

A-3 MATHS

01.

Q01 The Quadratic polynomial whose sum and product of zeroes are 4 and 5 respectively

- a) $P(x) = x^2 - 4x - 5$ c) $P(x) = x^2 - 5x + 4$
b) $P(x) = x^2 + 4x - 5$ d) $P(x) = x^2 - 4x + 5$

02 If $\sin A = \frac{1}{\sqrt{2}}$, the magnitude of A is

- a) 90° b) 60° c) 80° d) 45°

03 If the roots of the Q.E. $x^2 + 6x + k = 0$ are equal then the value of "k" is

- a) 9 b) -9 c) 8 d) 15

04 The value of $\cos 48^\circ + \sin 42^\circ$ is

- a) 1 b) $\frac{1}{4}$ c) $\frac{1}{2}$ d) 1

05 The standard form of $2x^2 = x - 7$ is

- a) $2x^2 - x = -7$ b) $2x^2 = x - 7 = 0$ c) $2x^2 - x + 7 = 0$ d) $2x^2 + 7 + 7 = 0$

Q01

01 write the standard form of a Quadratic equation

$\rightarrow ax^2 + bx + c = 0$

02 If $\cos \theta = \frac{24}{25}$ then write the value of $\sec \theta$

$\rightarrow \sec \theta = \frac{1}{\cos \theta} = \frac{1}{\frac{24}{25}} = \frac{25}{24}$

03 write the degree of the polynomial $P(x) = x^2 + 2x^3 + 5x^4 + 6$

→ 4

04 Find the roots of the quadratic equation $x^2 + 7x + 12$

→

$$x^2 + 7x + 12 = 0$$

$$(x+3)(x+4) = 0$$

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05 $\sin(90^\circ)$ is equal to

a) $\cos 0$

b) $\tan 0$

c) $\sec 0$

d) $\cot 0$

06 If $13 \sin \theta = 12$, then (find) the value of $\cos \theta$ is

a) $\frac{12}{5}$

b) $\frac{13}{5}$

c) $\frac{12}{13}$

d) $\frac{13}{12}$

07 value of $\cot 90^\circ$ is

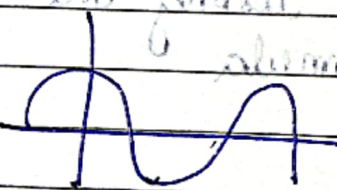
a) $\frac{1}{\sqrt{2}}$

b) 1

c) $\sqrt{3}$

d) 0

08 In the given graph the number of zeroes of the polynomial $y = P(x)$ is



→ The number of zeroes is 4 because as the graph intersects the axis at four points.

Q2

Q.1)

Find the value of the discriminant of the equation $4x^2 - 12x + 9 = 0$ and Hence write the nature of the roots

$$\rightarrow 4x^2 - 12x + 9 = 0$$

$$ax^2 + bx + c = 0$$

$$a = 4, b = -12, c = 9$$

$$\text{Discriminant} = b^2 - 4ac$$

$$\Delta = (-12)^2 - 4(4)(9)$$

~~$$\Delta = 144 - 16(9)$$~~

$$\Delta = 144 - 16(9)$$

$$\Delta = 144 - 144$$

$$\Delta = 0$$

∴ The nature of the roots is real and equal.

$$= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-12) \pm \sqrt{0}}{2(4)}$$

$$= \frac{12 \pm \sqrt{0}}{8}$$

$$= \frac{3 \pm \sqrt{0}}{2}$$

$$\left| = \frac{3 + \sqrt{0}}{2} \right| \quad \text{or} \quad \left| = \frac{3 - \sqrt{0}}{2} \right|$$

Q2 Find the roots of the Quadratic equation $x^2 + 4x + 5 = 0$ using the Quadratic formula

$$\rightarrow x^2 + 4x + 5 = 0$$

$$ax^2 + bx + c = 0$$

$$a = 1, b = 4, c = 5$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-4 \pm \sqrt{(4)^2 - (4)(1)(5)}}{2(1)}$$

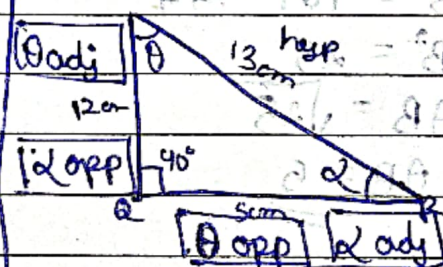
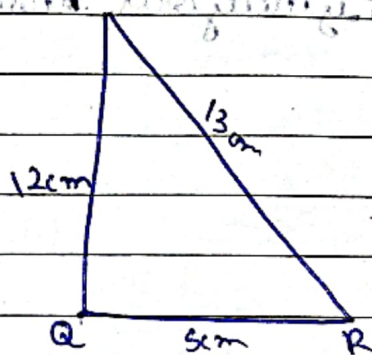
$$x = \frac{-4 \pm \sqrt{16 - 20}}{2}$$

$$x = \frac{-4 \pm \sqrt{-4}}{2}$$

$$x = -2 + \sqrt{-4}$$

$$\text{or } x = -2 - \sqrt{-4}$$

03 In the figure given below find the value of $\sin \theta$ & $\cos \theta$.



→ We know that,

$$\sin \theta = \frac{\text{Opp}}{\text{hyp}}$$

$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\sin \theta = \frac{QR}{PR}$$

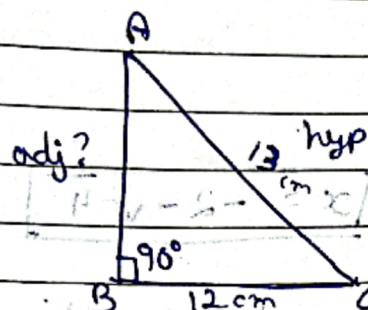
$$\cos \theta = \frac{QR}{PR}$$

$$\therefore \sin \theta = \frac{5}{13} \quad \cos \theta = \frac{5}{13}$$

\therefore The values of $\sin \theta$ & $\cos \theta$ are same, $\frac{5}{13}$ & $\frac{5}{13}$.

