

ASSIGNMENT 4: FACE DETECTION

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(1) Summary

The aim of this project is to classify images based on the concept of Eigenface approach. We have a training data set, where we need to apply this concept of Eigen vectors in order to identify eigen faces from the training set. We need to follow this procedure for different values of the number of eigen faces chosen for comparison, the maximum of which is the total number of testing images. Using this eigenface approach for classifying faces, we have to find out the total number of images correctly recognized from the entire pool of the testing images and also in case of the subjects of the testing dataset.

A few other things mentioned for us to try out were to compare the faces from the two different sets using different metrics in order to compare the performance. And we also have to try to perform this procedure in different colour spaces.

(2) Brief Outline of Algorithmic Approach

- ➔ The first step is to create a vector of all the images from the training dataset in the required colour space. And then we calculate the mean of all the images.
- ➔ The calculated mean is then subtracted from all the values in the vector and then assign them to a image matrix.
- ➔ Now, we need to find the Eigen Decomposition of the image matrix to obtain eigen vectors and their values.
- ➔ The largest K values perform the better characterization of features. Hence, we can choose the later K values for accuracy from the ascending order of the values from the eigen vectors.
- ➔ From here, we can multiply the top K eigen vectors with image matrix to get the Eigen faces. We finally obtain the training alpha by multiplying the transpose of eigen faces with the image matrix.
- ➔ Now we have to perform the testing, where the testing images are the reference features that are compared with the calculated eigen features using a distance metric.
- ➔ The lesser the distance between the eigen value and the reference image, the more chances of them being recognized correctly. The one with the smallest distance is the match and we calculate its accuracy.
- ➔ We also calculate the subject accuracy where we compare each subject(and their images) in testing with all subjects in training and check which subject in the training has the least distance with the testing. This process is repeated for all the subjects in the testing set.

(3) Intermediate and Final Results

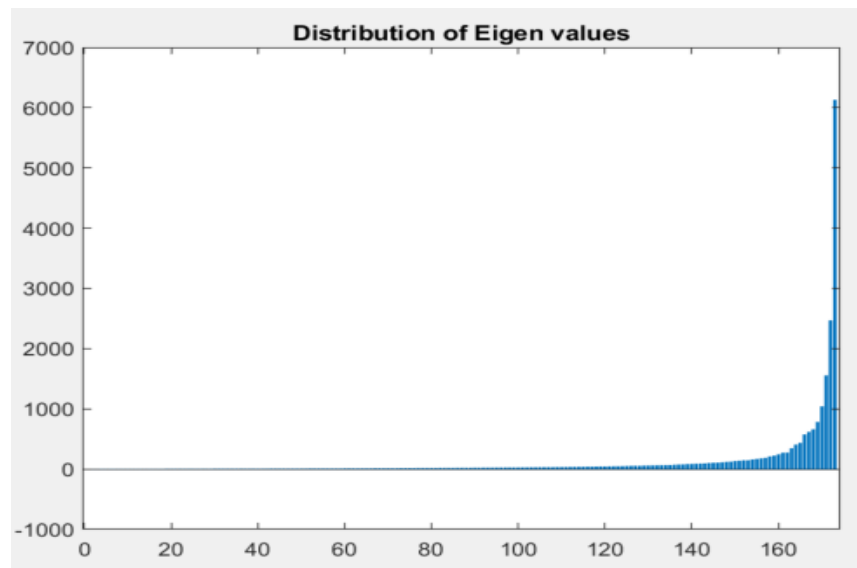


Figure: Eigen Values in Ascending order

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Eigen Faces Algorithm
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Value of K: 100
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Euclidean Image Accuracy: 0.41
Euclidean Subject Accuracy: 0.54
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Manhattan Image Accuracy: 0.56
Manhattan Subject Accuracy: 0.54
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Mahalanobis Image Accuracy: 0.39
Mahalanobis Subject Accuracy: 0.54
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Figure: Final Result

