

Date: / /

Subject: Digital Logic

## K-map

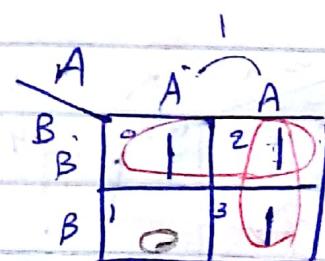
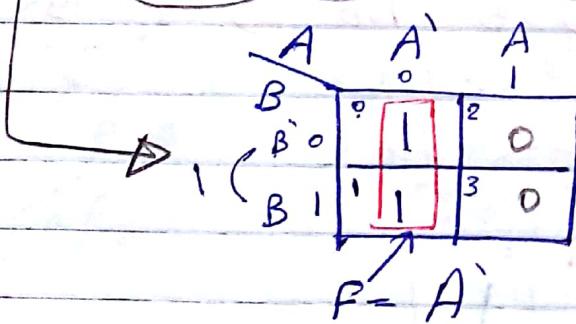
2 Variable  $\rightarrow 2^2 \rightarrow 4$  Prob.

### Truth table

A	B	f
0	0	1
1	0	1
0	1	0
1	1	0

$$\begin{aligned}
 f &= \sum m(0, 1) \Rightarrow f = \overline{A}B + A\overline{B} \\
 &= A'(\overline{B} + B) \\
 &= A'
 \end{aligned}$$

K-map For 2 Var.  $\rightarrow 4$  Prob.



$$\begin{aligned}
 F &= B' + A
 \end{aligned}$$



$$\begin{aligned}
 F &= A'B' + AB
 \end{aligned}$$

$$\begin{aligned}
 F &= B' + AB \\
 &= B' + A
 \end{aligned}$$



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 $\frac{A \oplus B}{W \oplus Z}$ 

16

 $\begin{matrix} X \\ 8 \\ 4 \\ 2 \end{matrix}$ 

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3 variable  $\rightarrow 2^3 \rightarrow 8$  Prob.  $\rightarrow o = 7$

 $A, B, C$  $F = \{m(0, 1, 4, 5, 6, 7)\}$ 

	$A$	$B$	$A$	$B'$
$C$	$AB$	$\bar{A}\bar{B}$	$\bar{A}B$	$AB$
$\bar{C}$	1	2	6	4
$C$	1	3	7	5

$$F = A + B'$$

	$A$	$B$	$\bar{A}\bar{B}$	$\bar{A}B$	$AB$	$AB'$
$C$	$AB$	$\bar{A}\bar{B}$	$\bar{A}B$	$AB$	$AB'$	
$\bar{C}$	1	2	6	1	4	
$C$	1	3	7	1	5	

$$F = \bar{A}\bar{B}\bar{C} + BC + AB$$

\* 4 variables  $\rightarrow 2^4 \rightarrow 16$  Prob.  $\rightarrow o = 15$

	$w$	$x$	$y$	$z$	$wx$	$w\bar{x}$	$\bar{w}x$	$w\bar{x}$	$\bar{w}\bar{x}$
$\bar{y}$	0	1	0	1	0	1	0	1	0
$y$	1	0	1	0	1	0	1	0	1
$\bar{z}$	0	1	1	0	0	1	1	0	1
$z$	1	0	0	1	1	0	0	1	0
$\bar{w}$	1	0	1	0	0	1	0	1	0
$w$	0	1	0	1	1	0	1	0	1

$$F = \bar{x}\bar{z} + \bar{x}z + w\bar{x}/wz \leftarrow SOP$$

$$F_1 = \bar{x}\bar{z} + xz + w\bar{x}$$

$$F_2 = \bar{x}\bar{z} + xz + wz$$

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(V)  $\rightarrow$  لذع

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Ex.: Simplify:  $F(a, b, c, d) = \sum m(0, 3, 7, 11, 12, 13, 15)$ 

to the minimum S.O.P &amp; P.O.S:-

$ab$	$cd$	$a'b'$	$ab'$	$ab$	$ab'$	
$a'b'c'd'$	$c'd'$	1	0	1	0	$abc$
$c$	$c'd$	1	0	1	0	
$cd$	3	1	1	1	1	$cd$
$cd'$	2	0	0	0	0	