Q4 If $\sin \theta = \frac{12}{13}$, find the values of $\cos \theta$ & $\tan \theta$

→ We know that $\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{12}{13}$



In this $\triangle ABC$, $\angle B = 90^\circ$ to solve

$AC^2 = AB^2 + BC^2$ → (Pythagoras theorem)

$$13^2 = AB^2 + 12^2$$

$$169 = AB^2 + 144$$

$$AB^2 = 169 - 144$$

$$AB^2 = 25$$

$$AB = \sqrt{25}$$

$$AB = 5$$

Now, we know that $\cos \theta = \frac{\text{adj}}{\text{hyp}}$ $\tan \theta = \frac{\text{opp}}{\text{adj}}$

$$\cos \theta = \frac{5}{13} \quad \tan \theta = \frac{12}{5}$$

Q30, find the quotient and the remainder when $P(x) = x^3 - 3x^2 + 5x - 3$ is divided by $g(x) = x^2 - 2$

→ $P(x) = x^3 - 3x^2 + 5x - 3$ and $g(x) = x^2 - 2$

$$\begin{array}{r|l}
 x-3 & x^2 - 3x^2 + 5x - 3 \\
 & \underline{-x^2 + 0x^2 - 2x} \downarrow \\
 & + -3x^2 + 7x - 3 \\
 & \underline{-3x^2 + 0x + 6} \\
 & 7x - 9 - 20 = (1-20)20 \\
 & \underline{-(1-20)(1-20)}
 \end{array}$$

\therefore quotient = $\boxed{x-3}$: Remainder = $\boxed{7x-9}$

02 find two numbers whose sum is 27 and product is 182

let those numbers whose sum = 27

be 1st number be "x" 2nd number be (27-x)

Product of $x(27-x) = 182$

$x(27-x) = 182$

$27x - x^2 = 182$

$x^2 - 27x - 182 = 0$

$x^2 - 13x - 14x - 182 = 0$

$x(x-13) - 14(x-13)$

$\therefore (x-13)(x-14)$

$x-13=0$

$\boxed{x=13}$

@

$\boxed{x=-13}$

$x-14=0$

$\boxed{x=14}$

@

$\boxed{x=-14}$

\therefore The two numbers whose sum is 27 and product is -182 are 13, 14 @ 14, 13

03 find the zeroes of the Quadratic polynomial and verify the relation between the zeroes & coefficient

(Questions Nahi Hain isliye sirf Method Dekhliye)

$$4s^2 - 4s + 1$$

$$\rightarrow 4s^2 - 4s + 1$$

$$4s^2 - 2s - 2s + 1$$

$$(2s-1)(2s-1)$$

$$2s(2s-1) - 1(2s-1)$$

$$(2s-1)(2s-1)$$

$$a = 4 \quad b = -4 \quad c = 1$$

$$P = 2s(2s-1) - 1(2s-1) = 0 \quad 2s-1=0 \text{ dividing}$$

$$s = \frac{1}{2}$$

$$s = \frac{1}{2}$$

both are same value

same value

LHS = RHS

The zeroes of the quadratic polynomial are $s = \frac{1}{2}$ and $s = \frac{1}{2}$

$$s = \frac{1}{2}$$

$$\text{Sum of zeroes} = -\frac{b}{a} = \frac{1}{2} + \frac{1}{2} = 1$$

$$\text{Product of zeroes} = \frac{c}{a} = \frac{1}{4}$$

$$\text{Coefficient of } s^2 = 4 \quad \text{Coefficient of } s = -4 \quad \text{Constant term} = 1$$

$$\text{Constant term} = \frac{c}{a} = \frac{1}{4}$$

if we divide both sides by 4

$$s^2 - s + \frac{1}{4} = 0$$

or

$$\frac{1}{4} = \frac{1}{4}$$

$$\frac{1}{4} = \frac{1}{4}$$

LHS = RHS

LHS = RHS

both sides are same

both sides are same

$$03 \quad (\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2 \\ = 7 + \tan A + \cos^2 A$$

$$\textcircled{m} \quad \sqrt{\frac{1 + \sin A}{1 - \sin A}} = \sec A + \tan A$$

$$\rightarrow \text{LHS} = \sqrt{\frac{1 + \sin A}{1 - \sin A}}$$

$$= \sqrt{\frac{1 + \sin A}{1 - \sin A}} \times \frac{1 + \sin A}{1 + \sin A}$$

$$= \sqrt{\frac{(1 + \sin A)^2}{1 - \sin^2 A}}$$

$$= \sqrt{\frac{(1 + \sin A)^2}{\cos^2 A}}$$

$$= \frac{\sqrt{(1 + \sin A)^2}}{\sqrt{\cos^2 A}}$$

$$= \frac{1 + \sin A}{\cos A}$$

$$= \frac{1}{\cos A} + \frac{\sin A}{\cos A}$$

$$= \underline{\sec A} + \underline{\tan A}$$

$$\underline{\text{LHS}} = \underline{\text{RHS}}$$

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