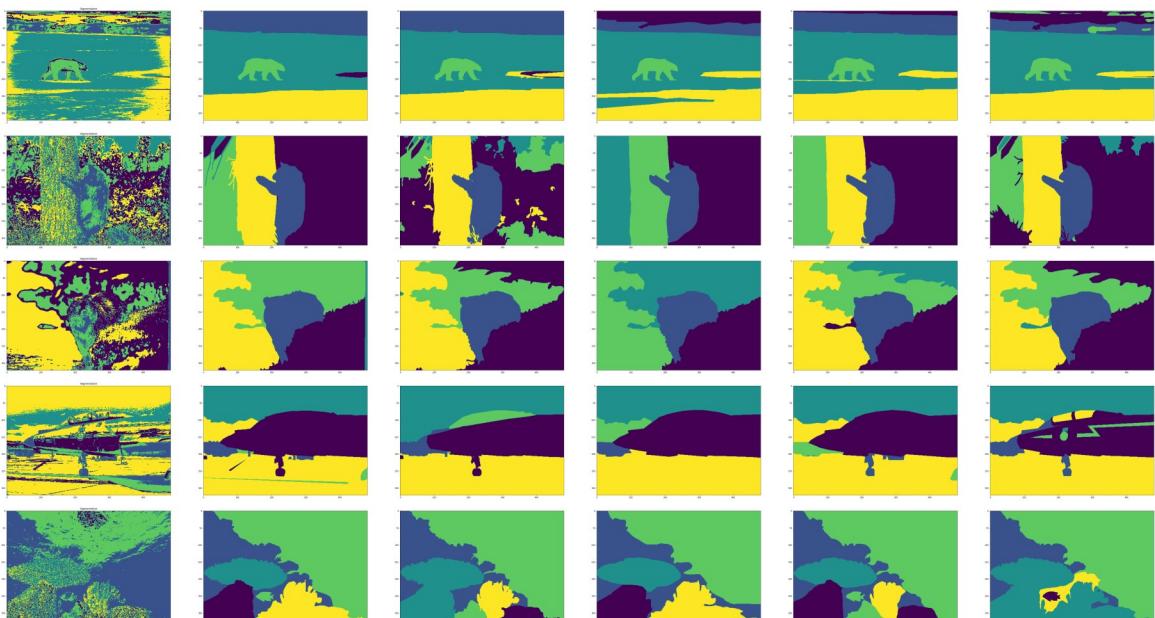
plt.show()