$$\Rightarrow F_1 = cd + ab\bar{c} + a'b'cd'$$

S.O.P:  $\rightarrow$ \* in P.O.S

$$F = cd' + a'b\bar{c} + b'\bar{c}d + ab\bar{c}\bar{d}/ab\bar{d}'$$

$$\rightarrow (F) = (\bar{c} + d)(a + b + c)(b + c + d')(a' + b + c)/(a' + b + d)$$

$$\rightarrow F_2 = (\bar{c} + d)(\bar{a} + b + c)(b + c + d')(a' + b + c)$$

$$\rightarrow F_3 = (\bar{c} + d)(a + b + c)(b + c + d')(a' + b + d)$$



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Ex: Simplify:  $f(A, B, C, D) = \prod (1, 3, 5, 7, 13, 15)$

To the minimum SOP & the minimum POS.

of Var.  $\rightarrow A, B, C, D$

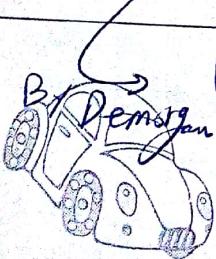
	A	B	A'	B'
D	AB	AB	AB	AB
CD	1	4	12	8
C	CD	5	13	9
D	CD	0	0	1
CD	0	0	0	1
C	2	6	14	10
CD	1	1	1	1

\* The minimum SOP:-

$$\hookrightarrow f = D' + AB' = (D' + AB)(D' + B')$$

\* The minimum POS:-

$$\hookrightarrow f' = A'D + BD$$



$$(f')' = (A'D + BD)'$$

$$f = (A + D')(B' + D).$$

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Ex:

Simplify:

(3)' 12 + JS'

SOP  $\rightarrow$  12

$$F(A, B, C, D) = \underline{ACD} + \underline{CD} + A\bar{B} + ABCD$$

To the minimum SOP form & POS form:-

	A' B	A' B	A B	A B
D'	CD	$\bar{A}'\bar{B}$	$\bar{A}'B$	$A\bar{B}$
C'	CD	0	0	0
D	CD	1	1	1
C	CD	1	1	1
	CD	0	0	0
	CD	0	1	1

\* SOP:  $\square^{\circ}s$

$$\hookrightarrow F = \bar{C}D + A\bar{B} + AC$$

\* POS:  $\rightarrow \square^{\circ}s$

$$\hookrightarrow F = \bar{A}C + \bar{A}D + B\bar{C}\bar{D}$$

$$\hookrightarrow (F')' = (\bar{A}C + \bar{A}D + B\bar{C}\bar{D})'$$

$$\hookrightarrow F = (A + C)(A + D)(B + C + D)$$

Ex: Simplify:

$$f(A, B, C, D) = \text{مخرج المدخلات}$$

$$(A' + B + D')(A' + B' + C')(A' + B' + C)$$

Pos  $(B' + C + D') \rightarrow T$  SOP & P-IN

Ans.

$$f' = ABD + ABC + ABC' + BCD$$

OP

	A	B	A'	B'
D'	AB	AB'	AB	A'B'
C'	CD	CD	CD	CD
D	CD	CD	CD	CD
C	CD	CD	CD	CD

The Karnaugh map shows the following minterms marked with circles: M<sub>0</sub>, M<sub>1</sub>, M<sub>2</sub>, M<sub>3</sub>, M<sub>4</sub>, M<sub>5</sub>, M<sub>6</sub>, M<sub>7</sub>, M<sub>10</sub>, M<sub>11</sub>, M<sub>12</sub>, M<sub>13</sub>, M<sub>14</sub>, M<sub>15</sub>. Red circles highlight groups of 4 (M<sub>0</sub>-M<sub>3</sub>, M<sub>12</sub>-M<sub>15</sub>), purple circles highlight groups of 2 (M<sub>0</sub>-M<sub>1</sub>, M<sub>2</sub>-M<sub>3</sub>, M<sub>4</sub>-M<sub>5</sub>, M<sub>6</sub>-M<sub>7</sub>, M<sub>10</sub>-M<sub>11</sub>, M<sub>12</sub>-M<sub>13</sub>).

