



model initialization

$$b_{n+1} = b_n + \alpha(d_n - y_n)$$

$$w_{n+1} = w_n + \alpha x_n(d_n - y_n)$$

update Rules

| $x_1$ | $x_2$ | NAND |
|-------|-------|------|
| 0     | 0     | 1    |
| 0     | 1     | 1    |
| 1     | 0     | 1    |
| 1     | 1     | 0    |

Dataset

① input = [0, 0]  $d = 1$

$$y = 0 \times 0.1 + 0 \times 0.2 + 1 = 1$$

$$b_{new} = 1 + 0.1(1 - 1) = \boxed{1}$$

$$w_{1new} = 0.1 + 0.1(0)(1 - 1) = \boxed{0.1}$$

$$w_{2new} = 0.2 + 0.1(0)(1 - 1) = \boxed{0.2}$$

② input = [0, 1]  $d = 1$

$$y = 0 \times 0.1 + 1 \times 0.2 + 1 = 1.2$$

$$b_{new} = 1 + 0.1(1 - 1.2) = \boxed{0.98}$$

$$w_{1new} = 0.1 + 0.1(0)(1 - 1.2) = \boxed{0.1}$$

$$w_{2new} = 0.2 + 0.1(1)(1 - 1.2) = \boxed{0.18}$$

③ input = [1, 0]  $d = 1$

$$y = 0.1 \times 1 + 0.18 \times 0 + 0.98 = 1.08$$

$$b_{new} = 0.98 + 0.1(1 - 1.08) = \boxed{0.972}$$

$$w_{1new} = 0.1 + 0.1(1)(1 - 1.08) = \boxed{0.092}$$

$$w_{2new} = 0.18 + 0.1(0)(1 - 1.08) = \boxed{0.18}$$

④ input = [1, 1]     d = 0

$$y = 0.092 + 1 + 0.18 + 1 + 0.972 = 1.244$$

$$b_{\text{new}} = 0.972 + 0.1(0 - 1.244) = 0.8476$$

$$W_{1\text{new}} = 0.092 + 0.1(1)(0 - 1.244) = 0.092 - 0.0324$$

$$W_{2\text{new}} = 0.18 + 0.1(1)(0 - 1.244) = 0.0556$$