for k = 3 : F-score per dataset: 0.7025027323162596    Entropy per dataset: 0.267
7956151581025
for k = 5 : F-score per dataset: 0.6807246951194934    Entropy per dataset: 0.327
3995441475374
for k = 7 : F-score per dataset: 0.6987563859007224    Entropy per dataset: 0.325
0597296048128
for k = 9 : F-score per dataset: 0.7475784559070928    Entropy per dataset: 0.360
0018064443664
for k = 11 : F-score per dataset: 0.7810211292750207    Entropy per dataset: 0.38
2556285253411
```

for k = 3	Average F-score	Average Conditional Entropy	for k = 5	Average F-score	Average Conditional Entropy	for k = 7	Average F-score	Average Conditional Entropy	for k = 9	Average F-score	Average Conditional Entropy	for k = 11	Average F-score	Average Conditional Entropy
1	0.81094307316991432	0.1212217473696293	1	0.6569736402006298	0.2736470815718778	1	0.6403721323421132	0.2038374793180106	1	0.770437299095849	0.34099124180127854	1	0.7377160972668363	0.17722526123746707
2	0.6562471815340151	0.32459860794591	2	0.58692168021189	0.47375482720107	2	0.5857309729944336	0.521616048282517	2	0.669080136581818	0.40903435438240204	2	0.759542761566482	0.5372721099362747
3	0.4993036131746034	0.12094261207366588	3	0.46945325050642046	0.09534344903038705	3	0.813697215558426	0.1551217080530796	3	0.9607746003783952	0.1252516520116378	3	1.0796597294500075	0.3414839128619982
4	0.60739343262747493	0.25912873779560174	4	0.55610321109698	0.309976444815653	4	0.47305658484904454	0.2488773513610088	4	0.609632798025262	0.22751488087200028	4	0.7073377983880123	0.3249888731706737
5	0.480010473269540804	0.21944033605640804	5	0.4126128043347274	0.33253098968307124	5	0.6735151849253349	0.3008204719803746	5	0.67500335102343776	0.3212089426956213	5	0.7537037208242909	0.1344219760148123
6	0.6260953204741983	0.1174978274338404	6	0.5871996322801628	0.48159940008517	6	0.5752699793917009	0.4652332055156586	6	0.611680333775247	0.5270866620438	6	0.67050908848012444	0.55860902869102
7	0.71234103012468905	0.34191104563673045	7	0.8239503210512127	0.452201800886882	7	0.8316055508040963	0.5032482496081198	7	0.81141643730962	0.2443254496082826	7	0.8128517550831769	0.454387995045342
8	0.555346045388381	0.3838037781153931	8	0.576180968031043	0.479277815627215	8	0.647054148388416	0.4743655119320319	8	0.8258708835152087	0.49008454562343756	8	0.8753063525402093	0.5275010806226037
9	0.6313082771146071	0.1850802451114025	9	0.5721308744340748	0.2335739805179053	9	0.65140014717664	0.2086346172296758	9	0.7019310372755298	0.27910927711544	9	0.841615145015683	-0.4112615300346973
10	0.67916284539895	0.273296029096833	10	0.75896480571055	0.3912094485038753	10	0.76789524080679517	0.393137632282244	10	0.710634105614551	0.311164681275885364	10	1.03283055429373	0.3766022263139865
11	0.780049547895326	0.1813910781900768	11	0.7545870225730608	0.3485377754669683	11	0.8802880808291206	0.3321953321896098	11	0.108118636634838	0.4180126143324293	11	1.1301154280032553	0.4534031830466888
12	0.7647904212861425	0.255152311782686467	12	0.5181361841515169	0.3052135736305485	12	0.723362928223563	0.3587671758834747	12	0.8048161177589965	0.4199613018806508	12	0.8994775976186333	0.3980044849215624
13	0.7284751443771144	0.2838240629088846	13	0.8046153554064239	0.23232416154610942	13	0.8804140584731586	0.33801711032615956	13	1.0054509102409813	0.4204959660840813	13	1.0283055429373	0.3766022263139865
14	0.89382672678502	0.221005981388406745	14	0.92784724960343	0.268847872104913	14	0.98571832520421	0.3203211307891798	14	1.057483036303585	0.47955639188798	14	0.9704367180139087	0.2035402561168127
15	0.88514396762416485	0.277173248052692	15	1.108103818818859	0.31120181191334867	15	1.351938027959696	0.3442368475463314	15	1.388104644055919	0.295322293676987	15	1.4089063079744004	0.3859481466575256
16	0.697598803932929	0.178764198170570544	16	0.6822951241252629	0.3258957025434893	16	0.5420925843705135	0.296648415533174	16	0.644592680434950	0.4080111387404239	16	0.668499974205827	0.3720014622815193
17	0.795775698915306	0.3080421287954175	17	0.567469437202481	0.3076715560118234	17	0.69780059461763	0.3701971363155005	17	0.7342785354617136	0.4704217747782115	17	0.7561514824383027	0.5368732999741224
18	0.6845755821208414	0.2695952805460606	18	0.74849313384761	0.36393795849276173	18	0.5684348509285278	0.299142551171781	18	0.660209621043649	0.418183795782114	18	0.7194809312051581	0.4354568827115384
