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Mohammed Abu-Hadhoud

MSA, PMOC, PMP®, PMP®, PMP-ITIL®, CS, ITIL®, MCPD, MCD



لا تنسى الاشتراك في قناتنا على اليوتيوب ومشاركة القناة مع اصدقائك
لتعم الفائدة للجميع وانقاذ الاف الناس من التشتت جزاكم الله خيرا

لا تنسوننا من دعائكم وادعو لوالدي بالرحمة

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مهم جداً

هذا الملف للمراجعة السريعة واخذ الملاحظات عليه فقط ،لانه يحتوي على اقل من 20٪ مما يتم شرحه في الفيديوهات الاستعجال والاعتماد عليه فقط سوف يجعلك تخسر كميه معلومات وخبرات كثيره

يجب عليك مشاهدة فيديو الدرس كاملا

لاتنسى عمل لايك ومشاركة القناة لدعم الفائدة للجميع
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Algorithms & Problem Solving Level 6

Introduction to Rotations

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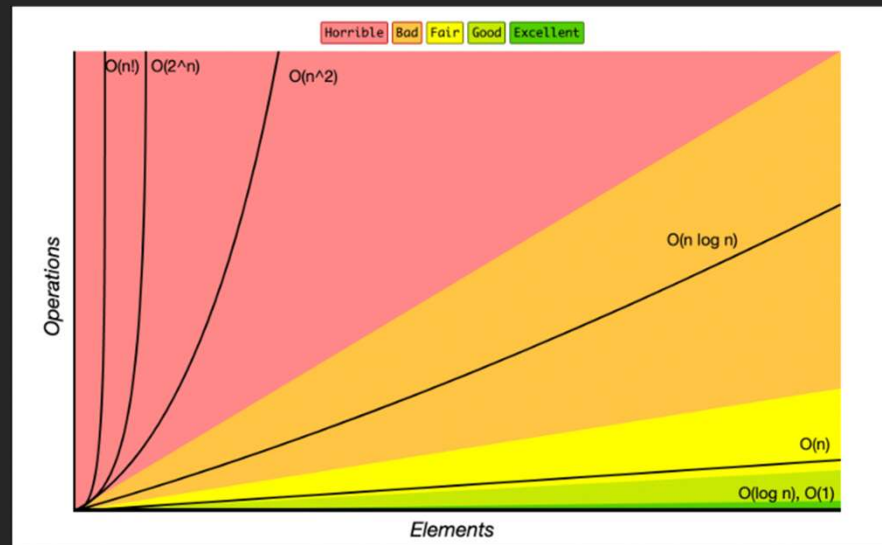
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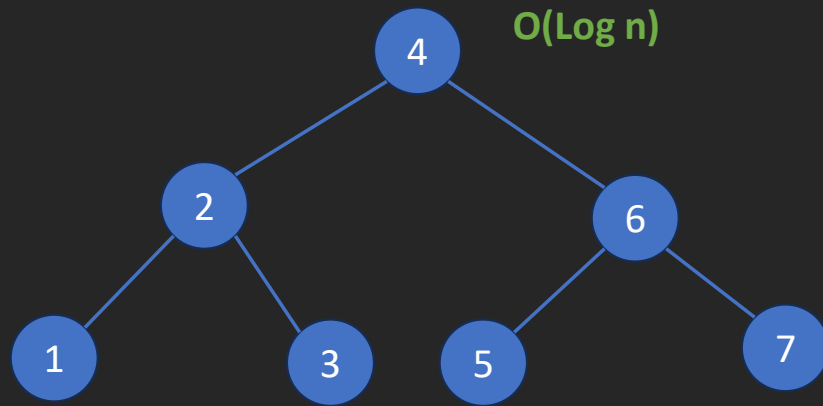
BST Search.

