Conditional inference tree

Learning objectives

Our learning objectives are to:

- Understand conditional inference tree (cit) algorithm Use the ML framework to:
- pre-process data train a cit model evaluate model predictability Explore a few new concepts:
- Iterative search with simulated annealing
- Selecting best model within 1 sd

Introduction

As we previously learned, linear regression models can suffer from **multicollinearity** when two or more predictor variables are highly correlated.

The methods we mentioned to overcome multicollinearity include:

- Dimensionality reduction (e.g., PCA)
- Variable selection: by hand by models

Today, we'll explore another model that performs variable selection, but in a different way: **conditional inference trees (CIT)**.

CIT

Conditional inference tree is a recursive model that works iteratively performing 2 steps:

- variable selection
- binary split

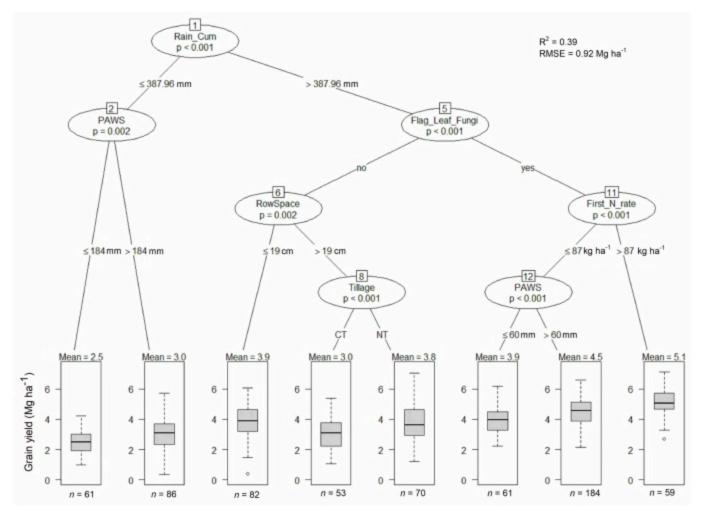
It performs **variable selection** by first running all possible bivariate models between the response variable (e.g., strength_gtex) and each individual explanatory variable (e.g., sum_precip.mm_June), in the form of **strength_gtex** ~ **sum_precip.mm_June**. Then, it selects the explanatory variable with the **lowest p-value** as the most important.

After it selects the most important variable, it performs a **binary split** on that variable, which involves finding a value of the explanatory variable which, if used to split the data in 2 groups, will minimize the error of the two splits.

After making the first split, it performs a new iteration on each of the splits, performing again variable selection and binary split.

The tree stops growing (stops iterating) when it reaches a given stopping criteria, as for example, maximum tree depth.

Let's look into how it works, with figures.



Terminology:

- **Root node**: node on top, with all observations (Rain_Cum)
- **Internal node**: all intermediate nodes (e.g., Flag_Leaf_Fungi)
- Leaf/terminal node: the bottom nodes with the boxplots

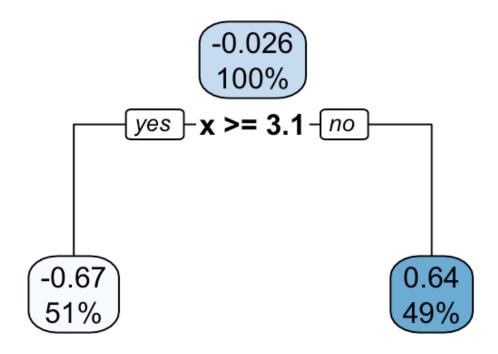
scientist with engineering this platforms can creat new specificity

Variables selected first (on top) are more important than variables selected afterwards. In this example, the most important variable in explaining grain yield is **Rain_Cum**.

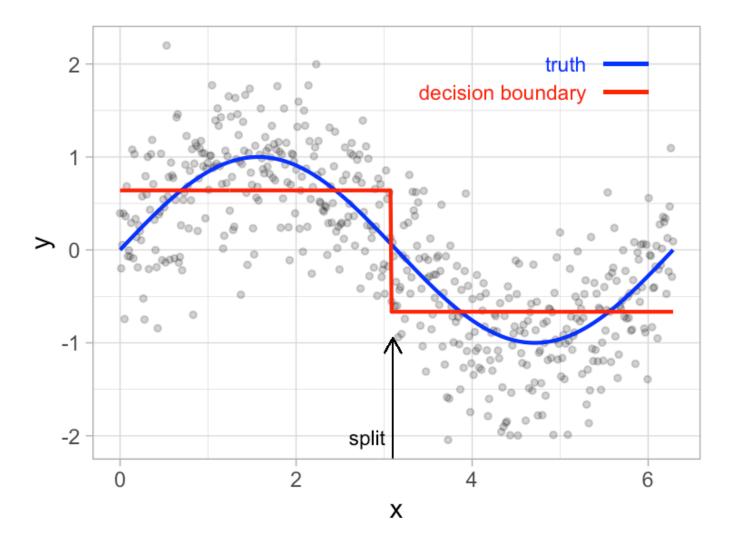
Creating partitions

Let's look into a simpler example where we are predicting y as a function of x.