19	1.015172494913984	0.18773714424760508	19	1.1607229110136131	0.24803991285277477	19	1.079572085175514644	0.24011170951878866	19	1.1209511048465098	0.32877462821292118	19	1.172321039709251	0.327884249280982787
20	0.5179517914976458	0.327474174538834	20	0.5770578535159964	0.3696901971460729	20	0.5391598373050582	0.4926221305480606	20	0.556039575101840517	0.4511441304050187	20	0.69649115171492476	0.3560242404501703
21	0.4883801777433235	0.3493189978488025	21	0.8772421580348091	0.2950034435157548	21	1.043507576225152	0.4429606704879506	21	1.0902589738833031	0.33354606843808688	21	1.1294285715305099	0.5574321603103769
22	0.74183618694748433	0.5747304893320667	22	0.8634064048477382	0.329205407371852	22	1.0514699708708212034	0.32862051307212034	22	1.1010948477999197	0.4262017205107383	22	1.1596616088368363	0.4605870339708783
23	0.798565359632658	0.1586732429147763	23	0.71140699636367	0.1307246125285222	23	0.932536357173806	0.0659368907947891	23	1.1209712126761616	0.1831806463561724	23	1.137561409552833	0.2728021028804951
24	0.64822932131669377	0.2719074229425455	24	0.5501932728160634	0.4574161006437717	24	0.6149019758130454	0.515138578495707	24	0.56830673628562	0.5471321928966981	24	0.5425426107813723	0.5567765550524251
25	0.84040066327059514	0.1865057556832115	25	0.8647401455274715	0.29213110703620453	25	0.7606041325205086	0.3181441237603056	25	0.7242994815884489	0.2839517291533556	25	0.787225374311423	0.3262571770811527
26	0.682361320121663	0.322880230736637	26	0.550782708462907	0.41503821177946787	26	0.5604511545971173	0.3893508156395934	26	0.525158589716759	0.4860726673737017	26	0.557851724887055	0.4190875948611066
27	0.559528452099282	0.3454693387651456	27	0.512840398697931	0.4802857647671755	27	0.641361284200168	0.3963461338083323	27	0.786303488304383	0.4289446426180599	27	0.8390411309074855	0.451224128752776
28	0.63152056146623942	0.277111046623942	28	0.60304815957949	0.3845606973534544	28	0.4921182178708701	0.17075096841315	28	0.5447893070870222	0.411996933753847	28	0.580407274488949	0.4707025205709993
29	0.7136838513646469	0.253988382926115	29	0.6475148293888231	0.3037162402528047	29	0.4887967028699494	0.2770568459719313	29	0.4604866087328724	0.287144334728793	29	0.43247741559454513	0.2220034492830131
30	0.766544506136642	0.272710527737046	30	0.64892215159909	0.31211701548482423	30	0.6042841572824245	0.31886088134923	30	0.6205514292860942	0.386525252511896	30	0.5767214151902393	0.597092061806334
31	0.70581473330579578	0.3222633366377703	31	0.5444661007107174	0.375602077525499	31	0.39627447055048796	0.317022184206593	31	0.404254930361854	0.3773812049636214	31	0.6755081385882001	0.4677145324557281
32	0.713351102123631	0.2945068812921325	32	0.6881751422864639	0.4090455383337717	32	0.5013612915033419	0.00719129182489746	32	0.68096107321509134	0.0685581866569437	32	0.35756918731958466	0.28252310839120203
33	0.68978080931306487	0.2202490732122026	33	0.717800814557345	0.34172013598736136	33	0.731911243032881	0.3517548849435959	33	0.83414917312059563	0.2799446505199595	33	0.8998081448138417	0.37340601830639547
34	0.6177408117071114	0.26135102053048784	34	0.6294585756830106	0.3817395755276455	34	0.709281972962052	0.377300518471779	34	0.8410421402212611	0.39121265929308524	34	0.8256079732246151	0.3112113968637046
35	0.622552264652358	0.33192031153591364	35	0.54344858271112	0.495514748918723	35	0.5429955151051085	0.47221849664937983	35	0.55373016063755457	0.4267711350699865	35	0.611048569660605	0.1977991253561737
36	0.6122089117947469	0.278811765127073	36	0.635822947219176	0.11579433986648443	36	0.77753126093434309	0.141117360491283	36	0.775531173611750175	0.333993173611750175	36	0.88224750713992977	0.4889220412810174
37	0.7111099488448422	0.2687872071315745	37	0.4874735054140746	0.39456380545282887	37	0.5045758308456413	0.2497389515129987	37	0.5460865067160211	0.3899830781903668	37	0.6755081385882001	0.4677145324557281
38	0.7025988750586394	0.2576230853261575	38	0.57971905705528334	0.189530219423626	38	0.5628112679896443	0.05984327317092216	38	0.56487078774667464	0.2626595848840488	38	0.775531173611750175	0.333993173611750175
39	0.6122552264652358	0.278811765127073	39	0.635822947219176	0.11579433986648443	39	0.77753126093434309	0.141117360491283	39	0.775531173611750175	0.333993173611750175	39	0.88224750713992977	0.4889220412810174
40	0.851817819038744	0.2618221222021058	40	0.6493465954541468	0.48239545954541468	40	0.6222625296017905	0.373771260491283	40	0.6465100510819296	0.3427495			