- Best/Average Case is $O(\log n)$
- Worst Case $O(n)$



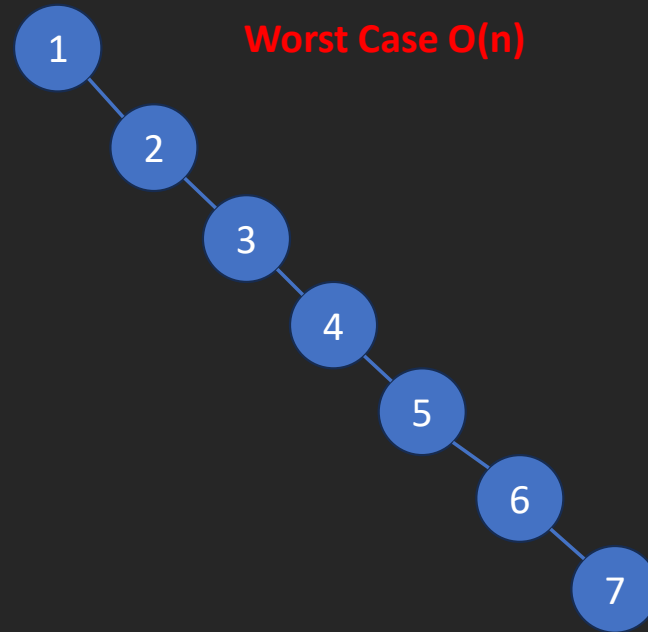
Balanced vs Imbalanced BST

Suppose that we entered data in BST in the following order:
4, 2, 6, 1, 3, 5, 7



Balanced

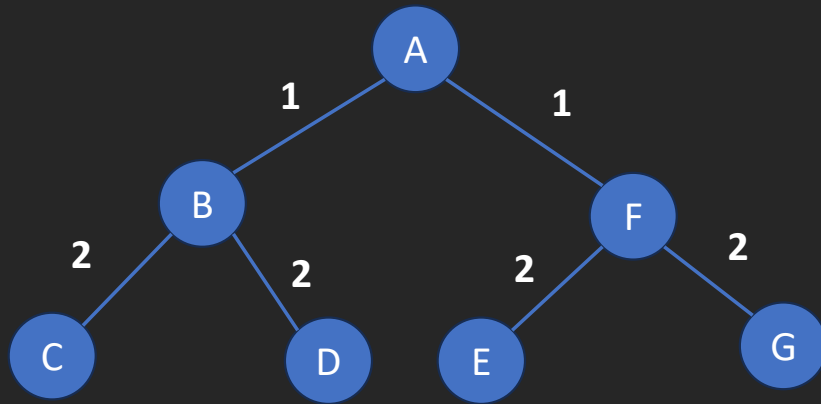
Suppose that we entered data in BST in the following order:
1, 2, 3, 4, 5, 6, 7



Unbalanced

Balanced Or Imbalanced?

$$BF = 2 - 2 = 0$$



Balanced

Rule:

Heights of the two child subtrees of any node differ by no more than one.

$DF = \text{Hight}(\text{Left Subtree}) - \text{Hight}(\text{Right Subtree})$

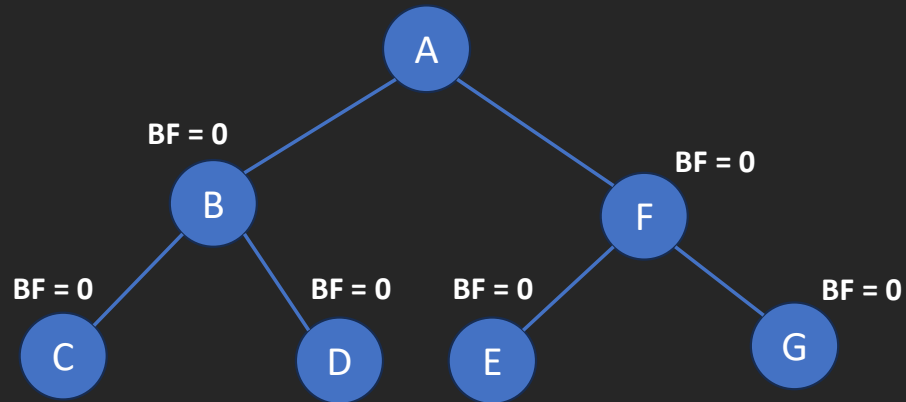
Hight = the number of edges for the longest path from the node to the last leaf

Balance Factor (BF) = DF.

If $ABS(BF) > 1$ then it is not balanced.

BF for each Node

BF = 0



Balanced

Rule:

Heights of the two child subtrees of any node differ by no more than one.