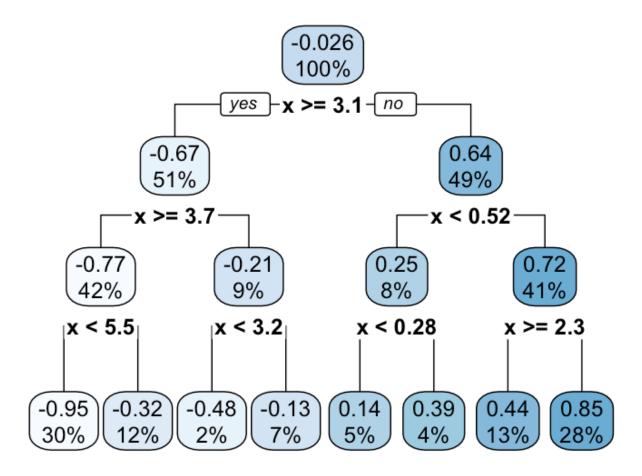
A simple CIT model from this relationship would be with a single break:



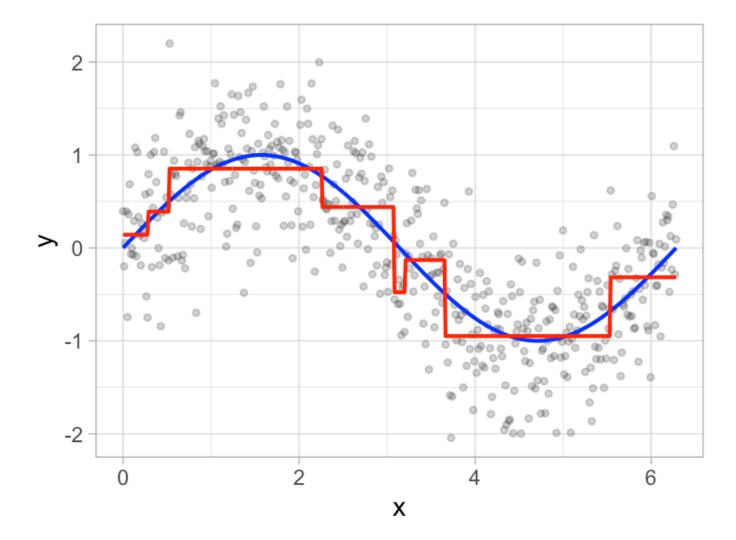
If we make a plot of $y \sim x$ and show the split above along the x axis, this is how it would look like:



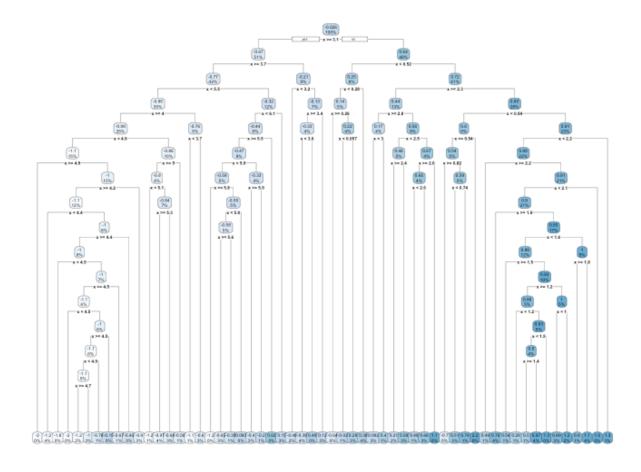
We can build a more complex tree by allowing it to be deeper:



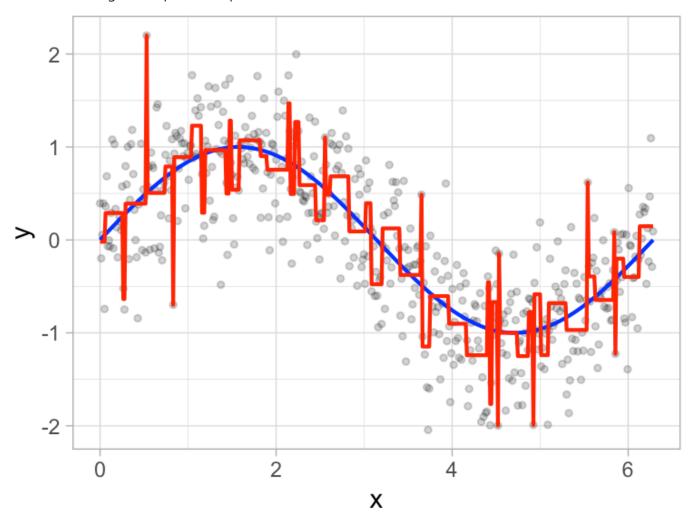
Which will translate into more breaks along the x-axis of the scatterplot:



We can allow it to be VERY complex:



With the following scatterplot breakpoints:



So, how can we control the simplicity/complexity of the tree?

Training a model by fine-tuning its hyper-parameters.