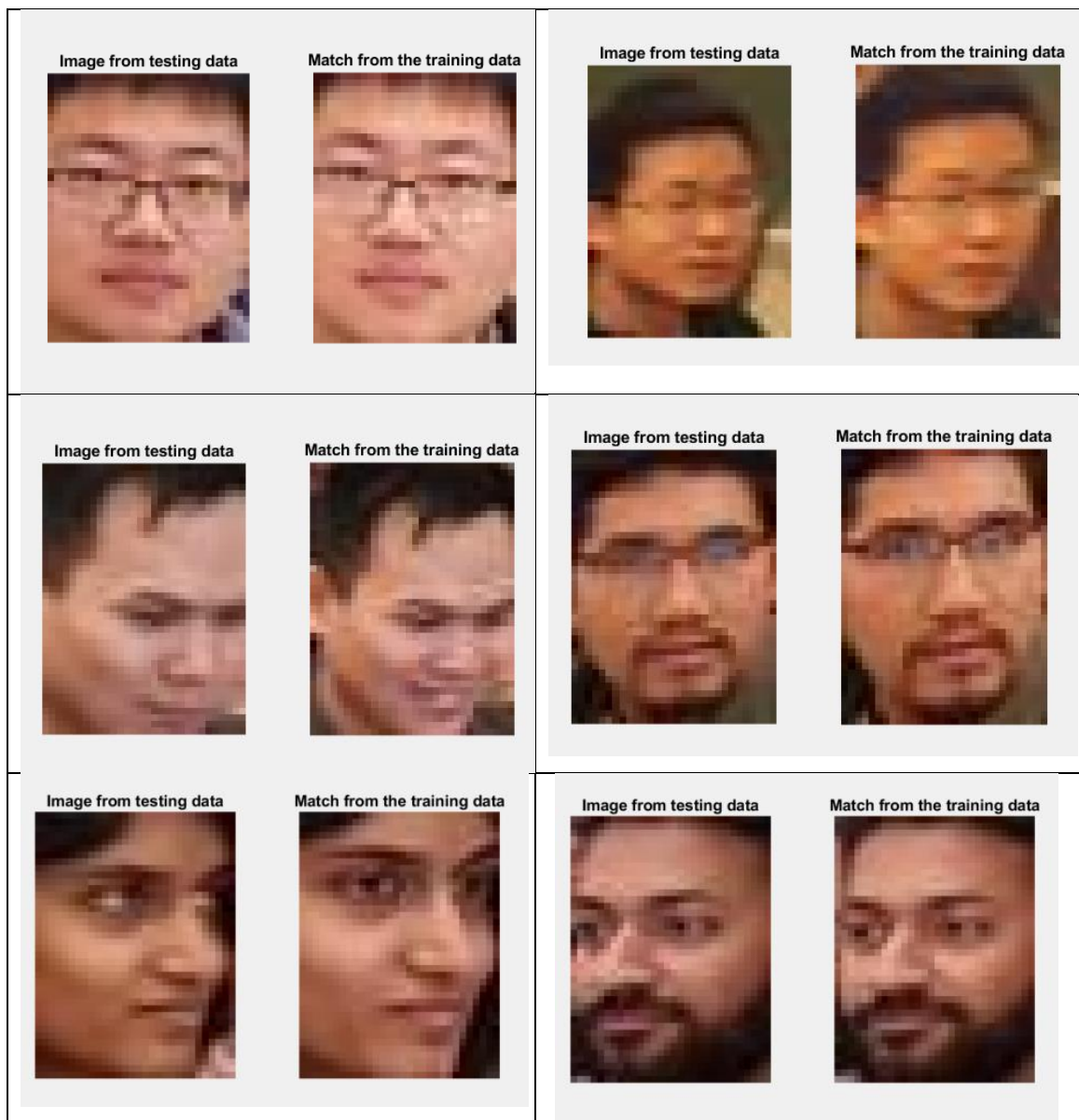


Figure: Output of matched faces

RGB

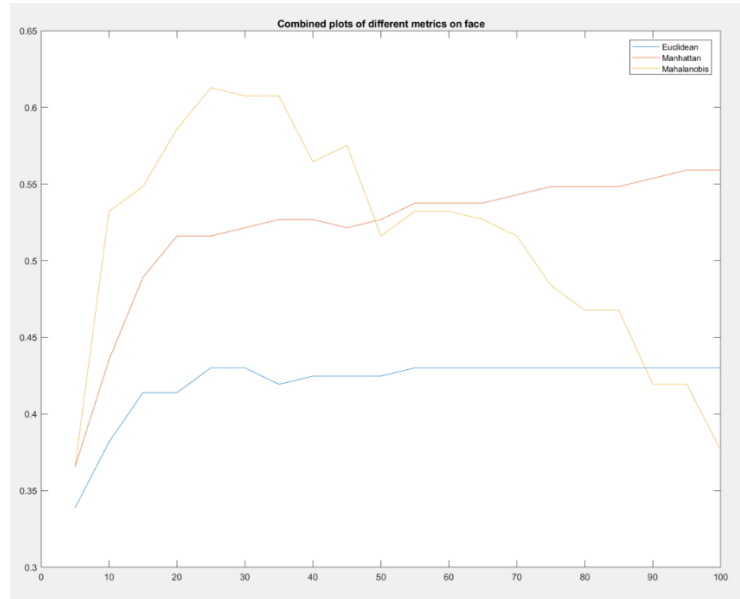


Figure: Accuracy of Faces using different metrics

| K | Face Accuracy | | | Subject Accuracy | | |
|-----|---------------|-------------|-------------|------------------|-------------|-------------|
| | Euclidean | Manhattan | Mahalanobis | Euclidean | Manhattan | Mahalanobis |
| 5 | 0.33870968 | 0.365591398 | 0.365591398 | 0.571428571 | 0.571428571 | 0.571428571 |
| 10 | 0.38172043 | 0.435483871 | 0.532258065 | 0.535714286 | 0.535714286 | 0.535714286 |
| 15 | 0.41397849 | 0.489247312 | 0.548387097 | 0.571428571 | 0.571428571 | 0.571428571 |
| 20 | 0.41397849 | 0.516129032 | 0.586021505 | 0.535714286 | 0.535714286 | 0.535714286 |
| 25 | 0.43010753 | 0.516129032 | 0.612903226 | 0.678571429 | 0.678571429 | 0.678571429 |
| 30 | 0.43010753 | 0.521505376 | 0.607526882 | 0.571428571 | 0.571428571 | 0.571428571 |
| 35 | 0.41935484 | 0.52688172 | 0.607526882 | 0.642857143 | 0.642857143 | 0.642857143 |
| 40 | 0.42473118 | 0.52688172 | 0.564516129 | 0.535714286 | 0.535714286 | 0.535714286 |