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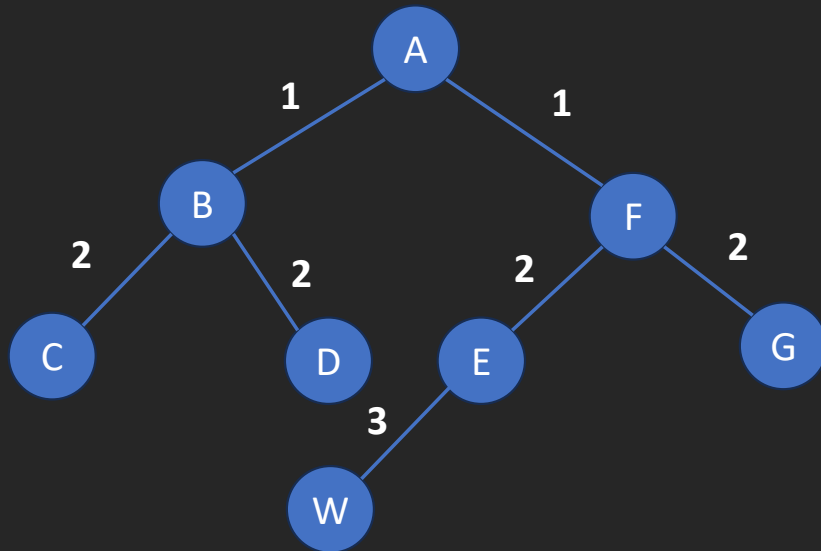
Hight = the number of edges for the longest path from the node to the last leaf

Balance Factor (BF) = DF.

If $ABS(BF) > 1$ then it is not balanced.

Balanced Or Imbalanced?

$$BF = 2 - 3 = -1$$



Balanced

Rule:

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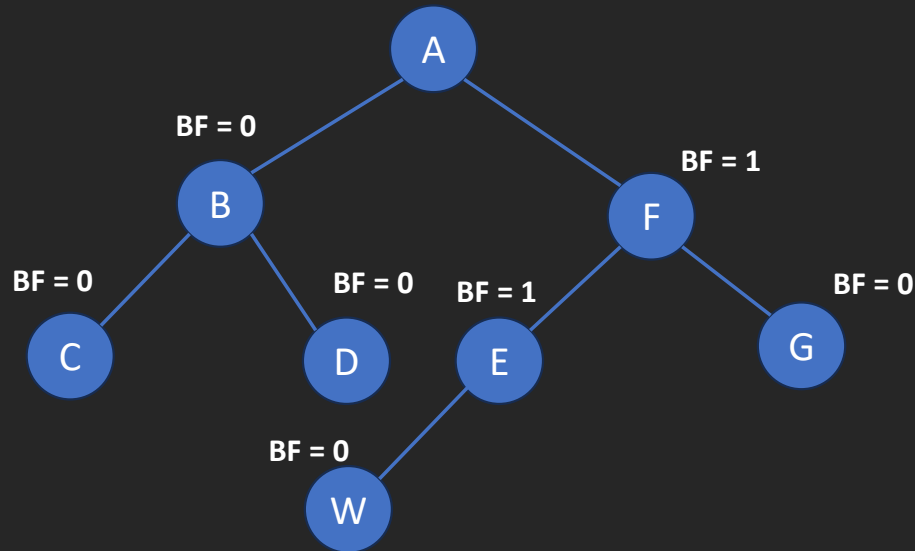
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Balanced