There will be 2 main hyperparameters that we will fine-tune:

- **maximum depth**: maximum (vertical) depth of the tree - **minimum criterion**: the value of (1 - p-value) that must be exceeded in order to implement a split

Pros vs. cons of CIT

Pros:

- Non-parametric
- It can model non-linear relationships
- The model created is a decision tree, very easy to interpret
- Can be used with both numerical and categorical response variables

Cons:

- Can have higher bias

- Potentially lower predictive power: any observation matching a given condition will be predicted as the mean of the terminal node.

Setup

```
#install.packages("partykit")
#install.packages("finetune")
#install.packages("bonsai")
#install.packages("tidymodels")
#install.packages("vip")

library(tidymodels)
library(tidyverse)
library(vip)
library(partykit)
library(finetune)
library(bonsai)
```

```
weather <- read_csv("../data/weather_monthsum.csv")</pre>
```

```
Rows: 698 Columns: 75

— Column specification 
Delimiter: ","
chr (1): site
dbl (74): year, strength_gtex, mean_dayl.s_Jan, mean_srad.wm2_Jan, mean_tmax...

i Use `spec()` to retrieve the full column specification for this data.
i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

weather

```
# A tibble: 698 × 75
                  strength_gtex mean_dayl.s_Jan mean_srad.wm2_Jan mean_tmax.c_Jan
    year site
   <dbl> <chr>
                          <dbl>
                                           <dbl>
                                                              <dbl>
                                                                               <dbl>
 1 1980 Altus,...
                           25.3
                                          35873.
                                                               242.
                                                                                10.2
 2 1980 Ames P...
                           27.2
                                                               215.
                                                                                 9.2
                                          35743.
 3 1980 Artesi...
                           26
                                          36359
                                                               279.
                                                                                13.4
 4 1980 Auburn...
                           24.8
                                                                                13.9
                                          36420.
                                                               240.
 5 1980 Beevil...
                           24.5
                                          37494.
                                                               277
                                                                                19.9
 6 1980 Belle ...
                                                               224.
                                                                                 9.7
                           28.1
                                          35873.
 7 1980 Bossie...
                           25.9
                                          36451.
                                                               221.
                                                                                13.2
 8 1980 Chicka...
                           25.9
                                          35760.
                                                               244
                                                                                 9.5
 9 1980 Clarkd...
                           26.1
                                          35678.
                                                               265.
                                                                                 5.8
10 1980 Colleg...
                           27.1
                                          36941.
                                                               254
                                                                                15.8
# i 688 more rows
```

i 69 more variables: mean_tmin.c_Jan <dbl>, mean_vp.pa_Jan <dbl>,

```
# sum_prcp.mm_Jan <dbl>, mean_dayl.s_Feb <dbl>, mean_srad.wm2_Feb <dbl>,
# mean_tmax.c_Feb <dbl>, mean_tmin.c_Feb <dbl>, mean_vp.pa_Feb <dbl>,
# sum_prcp.mm_Feb <dbl>, mean_dayl.s_Mar <dbl>, mean_srad.wm2_Mar <dbl>,
# mean_tmax.c_Mar <dbl>, mean_tmin.c_Mar <dbl>, mean_vp.pa_Mar <dbl>,
# sum_prcp.mm_Mar <dbl>, mean_dayl.s_Apr <dbl>, mean_srad.wm2_Apr <dbl>, ...
```

ML workflow

We're going to use the same workflow as we used for elastic net.

1. Pre-processing

Here's where we perform data split and data processing.

a. Data split

For data split, let's use 70% training / 30% testing.

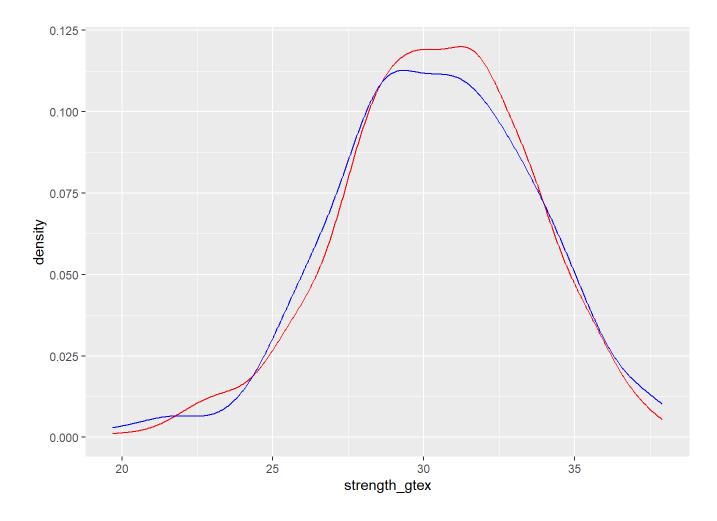
<Training/Testing/Total> <487/211/698>

```
# Setting train set
weather_train <- training(weather_split)
weather_train</pre>
```