```
In [14]: segmented_imgs, flat_segmented_imgs = image_segmentation(k=5)
for img_index in range(5):
    fig, axs = plt.subplots(1, 6, figsize=(100, 20))
    axs[0].imshow(segmented_imgs[img_index] + 1)
    axs[0].set_title("Segmentation")

    for gt_img_index in range(len(groundTruth[img_index])):
        _, _, _new_gt = evaluate_segmentation(img_index, gt_img_index, flat_segm
        axs[gt_img_index + 1].imshow(_new_gt)
```



```
In [6]: # resize and get distance matrix
dist_mat=[]
for i in range(5):
    resized_image = cv2.resize(images[i], (100, 100))
    flattened_image = resized_image.reshape(resized_image.shape[0] *resized_imag
    dist_mat.append(distance_matrix(flattened_image,flattened_image,p=2))
dist_mat=np.array(dist_mat)
```

```
In [7]: def Ncut(dist_mat, k, knn):

    #lab. mat
    A = kneighbors_graph(dist_mat , knn , mode='connectivity' , include_self=False)
    D = np.diag(np.sum(A, axis=1))
    L = D - A

    #eigen
    eigen_values, eigen_vectors = np.linalg.eig(np.dot(np.linalg.inv(D),L))

    idx = eigen_values.argsort()[:1]
    eigen_values = eigen_values[idx]
    eigen_vectors = eigen_vectors[:,idx]