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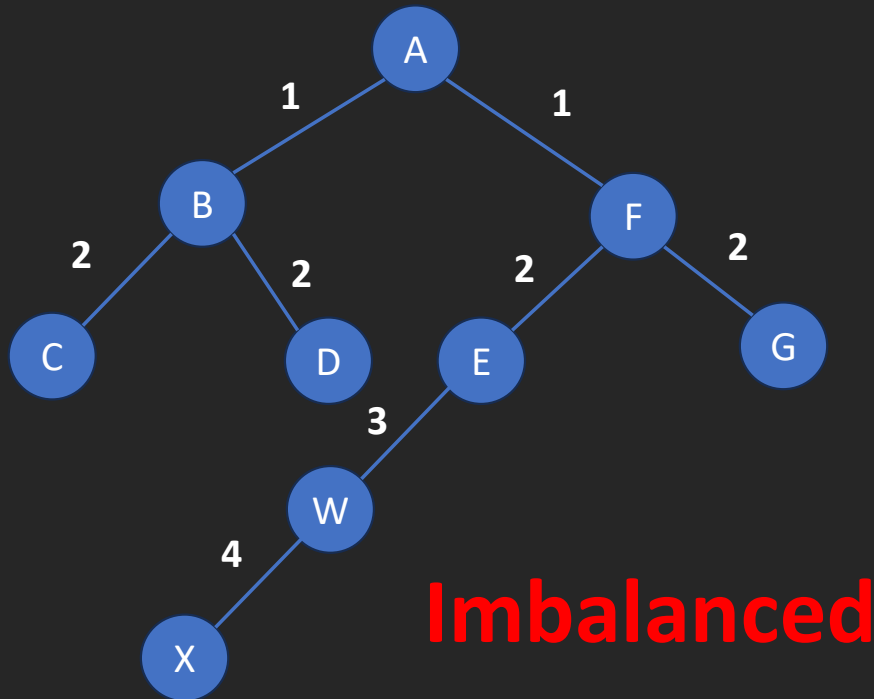
Hight = the number of edges for the longest path from the node to the last leaf

Balance Factor (BF) = DF.

If $ABS(BF) > 1$ then it is not balanced.

Balanced Or Imbalanced?

$$BF = 2 - 4 = -2$$



Rule:

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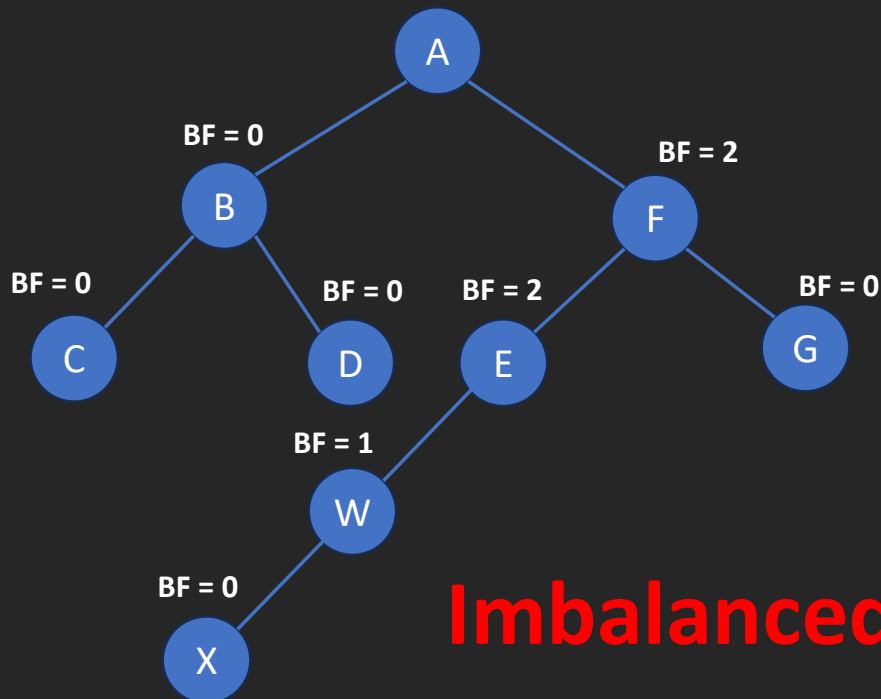
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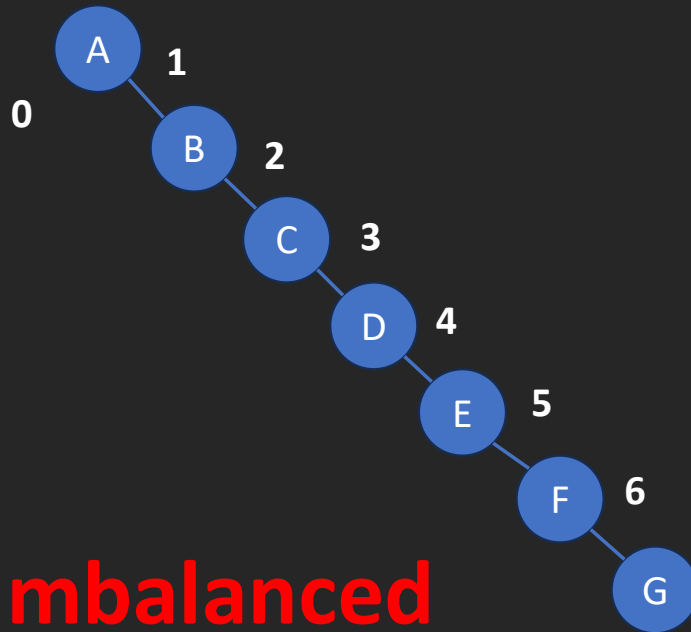
Hight = the number of edges for the longest path from the node to the last leaf