```
# A tibble: 487 × 75
    year site
                  strength_gtex mean_dayl.s_Jan mean_srad.wm2_Jan mean_tmax.c_Jan
                                                               <dbl>
   <dbl> <chr>>
                           <dbl>
                                            <dbl>
                                                                                 <dbl>
 1 1980 Altus,...
                            25.3
                                           35873.
                                                                242.
                                                                                  10.2
                                                                                   9.2
 2 1980 Ames P...
                            27.2
                                           35743.
                                                                215.
 3 1980 Artesi...
                            26
                                           36359
                                                                 279.
                                                                                  13.4
 4 1980 Belle ...
                            28.1
                                           35873.
                                                                224.
                                                                                  9.7
 5 1980 Bossie...
                            25.9
                                           36451.
                                                                221.
                                                                                  13.2
 6 1980 Chicka...
                            25.9
                                           35760.
                                                                244
                                                                                   9.5
 7 1980 Clarkd...
                            26.1
                                                                                   5.8
                                           35678.
                                                                265.
 8 1980 Colleg...
                            27.1
                                           36941.
                                                                254
                                                                                  15.8
```

```
26.9
                                                               272.
                                                                                12.5
 9 1980 Lamesa...
                                          36390.
10 1980 Mangum...
                           26.8
                                          35808.
                                                               245.
                                                                                 9.6
# i 477 more rows
# i 69 more variables: mean_tmin.c_Jan <dbl>, mean_vp.pa_Jan <dbl>,
    sum_prcp.mm_Jan <dbl>, mean_dayl.s_Feb <dbl>, mean_srad.wm2_Feb <dbl>,
    mean_tmax.c_Feb <dbl>, mean_tmin.c_Feb <dbl>, mean_vp.pa_Feb <dbl>,
#
    sum_prcp.mm_Feb <dbl>, mean_dayl.s_Mar <dbl>, mean_srad.wm2_Mar <dbl>,
    mean_tmax.c_Mar <dbl>, mean_tmin.c_Mar <dbl>, mean_vp.pa_Mar <dbl>,
#
#
    sum_prcp.mm_Mar <dbl>, mean_dayl.s_Apr <dbl>, mean_srad.wm2_Apr <dbl>, ...
How many observations?
 # Setting test split
 weather_test <- testing(weather_split)</pre>
 weather_test
# A tibble: 211 × 75
    year site
                  strength_gtex mean_dayl.s_Jan mean_srad.wm2_Jan mean_tmax.c_Jan
   <dbl> <chr>>
                          <dbl>
                                           <dbl>
                                                              <dbl>
                                                                               <dbl>
 1 1980 Auburn...
                           24.8
                                          36420.
                                                               240.
                                                                                13.9
 2 1980 Beevil...
                           24.5
                                          37494.
                                                               277
                                                                                19.9
 3 1980 Coolid...
                           32.1
                                                                                19.8
                                          36328.
                                                               268.
 4 1980 Floren...
                           26.1
                                          36000.
                                                               228.
                                                                                12.3
 5 1980 Jackso...
                           28.5
                                          35596.
                                                               209.
                                                                                 8.7
 6 1980 Marico...
                           24.8
                                          36298.
                                                               275.
                                                                                19.6
 7 1981 Bossie...
                           27.6
                                          36451.
                                                               266.
                                                                                13.4
 8 1981 Chilli...
                                                               274.
                                                                                13.5
                           26.1
                                          35984.
   1981 Floren...
                           27.9
                                          36000.
                                                               269.
                                                                                10.5
10 1981 Halfwa...
                           26.2
                                          36000.
                                                               290.
                                                                                12.4
# i 201 more rows
# i 69 more variables: mean_tmin.c_Jan <dbl>, mean_vp.pa_Jan <dbl>,
#
    sum_prcp.mm_Jan <dbl>, mean_dayl.s_Feb <dbl>, mean_srad.wm2_Feb <dbl>,
#
    mean_tmax.c_Feb <dbl>, mean_tmin.c_Feb <dbl>, mean_vp.pa_Feb <dbl>,
    sum_prcp.mm_Feb <dbl>, mean_dayl.s_Mar <dbl>, mean_srad.wm2_Mar <dbl>,
#
#
    mean_tmax.c_Mar <dbl>, mean_tmin.c_Mar <dbl>, mean_vp.pa_Mar <dbl>,
#
    sum_prcp.mm_Mar <dbl>, mean_dayl.s_Apr <dbl>, mean_srad.wm2_Apr <dbl>, ...
How many observations?
```

Let's check the distribution of our predicted variable **strength_gtex** across training and testing:



Now, we put our **test set** aside and continue with our **train set** for training.

b. Data processing

Before training, we may need to perform some processing steps, like

- normalizing
- removing unimportant variables
- dropping NAs
- performing PCA on the go
- removing columns with single value
- others?

For that, we'll create a **recipe** of these processing steps.

This recipe will then be applied now to the **train data**, and easily applied to the **test data** when we bring it back at the end.

Creating a recipe is as easy way to port your processing steps for other data sets without needing to repeat code, and also only considering the data it is being applied to.

You can find all available recipe step options here: https://tidymodels.github.io/recipes/reference/index.html

Different model types require different processing steps.

Let's check what steps are required for an elastic net model (linear_reg). We can search for that in this link: https://www.tmwr.org/pre-proc-table

Differently from elastic net, variables do not need to be normalized in conditional inference tree, so we'll skip this step

- Recipe
пестре
- Inputs
when of vanishles by male
umber of variables by role
utcome: 1
redictor: 74
- Operations

• Variables removed: year, site, matches("Jan|Feb|Mar|Apr|Nov|Dec")

Now that we have our recipe ready, we **need to apply it** to the training data in a process called prepping:

```
weather_prep <- weather_recipe %>%
  prep()
weather_prep
```

Recipe				
 кестре				

- Inputs

Number of variables by role

outcome: 1
predictor: 74

- Training information

Training data contained 487 data points and no incomplete rows.

- Operations
- Variables removed: year, site, mean_dayl.s_Jan, ... | Trained Now, we're ready to start the model training process!

2. Training

a. Model specification

First, let's specify:

- the **type of model** we want to train
- which **engine** we want to use
- which **mode** we want to use

Elastic nets can only be run for a numerical response variable. CITs can be run with either numerical (regression) or categorical (classification) explanatory variable. Therefore, we have the need to specify the mode here.

Conditional inference tree **hyperparameters**:

- **tree_depth**: maximum depth of the tree
- mincriterion: the value of 1 p-value that must be exceeded in order to implement a split
- min_n: minimum number of data points in a node that are required for the node to be split further

Let's create a model specification that will **fine-tune** the first two for us.

A given model type can be fit with different engines (e.g., through different packages). Here, we'll use the **partykit** engine/package.

```
cit_spec
```

```
Decision Tree Model Specification (regression)
```

```
Main Arguments:
   tree_depth = tune()

Engine-Specific Arguments:
   conditional_min_criterion = tune()
```

Computational engine: partykit

Notice how the main arguments above do not have a value **yet**, because they will be tuned.

Notice how we have one hyperparameter at the level of decision tree (tree_depth) and another one at the level of the engine (min_criterion).

b. Hyper-parameter tuning

On our previous exercise, we used a fixed grid search approach. This time, let's use an iterative search approach.

For our iterative search, we need:

- Our model specification (cit_spec)
- The recipe (weather_recipe)
- Our resampling strategy (don't have yet)
- Parameter information (don't have yet)

Let's define our resampling strategy below, using a 10-fold cross validation approach:

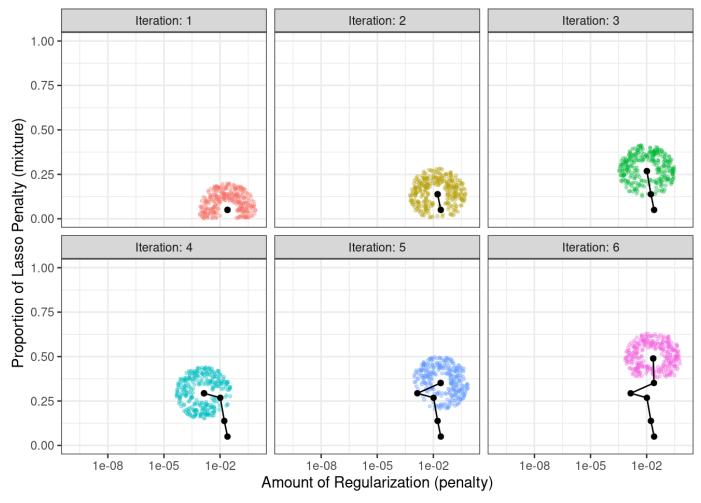
```
8 <split [439/48]> Fold08
 9 <split [439/48]> Fold09
10 <split [439/48]> Fold10
 resampling_foldcv$splits[[1]]
<Analysis/Assess/Total>
<438/49/487>
 resampling_foldcv$splits[[2]]
<Analysis/Assess/Total>
<438/49/487>
On each fold, we'll use 438 observations for training and 49 observations to assess performance.
Now, let's define our parameter information.
We need to create this object because engine-specific hyperparameters have a missing object, and it is
required to be not missing to perform simulated annealing.
 cit_param = cit_spec %>%
   extract_parameter_set_dials() %>%
   update(conditional_min_criterion = conditional_min_criterion())
 cit_param
Collection of 2 parameters for tuning
                 identifier
                                                  type
                                                          object
                 tree_depth
                                            tree_depth nparam[+]
 conditional_min_criterion conditional_min_criterion nparam[+]
 cit_param$object
[[1]]
Tree Depth (quantitative)
Range: [1, 15]
[[2]]
Value Needed for Split (quantitative)
Transformer: prob-logis [0, 1]
```

Range (transformed scale): [1.39, 15]

Now, let's perform the search below.

We will use an iterative search algorithm called **simulated annealing**.

Here's how it works:



- In the example above, mixture and penalty from an elastic net model are being tuned.
 - It finds a candidate value of hyperparameters and their associated rmse to start (iteration 1).
 - It establishes a radius around the first proposal, and randomly chooses a new set of values within that radius.
 - If this achieves better results than the previous parameters, it is accepted as the new best and the process continues. If the results are worse than the previous value the search procedure may still use this parameter to define further steps.
 - After a given number of iterations, the algorithm stops and provides a list of the best models and their hyperparameters.

In the algorithm below, we are asking for 50 iterations.