| 45 | 0.42473118 | 0.521505376 | 0.575268817 | 0.535714286 | 0.535714286 | 0.535714286 |
| 50 | 0.42473118 | 0.52688172 | 0.516129032 | 0.571428571 | 0.571428571 | 0.571428571 |
| 55 | 0.43010753 | 0.537634409 | 0.532258065 | 0.678571429 | 0.678571429 | 0.678571429 |
| 60 | 0.43010753 | 0.537634409 | 0.532258065 | 0.607142857 | 0.607142857 | 0.607142857 |
| 65 | 0.43010753 | 0.537634409 | 0.52688172 | 0.607142857 | 0.607142857 | 0.607142857 |
| 70 | 0.43010753 | 0.543010753 | 0.516129032 | 0.642857143 | 0.642857143 | 0.642857143 |
| 75 | 0.43010753 | 0.548387097 | 0.483870968 | 0.607142857 | 0.607142857 | 0.607142857 |
| 80 | 0.43010753 | 0.548387097 | 0.467741935 | 0.571428571 | 0.571428571 | 0.571428571 |
| 85 | 0.43010753 | 0.548387097 | 0.467741935 | 0.642857143 | 0.642857143 | 0.642857143 |
| 90 | 0.43010753 | 0.553763441 | 0.419354839 | 0.571428571 | 0.571428571 | 0.571428571 |
| 95 | 0.43010753 | 0.559139785 | 0.419354839 | 0.678571429 | 0.678571429 | 0.678571429 |
| 100 | 0.43010753 | 0.559139785 | 0.376344086 | 0.642857143 | 0.642857143 | 0.642857143 |