Balance Factor (BF) = DF.

If $ABS(BF) > 1$ then it is not balanced.

Balanced Or Imbalanced?

$$BF = 0 - 6 = -6$$



Rule:

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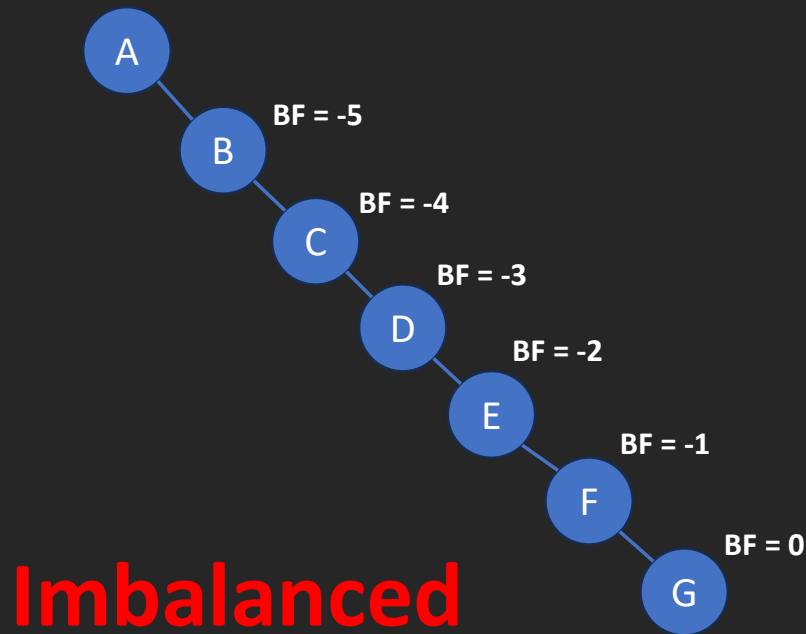
Hight = the number of edges for the longest path from the node to the last leaf

Balance Factor (BF) = DF.

If $\text{ABS}(\text{BF}) > 1$ then it is not balanced.

BF for each node

$$BF = 0 - 6 = -6$$



Rule:

Heights of the two child subtrees of any node differ by no more than one.

$$DF = \text{Hight}(\text{Left Subtree}) - \text{Hight}(\text{Right Subtree})$$

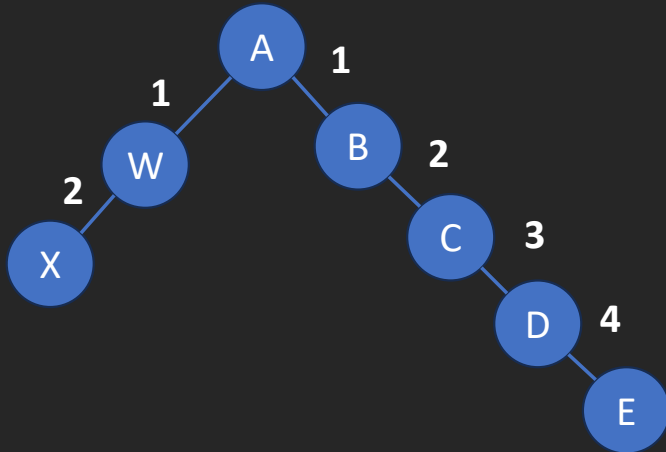
Hight = the number of edges for the longest path from the node to the last leaf

Balance Factor (BF) = DF.

If $\text{ABS}(\text{BF}) > 1$ then it is not balanced.