```
set.seed(76544)
cit_grid_result <- tune_sim_anneal(</pre>
```

```
object = cit_spec,
preprocessor = weather_recipe,
resamples = resampling_foldcv,
param_info = cit_param,
iter = 50
)
Optimizing rmse
```

```
Initial best: 3.00490
1 \( \text{accept suboptimal rmse=3.0049 (+/-0.133)} \)
2 ○ accept suboptimal rmse=3.0049 (+/-0.133)
3 ○ accept suboptimal rmse=3.0049 (+/-0.133)
4 ○ accept suboptimal rmse=3.0049 (+/-0.133)
5 ○ accept suboptimal rmse=3.0049 (+/-0.133)
6 ○ accept suboptimal rmse=3.0049 (+/-0.133)
7 ○ accept suboptimal rmse=3.0049 (+/-0.133)
8 X restart from best rmse=3.0049 (+/-0.133)
9 ○ accept suboptimal rmse=3.0049 (+/-0.133)
10 ○ accept suboptimal rmse=3.0049 (+/-0.133)
11 ○ accept suboptimal rmse=3.0049 (+/-0.133)
12 - discard suboptimal rmse=3.0086 (+/-0.1361)
13 ♥ new best
                       rmse=3.0034 (+/-0.1335)
14 - discard suboptimal rmse=3.024 (+/-0.1437)
15 ○ accept suboptimal rmse=3.0049 (+/-0.133)
16 ○ accept suboptimal rmse=3.0049 (+/-0.133)
17 + better suboptimal rmse=3.0034 (+/-0.1335)
18 ○ accept suboptimal rmse=3.0049 (+/-0.133)
19 ○ accept suboptimal rmse=3.0049 (+/-0.133)
20 ○ accept suboptimal rmse=3.0049 (+/-0.133)
```

```
21 X restart from best rmse=3.0034 (+/-0.1335)
```

- 22 O accept suboptimal rmse=3.0086 (+/-0.1361)
- 23 O accept suboptimal rmse=3.024 (+/-0.1437)
- 24 + better suboptimal rmse=3.0086 (+/-0.1361)
- 25 accept suboptimal rmse=3.0086 (+/-0.1361)
- 26 + better suboptimal rmse=3.0049 (+/-0.133)
- 27 accept suboptimal rmse=3.0049 (+/-0.133)
- 28 O accept suboptimal rmse=3.0086 (+/-0.1361)
- 29 **X** restart from best rmse=3.0086 (+/-0.1361)
- 30 accept suboptimal rmse=3.0034 (+/-0.1335)
- 31 accept suboptimal rmse=3.0034 (+/-0.1335)
- 32 accept suboptimal rmse=3.0034 (+/-0.1335)
- 33 accept suboptimal rmse=3.0086 (+/-0.1361)
- 34 accept suboptimal rmse=3.0086 (+/-0.1361)
- 35 accept suboptimal rmse=3.024 (+/-0.1437)
- 36 + better suboptimal rmse=3.0086 (+/-0.1361)
- 37 **X** restart from best rmse=3.024 (+/-0.1437)
- 38 accept suboptimal rmse=3.0049 (+/-0.133)
- 39 accept suboptimal rmse=3.0049 (+/-0.133)
- 40 accept suboptimal rmse=3.0049 (+/-0.133)
- 41 accept suboptimal rmse=3.0049 (+/-0.133)
- 42 accept suboptimal rmse=3.0049 (+/-0.133)
- 43 accept suboptimal rmse=3.0049 (+/-0.133)
- 44 accept suboptimal rmse=3.0049 (+/-0.133)
- 45 **X** restart from best rmse=3.0049 (+/-0.133)
- 46 discard suboptimal rmse=3.024 (+/-0.1437)

```
47   accept suboptimal rmse=3.0049 (+/-0.133)

48   accept suboptimal rmse=3.0049 (+/-0.133)

49   accept suboptimal rmse=3.0049 (+/-0.133)