\* SOP:

$$\rightarrow f = A'B + A'C + B'D + A'CD'$$



\* POS:

$$\rightarrow f = AB + AD + BCD$$

$$\rightarrow (f')' = (A' + B')(A' + D')(B' + C' + D')$$

↑ f in Pos.

$$\textcircled{1} \Rightarrow f = \sum m ( \dots, \dots ) \Leftrightarrow \boxed{1's} \text{ on K-map}$$

$$\textcircled{2} \Rightarrow f = \prod ( \dots, \dots ) \Leftrightarrow \boxed{0's} \text{ on K-map.}$$

$$\textcircled{3} \Rightarrow f = \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad}$$

$\boxed{1's}$  on K-map.

$$\textcircled{4} \Rightarrow f = ( + + ) ( + + ) ( + + )$$

$\swarrow P = \underline{\quad} + \underline{\quad} + \underline{\quad}$   
 $\swarrow \boxed{0's} \text{ on K-map.}$

⇒ Find the minterms of the following Boolean expressions by first plotting each function in a map, then simplify them.

$$f = \dots$$

⇒ Simplify the following function to SOP (OR) POS

⇒ Convert the following Boolean function from SOP form to a simplified POS form.

$$f = \underline{\quad} + \underline{\quad} + \underline{\quad}$$



K-map with don't Cates.

ENR

E(X) Simplify y.:  $F(x, y, z) = \varepsilon(0, 1, 4, 5, 6) \rightarrow$  15  
 $d(x, y, z) = \varepsilon(2, 3, 7) \rightarrow +$

$Xy$	$xy$	$X'y$	$xy$	$X'y$
$z_1^0$	1	2	$x$	$b_1$
$z_2^1$	1	3	$x$	$f_1$
$z_3^1$	1	3	$x$	$s_1$

$$\angle F = 1$$

Ex(2)

Simplify:  $F(A, B, C, D) = \Sigma(2, 4, 7, 10, 12)$

$$d(A, B, c, D) = \varepsilon(0, 6, \delta)$$

## To SOP Form

to pos farm

	AB	<del>AB</del>	<del>AB</del>	AB	AB
CD	0	X	4	1	12
CD	1		5		9
CD	3	7	1.	15	11
CD	2	16	X	14	16

$$\rightarrow F = \vec{CD} + \vec{BO} + \vec{AC}$$

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$\bar{A}B$	$\bar{A}\bar{B}$	$\bar{A}B$	$AB$	$AB$
$CD$				
$\vdash p$	X			X
$\dashv p$	0	0	0	0
$CD$	0		0	0
$\dashv \bar{C}\bar{D}$		X	0	0

$$\vec{F} = \vec{c}D + \vec{B}D + \vec{A}Br$$

$$G_F = (c + \delta)(\beta + \rho)$$

$$(A \cdot B + C)$$

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Ex 3:

Simplify:

$$F(W, X, Y, Z) = \sum m(4, 6, 11, 12, 13) + \sum d(3, 5, 7, 9, 10)$$

	W'X'	W'X	WX'	WX	
Y'Z'	0	4	11	12	13
Y'Z	5	X	13	1	9
YZ'	3	X	7	X	15
YZ	2	6	14	10	X

SOP.

$$\rightarrow F = W'X + X'Y + W'X'Z / W'X'Y / X'Y'Z$$

$$SF_1 = W'X + X'Y + W'X'Z$$

$$P_2 = W'X + X'Y + W'X'Y$$

$$P_3 = W'X + X'Y + X'Y'Z$$

	W'X'	W'X	WX'	WX	
Y'Z'	0			0	
Y'Z	0	X		X	
YZ'	X	X	0		
YZ	0		0	X	

P/S

$$\rightarrow P = W'X + X'Y + W'X'Y$$

$$\rightarrow SF = (W + X)(X'Y)(W' + X' + Y)$$



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\* two level NAND must be SOP.

\* two level NOR must be POS.

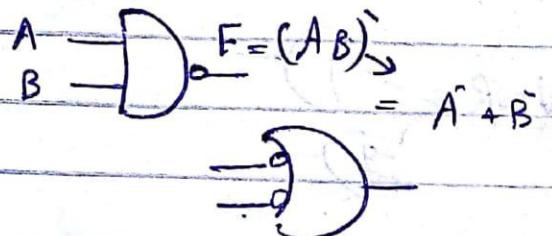
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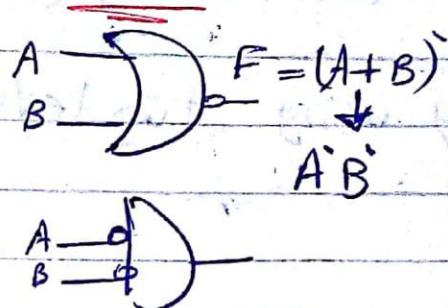
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### \* logic Diagrams ..