HSV

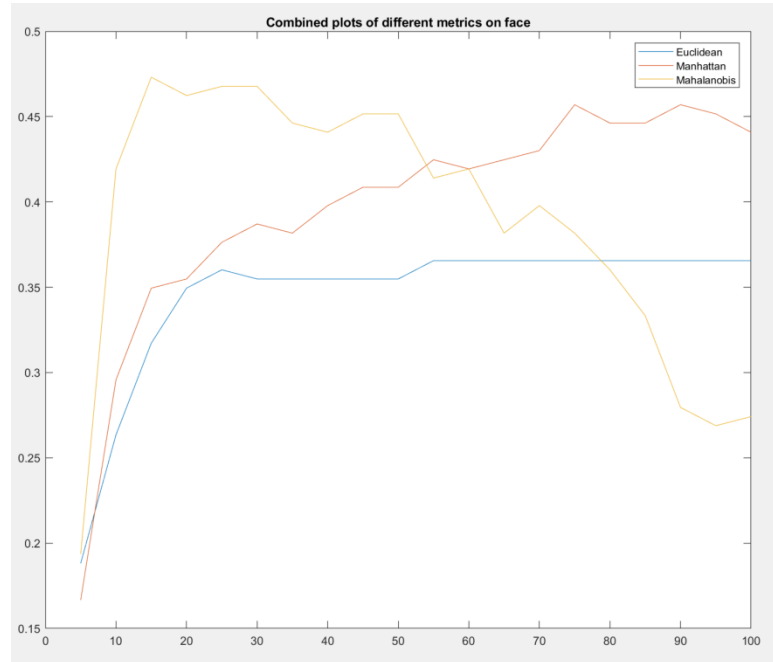


Figure: Accuracy of Faces using different metrics

| K | Face Accuracy | | | Subject Accuracy | | |
|-----|---------------|-------------|-------------|------------------|------------|-------------|
| | Euclidean | Manhattan | Mahalanobis | Euclidean | Manhattan | Mahalanobis |
| 5 | 0.188172 | 0.166666667 | 0.19354839 | 0.571429 | 0.57142857 | 0.571428571 |
| 10 | 0.263441 | 0.295698925 | 0.41935484 | 0.607143 | 0.60714286 | 0.607142857 |
| 15 | 0.317204 | 0.349462366 | 0.47311828 | 0.607143 | 0.60714286 | 0.607142857 |
| 20 | 0.349462 | 0.35483871 | 0.46236559 | 0.571429 | 0.57142857 | 0.571428571 |
| 25 | 0.360215 | 0.376344086 | 0.46774194 | 0.75 | 0.75 | 0.75 |
| 30 | 0.354839 | 0.387096774 | 0.46774194 | 0.642857 | 0.64285714 | 0.642857143 |
| 35 | 0.354839 | 0.38172043 | 0.44623656 | 0.607143 | 0.60714286 | 0.607142857 |
| 40 | 0.354839 | 0.397849462 | 0.44086022 | 0.642857 | 0.64285714 | 0.642857143 |
| 45 | 0.354839 | 0.408602151 | 0.4516129 | 0.607143 | 0.60714286 | 0.607142857 |
| 50 | 0.354839 | 0.408602151 | 0.4516129 | 0.5 | 0.5 | 0.5 |
| 55 | 0.365591 | 0.424731183 | 0.41397849 | 0.535714 | 0.53571429 | 0.535714286 |
| 60 | 0.365591 | 0.419354839 | 0.41935484 | 0.642857 | 0.64285714 | 0.642857143 |
| 65 | 0.365591 | 0.424731183 | 0.38172043 | 0.571429 | 0.57142857 | 0.571428571 |
| 70 | 0.365591 | 0.430107527 | 0.39784946 | 0.571429 | 0.57142857 | 0.571428571 |
| 75 | 0.365591 | 0.456989247 | 0.38172043 | 0.535714 | 0.53571429 | 0.535714286 |
| 80 | 0.365591 | 0.446236559 | 0.36021505 | 0.535714 | 0.53571429 | 0.535714286 |
| 85 | 0.365591 | 0.446236559 | 0.33333333 | 0.642857 | 0.64285714 | 0.642857143 |
| 90 | 0.365591 | 0.456989247 | 0.27956989 | 0.464286 | 0.46428571 | 0.464285714 |
| 95 | 0.365591 | 0.451612903 | 0.2688172 | 0.535714 | 0.53571429 | 0.535714286 |
| 100 | 0.365591 | 0.440860215 | 0.27419355 | 0.678571 | 0.67857143 | 0.678571429 |