50   accept suboptimal rmse=3.0049 (+/-0.133)
```

```
cit_grid_result$.metrics[[2]]
```

```
# A tibble: 2 × 6
 tree_depth conditional_min_criterion .metric .estimator .estimate .config
                                                             <dbl> <chr>
       <int>
                                <dbl> <chr>
                                              <chr>
          9
                                 1.00 rmse
                                              standard
                                                            3.42
                                                                   initial_Pre...
1
           9
2
                                 1.00 rsq
                                              standard
                                                            0.0554 initial_Pre...
```

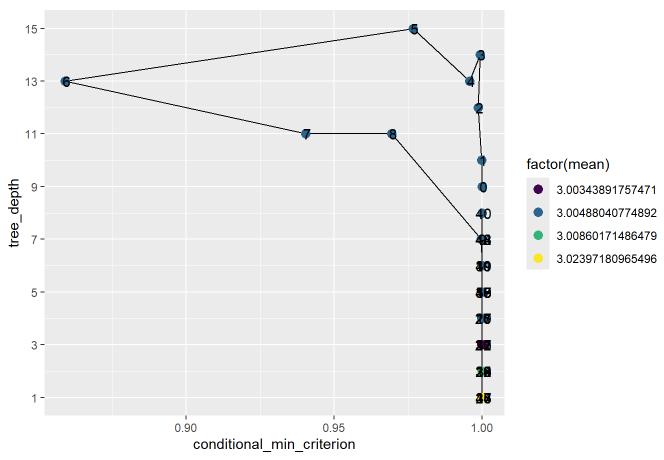
Notice how we have a column for iterations.

The first iteration uses a sensible value for the hyper-parameters, and then starts "walking" the parameter space in the direction of greatest improvement.

Let's collect a summary of metrics (across all folds, for each iteration), and plot them.

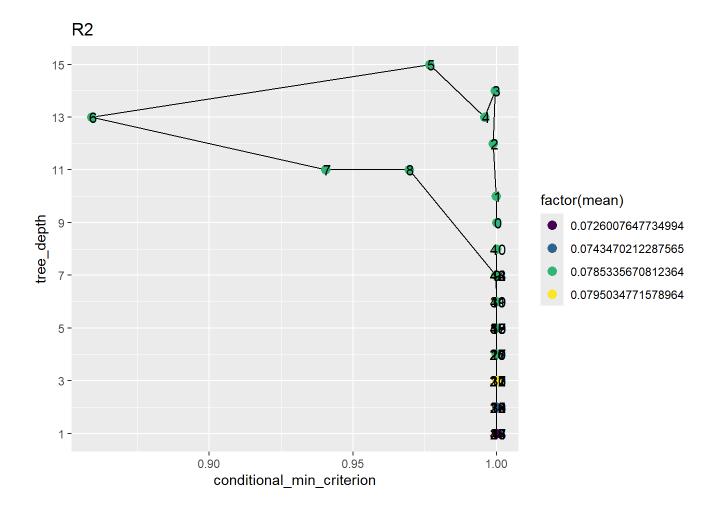
Firs, RMSE (lower is better):





What tree_depth and min criterion values created lowest RMSE?

Now, let's look into R2 (higher is better):



Previously, we selected the single best model. Now, let's select the best model within one std error of the metric, so we choose a model among the top ones that is more parsimonious.

Warning in select_by_one_std_err(., "tree_depth", metic = "rmse"): No value of `metric` was given; "rmse" will be used.

```
# Based on greatest R2
best_r2 <- cit_grid_result %>%
```

```
select_by_one_std_err("tree_depth",
                          metic = "rsq")
Warning in select_by_one_std_err(., "tree_depth", metic = "rsq"): No value of
`metric` was given; "rmse" will be used.
 best_r2
# A tibble: 1 \times 3
  tree_depth conditional_min_criterion .config
       <int>
                                  <dbl> <chr>>
                                   1.00 initial_Preprocessor1_Model1
Based on RMSE, we would choose
- tree_depth = 9
conditional_min_criterion = 0.999954
Based on R2, we would choose
- tree_depth = 9 - conditional_min_criterion = 0.999954
Let's use the hyperparameter values that optimized R2 to fit our final model.
 final_spec <- decision_tree(tree_depth = best_r2$tree_depth) %>%
   # Specify the engine
   set_engine("partykit",
              conditional_min_criterion = best_r2$conditional_min_criterion) %>%
   # Specifying mode
   set_mode("regression")
 final_spec
Decision Tree Model Specification (regression)
Main Arguments:
  tree_depth = best_r2$tree_depth
```

```
Engine-Specific Arguments:
  conditional_min_criterion = best_r2$conditional_min_criterion
```

3. Validation

Computational engine: partykit

Now that we determined our best model, let's do our last fit.

This means 2 things:

- Traninig the optimum hyperparameter values on the **entire training set**

- Using it to **predict** on the **test set**

These 2 steps can be completed in one function, as below:

```
# A tibble: 211 × 5
   .pred id
                           .row strength_gtex .config
  <dbl> <chr>
                                        <dbl> <chr>
                         <int>
 1 30.2 train/test split
                                        24.8 Preprocessor1 Model1
 2 30.2 train/test split
                              5
                                        24.5 Preprocessor1_Model1
 3 29.6 train/test split
                                        32.1 Preprocessor1_Model1
                            11
 4 30.2 train/test split
                            13
                                        26.1 Preprocessor1 Model1
 5 30.2 train/test split
                                        28.5 Preprocessor1_Model1
                            14
 6 29.6 train/test split
                                        24.8 Preprocessor1_Model1
                            19
 7 30.2 train/test split
                            32
                                        27.6 Preprocessor1 Model1
8 29.6 train/test split
                            33
                                        26.1 Preprocessor1_Model1
9 29.6 train/test split
                                        27.9 Preprocessor1 Model1
                            37
10 29.6 train/test split
                                         26.2 Preprocessor1_Model1
# i 201 more rows
```

Metrics on the **test set**:

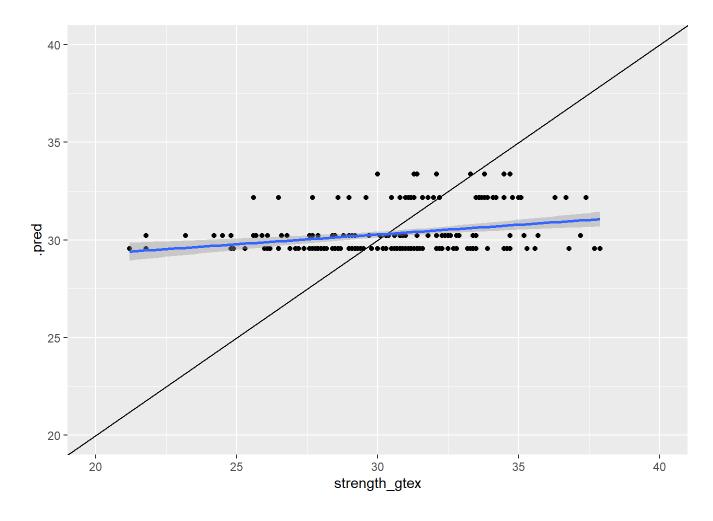
```
final_fit %>%
  collect_metrics()
```

Metrics on **train set** (for curiosity and compare to test set):

How does metrics on test compare to metrics on train?

Predicted vs. observed plot:

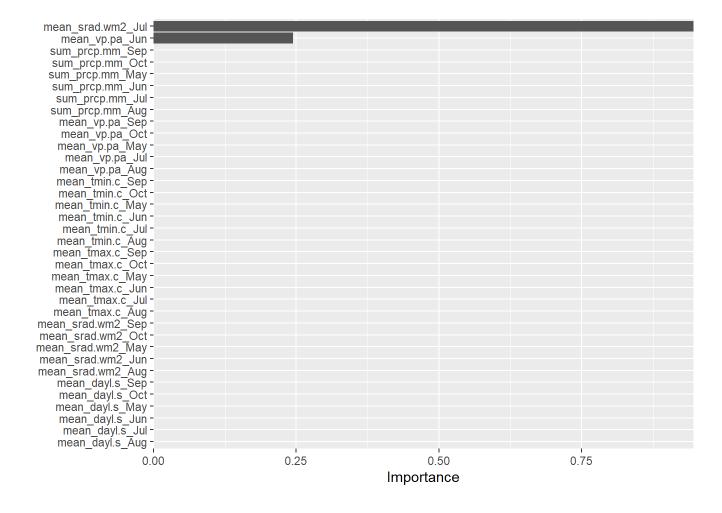
```
`geom_smooth()` using formula = 'y ~ x'
Warning: Removed 1 row containing non-finite outside the scale range
(`stat_smooth()`).
Warning: Removed 1 row containing missing values or values outside the scale range
(`geom_point()`).
```



Why the 4 horizontal lines?

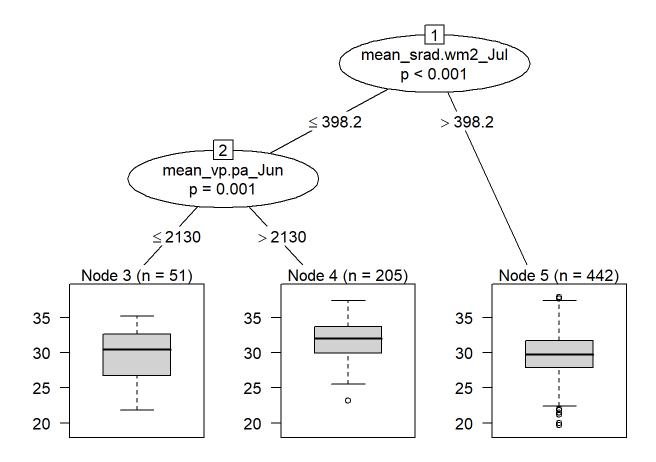
How can we get more horizontal lines in this type of algorithm?

Variable importance:



Tree:

```
final_spec %>%
fit(strength_gtex ~ .,
    data = bake(weather_prep, weather)
    ) %>%
.$fit %>%
plot()
```



Therefore, solar radiation in July and vapor pressure in June were the most important variables affecting cotton fiber strength.

Greater fiber strength was observed when solar radiation in July was < 398 W/m2 and vapor pressure in June was > 2130 Pa (terminal node 4).

For a nicer tree visualization, check out the package **ggparty**:

- https://github.com/martin-borkovec/ggparty
- https://jtr13.github.io/cc19/introduction-to-package-ggparty.html

Summary

In this exercise, we covered: - Conditional inference tree algorithm

- Set up a ML workflow to train an cit model
- Used recipes to process data Used rsamples to split data
- Used **iterative search** to find the best values for mas_depth and min_criterion
- Used 10-fold cross validation as the resampling method
- Used both R2 and RMSE as the metrics to select best model
- Once final model was determined, used it to predict **test set**
- Evaluated it with predicted vs. observed plot, R2 and RMSE metrics, variable importance, and tree plot