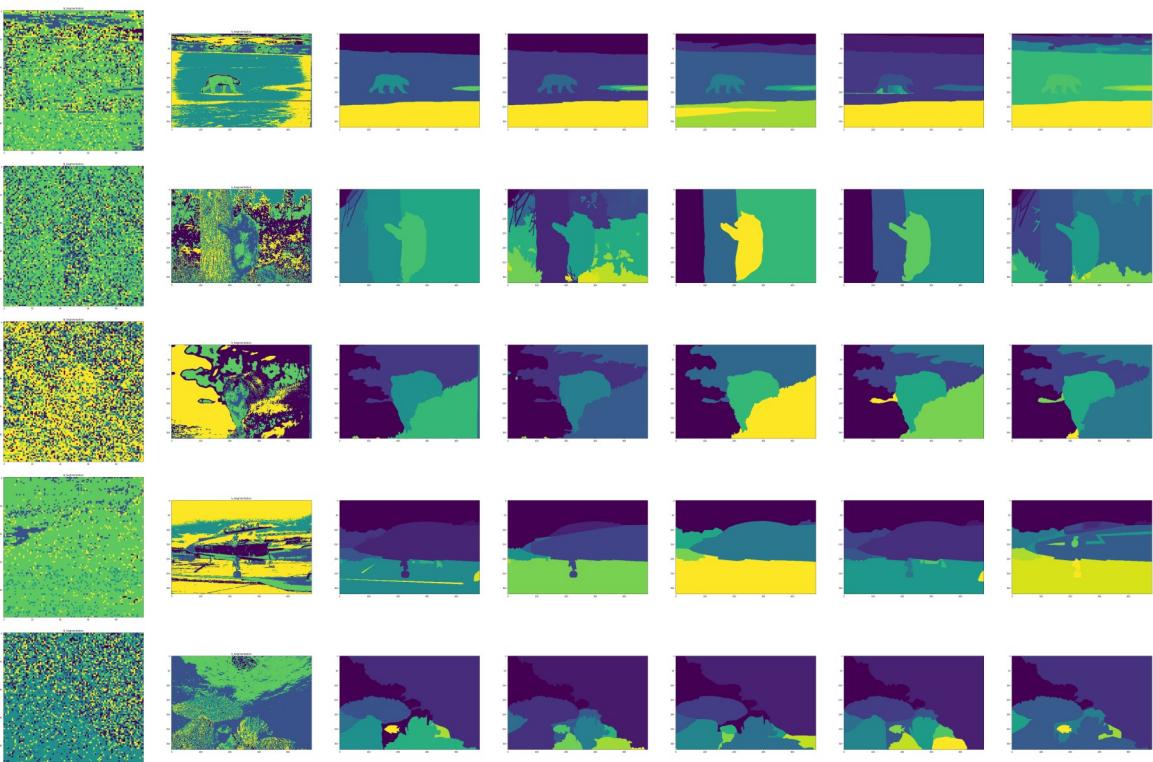
    Y = np.zeros(eigen_vectors.shape)
    for i in range(eigen_vectors.shape[0]):
        norm=np.linalg.norm(eigen_vectors[i])
        Y[i]=eigen_vectors[i]/norm

    km = KMeans(n_clusters=k).fit(Y)
    return km.labels_
```

```
In [8]: n_segmented=[]
for i in range(5):
    n_segmented.append(Ncut(dist_mat[i],k=5,knn=5))
n_segmented=np.array(n_segmented)

C:\Users\smart\sheet5\venv\lib\site-packages\ipykernel_launcher.py:17: ComplexWarning: Casting complex values to real discards the imaginary part
    app.launch_new_instance()
C:\Users\smart\sheet5\venv\lib\site-packages\ipykernel_launcher.py:17: ComplexWarning: Casting complex values to real discards the imaginary part
    app.launch_new_instance()
C:\Users\smart\sheet5\venv\lib\site-packages\ipykernel_launcher.py:17: ComplexWarning: Casting complex values to real discards the imaginary part
    app.launch_new_instance()
C:\Users\smart\sheet5\venv\lib\site-packages\ipykernel_launcher.py:17: ComplexWarning: Casting complex values to real discards the imaginary part
    app.launch_new_instance()
C:\Users\smart\sheet5\venv\lib\site-packages\ipykernel_launcher.py:17: ComplexWarning: Casting complex values to real discards the imaginary part
    app.launch_new_instance()
C:\Users\smart\sheet5\venv\lib\site-packages\ipykernel_launcher.py:17: ComplexWarning: Casting complex values to real discards the imaginary part
    app.launch_new_instance()
```

```
In [15]: for img_index in range(5):
    fig, axs = plt.subplots(1, 7, figsize=(100, 20))
    axs[0].imshow(n_segmented[img_index].reshape((100,100)))
    axs[0].set_title("N_Segmentation")
    axs[1].imshow(segmented_imgs[img_index])
    axs[1].set_title("k_Segmentation")
    for gt_img_index in range(len(groundTruth[i])):
        axs[gt_img_index + 2].imshow(groundTruth[img_index][gt_img_index])
```



```
In [18]: images=None
segmented_imgs=None
groundTruth=None
groundTruthPerImage=None
```

```
In [ ]:
```