#### NAND:



#### NOR:

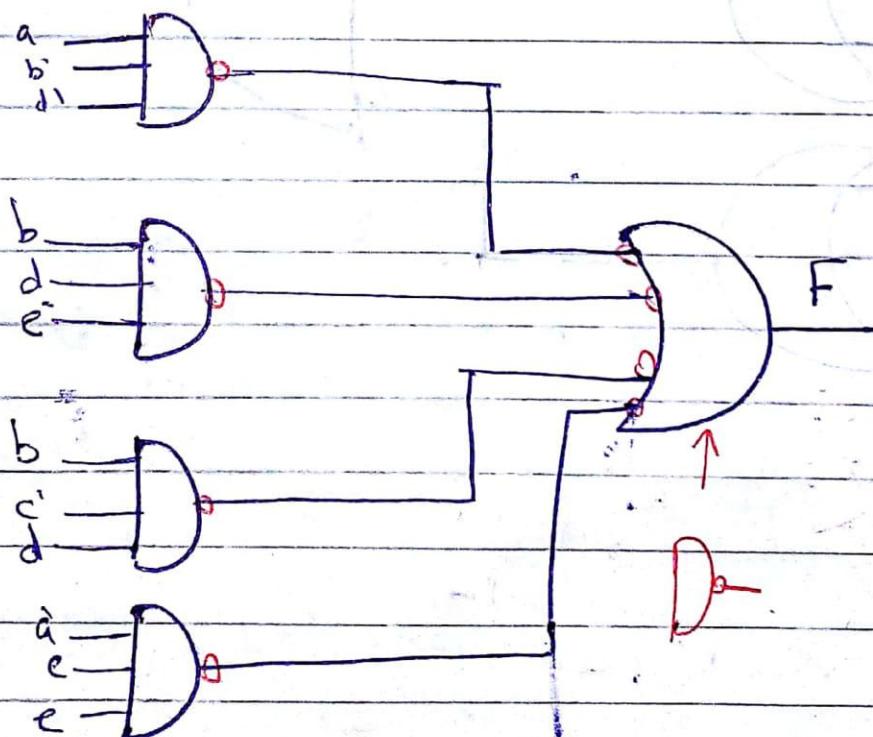


#### EX1 ..

↳ Show the block diagram of:

$$F = ab'd' + bde' + b'cd + ace$$

by using two level NAND

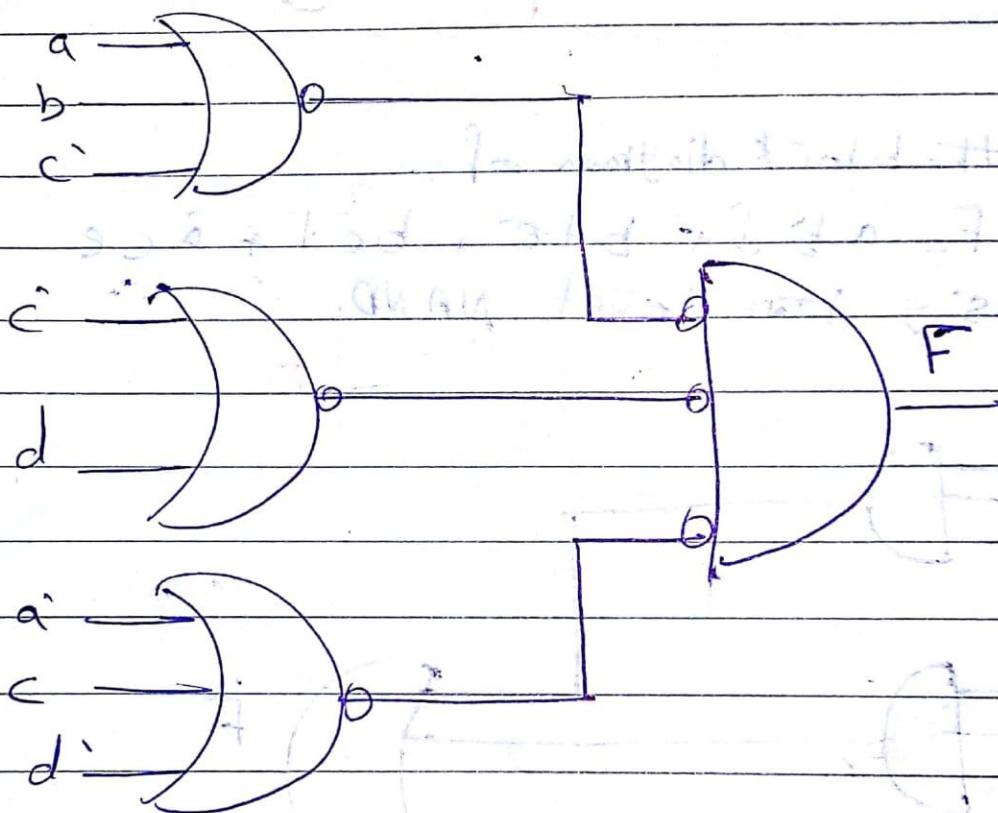


Ex2

↳ Show the block diagram of:

$$F = (a+b+c)(c+d)(a+c+d') \leftarrow \text{pos.}$$

↳ by using Two level NOR



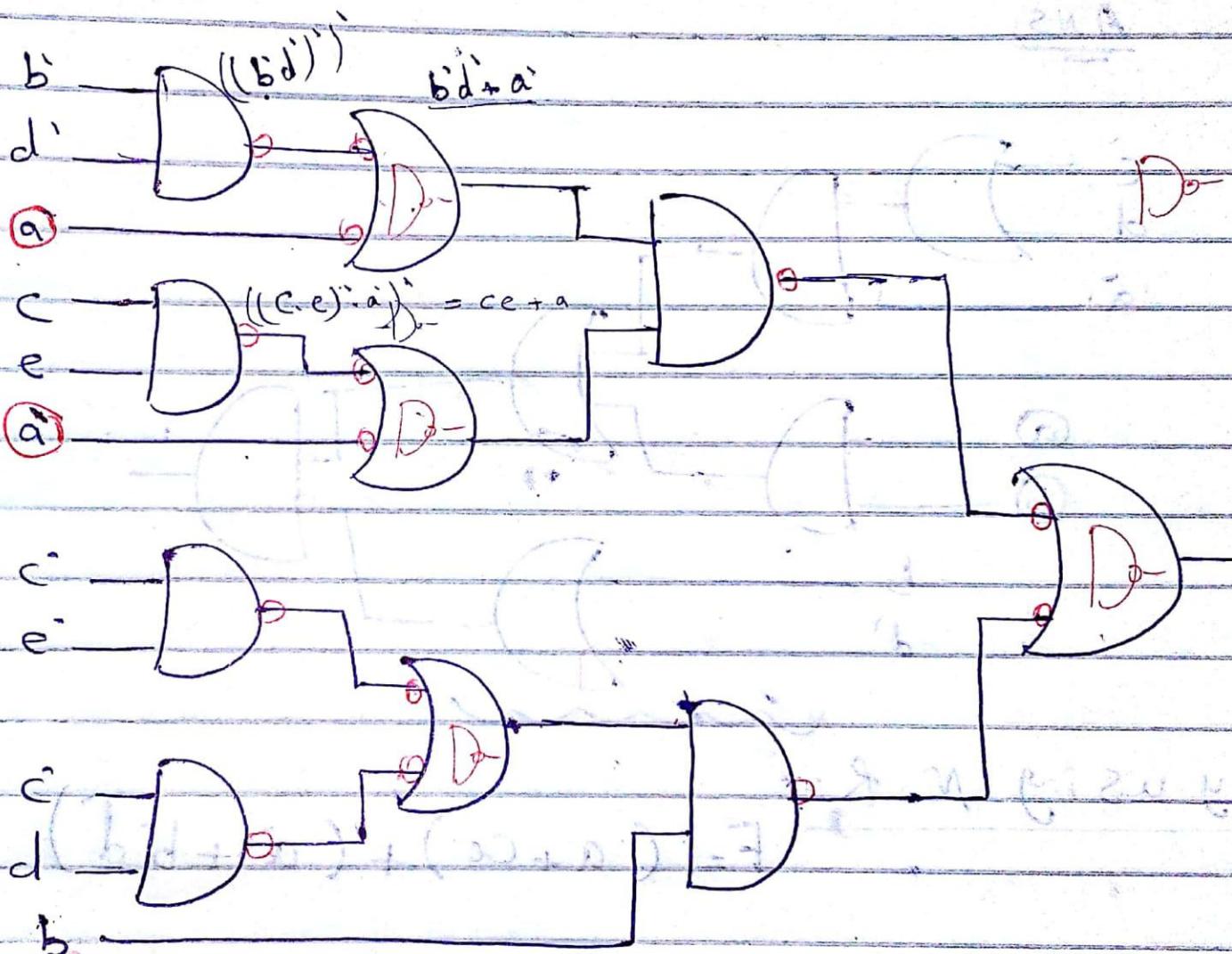
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 $b \rightarrow b$  (All Variable available)  
 $a, a', b, b'$  / / :  
: world's largest

