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# Differential Equations

Equation involving derivative (derivatives) of the dependent variable(y) with respect to independent variable (variables)(x) is called a differential equation. In this chapter we study the method formation of a Differential Equation and solving of a Differential Equation.

A differential equation involving derivatives of the dependent variable with respect to only one independent variable is called an **ordinary differential equation**

eg:

$$2\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^3 = 0$$

## Order of a differential equation

Order of a differential equation is defined as the order of the highest order derivative of the dependent variable with respect to the independent variable involved in the given differential equation.

eg:

$$\frac{d^2y}{dx^2} + y = 0 \text{ (order 2)}$$
$$\frac{dy}{dx} = e^x \text{ (order 1)}$$

## Degree of a differential equation

Degree of a DE is defined as the exponent of highest differential coefficient appearing in the equation provided the equation is made into polynomial form in all differential coefficient.

## Homogenous DE

A function  $F(x, y)$  is said to be **homogeneous function** of degree  $n$  if  $F(\lambda x, \lambda y) = \lambda^n F(x, y)$  for any nonzero constant  $\lambda$ . Then the function is of the form  $\frac{dy}{dx} = g\left(\frac{y}{x}\right)$

To solve put  $y = vx$  then

$$\frac{dy}{dx} = v + x \frac{dv}{dx}$$

. Then we can solve the DE in the variable separable form easily

## First order Linear DE

DE of the form

$$\frac{dy}{dx} + Py = Q$$

where P and Q are Functions of x only

To solve

- Find I.F =  $e^{\int p dx}$
- Write solution as

$$y(I.F) = \int (Q \times I.F) dx + C$$