YCbCr

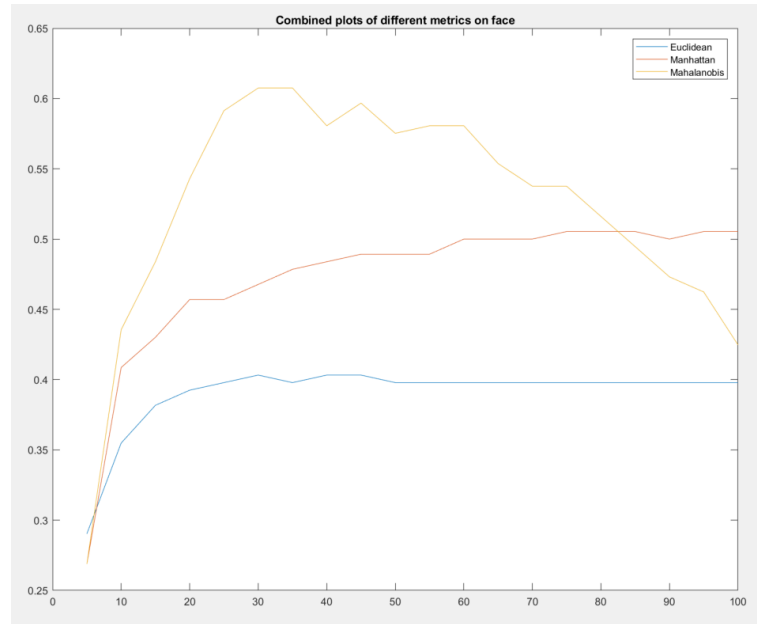


Figure: Accuracy of Faces using different metrics

| K | Face Accuracy | | | Subject Accuracy | | |
|-----|---------------|-------------|-------------|------------------|------------|-------------|
| | Euclidean | Manhattan | Mahalanobis | Euclidean | Manhattan | Mahalanobis |
| 5 | 0.290322581 | 0.268817204 | 0.268817204 | 0.57142857 | 0.57142857 | 0.571428571 |
| 10 | 0.35483871 | 0.408602151 | 0.435483871 | 0.64285714 | 0.64285714 | 0.642857143 |
| 15 | 0.38172043 | 0.430107527 | 0.483870968 | 0.60714286 | 0.60714286 | 0.607142857 |
| 20 | 0.392473118 | 0.456989247 | 0.543010753 | 0.67857143 | 0.67857143 | 0.678571429 |
| 25 | 0.397849462 | 0.456989247 | 0.591397849 | 0.64285714 | 0.64285714 | 0.642857143 |
| 30 | 0.403225806 | 0.467741935 | 0.607526882 | 0.60714286 | 0.60714286 | 0.607142857 |
| 35 | 0.397849462 | 0.478494624 | 0.607526882 | 0.67857143 | 0.67857143 | 0.678571429 |
| 40 | 0.403225806 | 0.483870968 | 0.580645161 | 0.64285714 | 0.64285714 | 0.642857143 |
| 45 | 0.403225806 | 0.489247312 | 0.596774194 | 0.57142857 | 0.57142857 | 0.571428571 |
| 50 | 0.397849462 | 0.489247312 | 0.575268817 | 0.57142857 | 0.57142857 | 0.571428571 |
| 55 | 0.397849462 | 0.489247312 | 0.580645161 | 0.64285714 | 0.64285714 | 0.642857143 |
| 60 | 0.397849462 | 0.5 | 0.580645161 | 0.64285714 | 0.64285714 | 0.642857143 |
| 65 | 0.397849462 | 0.5 | 0.553763441 | 0.60714286 | 0.60714286 | 0.607142857 |
| 70 | 0.397849462 | 0.5 | 0.537634409 | 0.5 | 0.5 | 0.5 |
| 75 | 0.397849462 | 0.505376344 | 0.537634409 | 0.64285714 | 0.64285714 | 0.642857143 |
| 80 | 0.397849462 | 0.505376344 | 0.516129032 | 0.57142857 | 0.57142857 | 0.571428571 |
| 85 | 0.397849462 | 0.505376344 | 0.494623656 | 0.67857143 | 0.67857143 | 0.678571429 |
| 90 | 0.397849462 | 0.5 | 0.47311828 | 0.67857143 | 0.67857143 | 0.678571429 |
| 95 | 0.397849462 | 0.505376344 | 0.462365591 | 0.53571429 | 0.53571429 | 0.535714286 |
| 100 | 0.397849462 | 0.505376344 | 0.424731183 | 0.57142857 | 0.57142857 | 0.571428571 |