Balanced Or Imbalanced?

$$BF = 2 - 4 = -2$$



Imbalanced

Rule:

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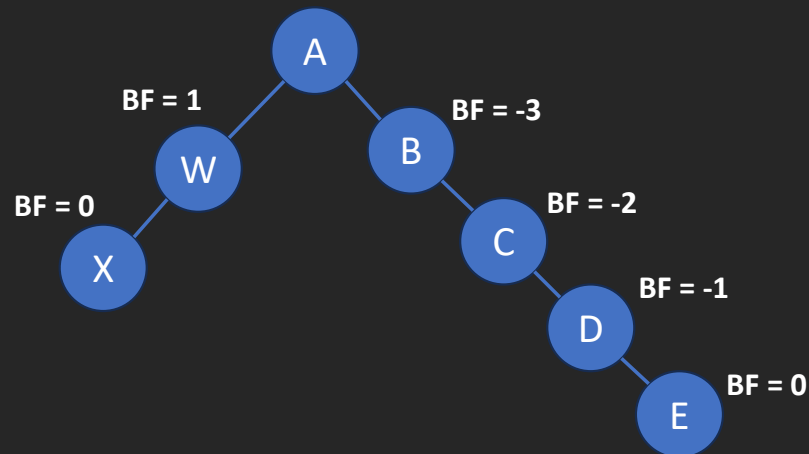
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Balance Factor (BF) = DF.

If $ABS(BF) > 1$ then it is not balanced.

Balanced Or Imbalanced?

$$BF = 2 - 4 = -2$$



Imbalanced

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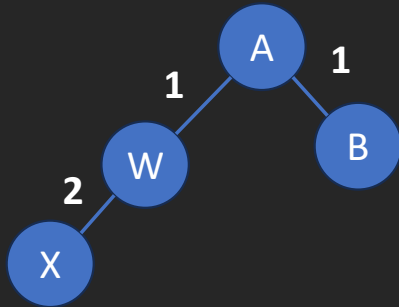
Hight = the number of edges for the longest path from the node to the last leaf

Balance Factor (BF) = DF.

If $ABS(BF) > 1$ then it is not balanced.

Balanced Or Imbalanced?

$$BF = 2 - 1 = 1$$



Balanced

Rule:

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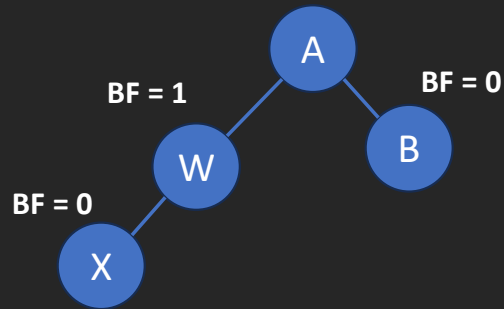
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BF for each node

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Hight = the number of edges for the longest path from the node to the last leaf

Balance Factor (BF) = DF.

If $\text{ABS}(\text{BF}) > 1$ then it is not balanced.

Node Is Balanced If...

- Should be -1 , 0 , or $+1$ for each node $\rightarrow \text{Abs}(\text{BF}) \leq 1$.
- If $\text{Abs}(\text{BF}) > 1$ then it is Imbalanced.
- If at any time they differ by more than one, rebalancing is done to restore this property.

What is AVL?

- AVL trees, named after their inventors Adelson-Velsky and Landis, are self-balancing binary search trees.
- In an AVL tree, the heights of the two child subtrees of any node differ by no more than one.
- If at any time they differ by more than one, rebalancing is done to restore this property.

In order to rebalance a node
you need to do rotations

What are Rotations?

- To maintain balance after insertions and deletions, AVL trees use rotations.
- Rotations are pivotal tree manipulations that shift nodes and their subtrees around to move higher nodes lower and lower nodes higher, thus restoring the required balance of the tree.
- Concept of rotations as operations that reorder the nodes of the tree to maintain or restore balance.

Types of Rotations:

- There are four types of basic rotations:
 - RR – Right Rotation (Single Right Rotation)
 - LL – Left Rotation (Single Left Rotation)
 - LR – Left-Right (Double Rotations)
 - RL – Right-Left Rotations (Double Rotations)



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Thank You

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