Ex 3:

Show the block diagram of.

$$F = b(c'd + c'e') + (a + ce)(a' + b'd')$$

→ Using Multilevel NAND.



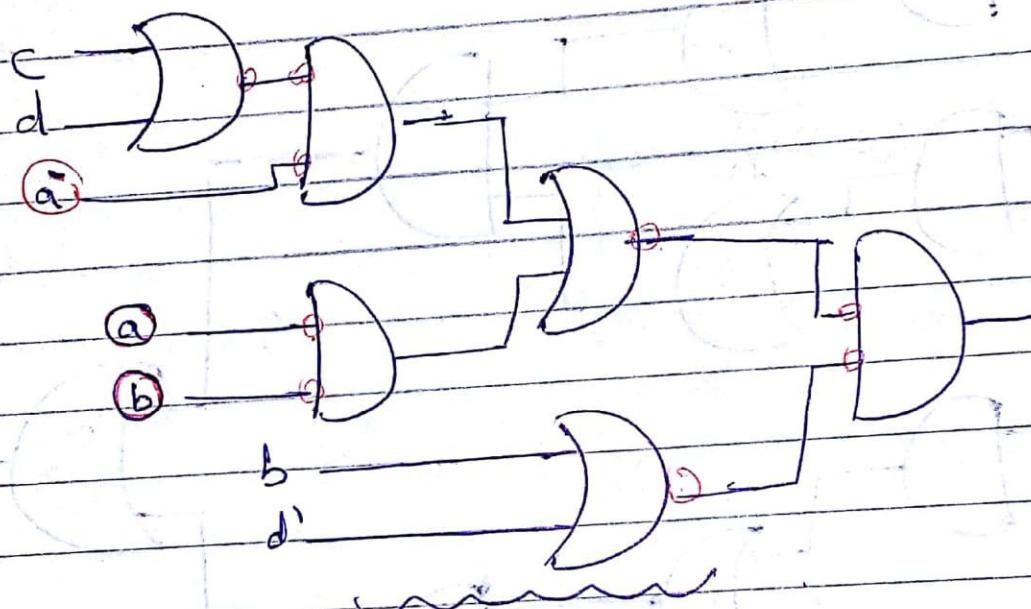
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EX4:

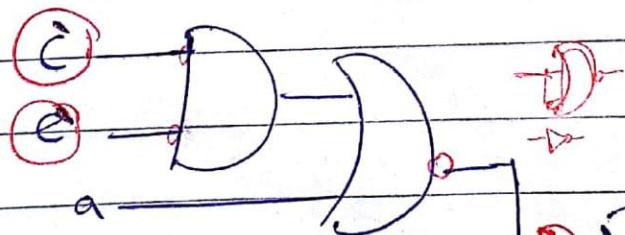
By using multi level NOR

$$F = [a'b' + a(c+d)] \cdot (b+d)$$

ANS:

by using NOR:

$$F = (a+ce) + (\bar{a}+bd')$$



$\times$   $\times$   
not



Ex:

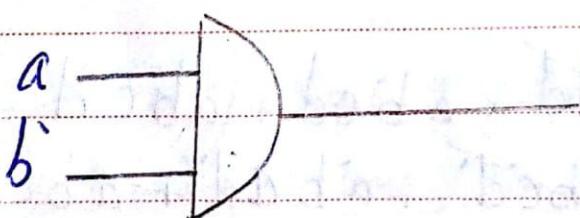
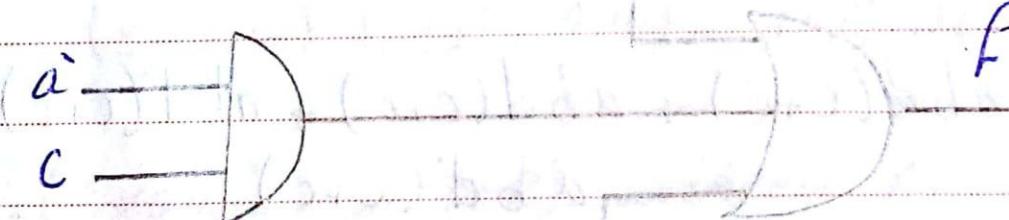
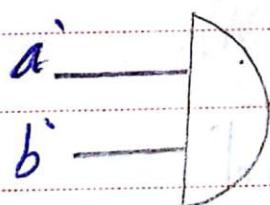
Given the function, (assume all variables are available)  
both complemented and uncomplemented)

$$F = \bar{a}'\bar{b}' + \bar{a}\bar{c} + ab$$

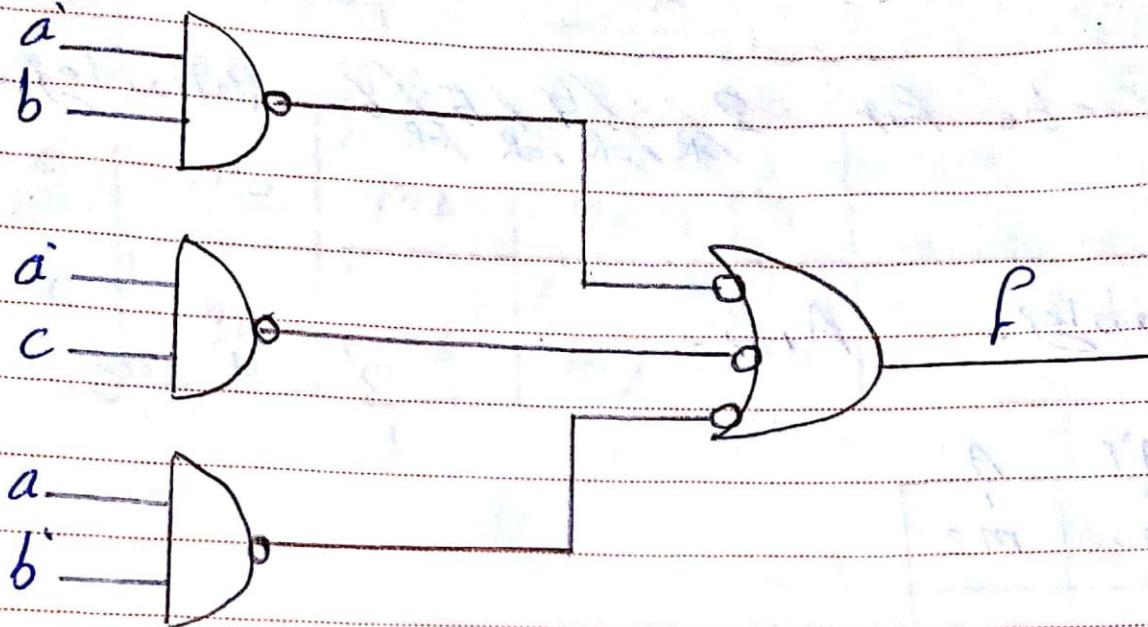
- a) Show a block diagram for a two-level implementation of  $F$  using AND and OR gates.
- b) Show a block diagram for an implementation of  $F$  using only NAND gates.
- c) Expand  $F$  to sum of minterms, eliminate any duplication.

Solutions:

a) The Block diagram by AND, OR.



b) The Block diagram by NAND:



c) The EXPanding of  $f = \bar{a}\bar{b} + \bar{a}\bar{c} + \bar{a}\bar{b}$

$$\begin{aligned}
 f &= \bar{a}\bar{b}(c+c') + \bar{a}\bar{c}(b+b') + \bar{a}\bar{b}(c+c') \\
 &= \bar{a}\bar{b}c + \bar{a}\bar{b}c' + \bar{a}\bar{b}c + \bar{a}\bar{b}c' + \bar{a}\bar{b}c + \bar{a}\bar{b}c' \\
 &= \bar{a}\bar{b}c + \bar{a}\bar{b}c' + \bar{a}\bar{b}c + \bar{a}\bar{b}c' + \bar{a}\bar{b}c
 \end{aligned}$$