HSVYCbCr

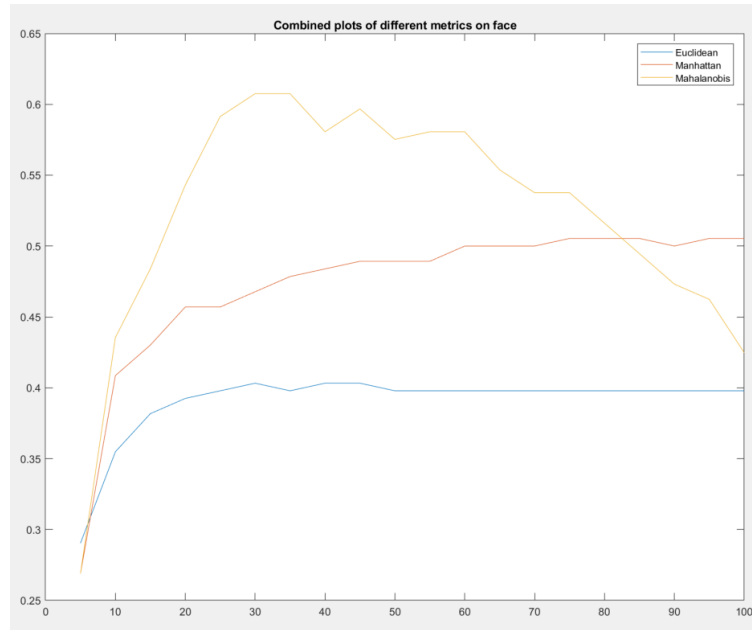


Figure: Accuracy of Faces using different metrics

| K | Face Accuracy | | | Subject Accuracy | | |
|-----|---------------|-----------|-------------|------------------|-------------|-------------|
| | Euclidean | Manhattan | Mahalanobis | Euclidean | Manhattan | Mahalanobis |
| 5 | 0.290323 | 0.268817 | 0.284946 | 0.571429 | 0.571428571 | 0.571428571 |
| 10 | 0.344086 | 0.408602 | 0.451613 | 0.714286 | 0.714285714 | 0.714285714 |
| 15 | 0.397849 | 0.473118 | 0.532258 | 0.535714 | 0.535714286 | 0.535714286 |
| 20 | 0.408602 | 0.510753 | 0.569892 | 0.535714 | 0.535714286 | 0.535714286 |
| 25 | 0.413978 | 0.548387 | 0.543011 | 0.5 | 0.5 | 0.5 |
| 30 | 0.408602 | 0.537634 | 0.569892 | 0.607143 | 0.607142857 | 0.607142857 |
| 35 | 0.413978 | 0.55914 | 0.596774 | 0.535714 | 0.535714286 | 0.535714286 |
| 40 | 0.413978 | 0.564516 | 0.580645 | 0.678571 | 0.678571429 | 0.678571429 |
| 45 | 0.413978 | 0.564516 | 0.596774 | 0.571429 | 0.571428571 | 0.571428571 |
| 50 | 0.419355 | 0.564516 | 0.602151 | 0.5 | 0.5 | 0.5 |
| 55 | 0.419355 | 0.575269 | 0.586022 | 0.571429 | 0.571428571 | 0.571428571 |
| 60 | 0.419355 | 0.575269 | 0.586022 | 0.571429 | 0.571428571 | 0.571428571 |
| 65 | 0.419355 | 0.575269 | 0.569892 | 0.642857 | 0.642857143 | 0.642857143 |
| 70 | 0.419355 | 0.575269 | 0.526882 | 0.571429 | 0.571428571 | 0.571428571 |
| 75 | 0.419355 | 0.575269 | 0.537634 | 0.571429 | 0.571428571 | 0.571428571 |
| 80 | 0.419355 | 0.575269 | 0.564516 | 0.535714 | 0.535714286 | 0.535714286 |
| 85 | 0.419355 | 0.575269 | 0.537634 | 0.607143 | 0.607142857 | 0.607142857 |
| 90 | 0.419355 | 0.575269 | 0.521505 | 0.571429 | 0.571428571 | 0.571428571 |
| 95 | 0.419355 | 0.575269 | 0.505376 | 0.75 | 0.75 | 0.75 |
| 100 | 0.419355 | 0.575269 | 0.473118 | 0.714286 | 0.714285714 | 0.714285714 |

Gradient

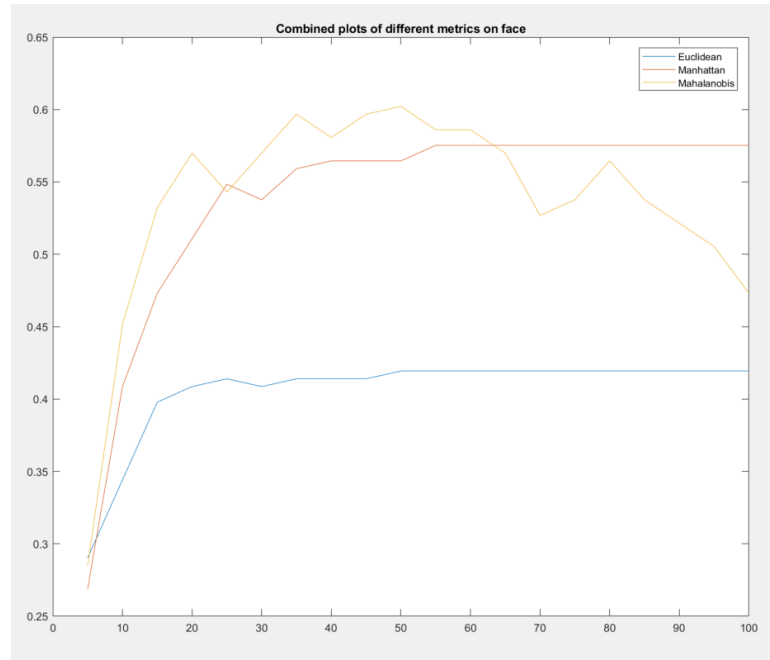


Figure: Accuracy of Faces using different metrics

| K | Face Accuracy | | | Subject Accuracy | | |
|-----|---------------|----------|-----------|------------------|----------|-----------|
| | Euclidean | Manhatta | Mahalanob | Euclidean | Manhatta | Mahalanob |
| | n | n | is | n | n | is |
| 5 | 0.290323 | 0.268817 | 0.284946 | 0.571429 | 0.571429 | 0.571429 |
| 10 | 0.344086 | 0.408602 | 0.451613 | 0.714286 | 0.714286 | 0.714286 |
| 15 | 0.397849 | 0.473118 | 0.532258 | 0.535714 | 0.535714 | 0.535714 |
| 20 | 0.408602 | 0.510753 | 0.569892 | 0.535714 | 0.535714 | 0.535714 |
| 25 | 0.413978 | 0.548387 | 0.543011 | 0.5 | 0.5 | 0.5 |
| 30 | 0.408602 | 0.537634 | 0.569892 | 0.607143 | 0.607143 | 0.607143 |
| 35 | 0.413978 | 0.55914 | 0.596774 | 0.535714 | 0.535714 | 0.535714 |
| 40 | 0.413978 | 0.564516 | 0.580645 | 0.678571 | 0.678571 | 0.678571 |
| 45 | 0.413978 | 0.564516 | 0.596774 | 0.571429 | 0.571429 | 0.571429 |
| 50 | 0.419355 | 0.564516 | 0.602151 | 0.5 | 0.5 | 0.5 |
| 55 | 0.419355 | 0.575269 | 0.586022 | 0.571429 | 0.571429 | 0.571429 |
| 60 | 0.419355 | 0.575269 | 0.586022 | 0.571429 | 0.571429 | 0.571429 |
| 65 | 0.419355 | 0.575269 | 0.569892 | 0.642857 | 0.642857 | 0.642857 |
| 70 | 0.419355 | 0.575269 | 0.526882 | 0.571429 | 0.571429 | 0.571429 |
| 75 | 0.419355 | 0.575269 | 0.537634 | 0.571429 | 0.571429 | 0.571429 |
| 80 | 0.419355 | 0.575269 | 0.564516 | 0.535714 | 0.535714 | 0.535714 |
| 85 | 0.419355 | 0.575269 | 0.537634 | 0.607143 | 0.607143 | 0.607143 |
| 90 | 0.419355 | 0.575269 | 0.521505 | 0.571429 | 0.571429 | 0.571429 |
| 95 | 0.419355 | 0.575269 | 0.505376 | 0.75 | 0.75 | 0.75 |
| 100 | 0.419355 | 0.575269 | 0.473118 | 0.714286 | 0.714286 | 0.714286 |

Gray

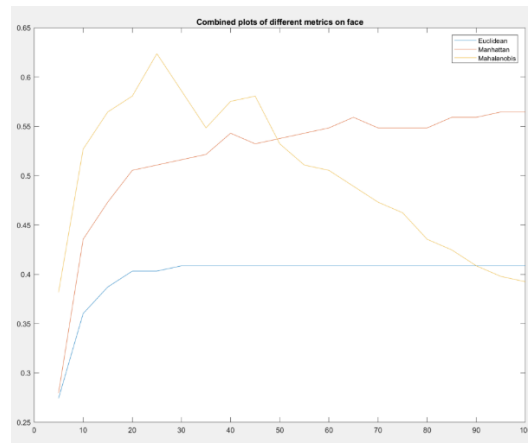


Figure: Accuracy of Faces using different metrics

| K | Face Accuracy | | | Subject Accuracy | | |
|-----|---------------|-------------|-------------|------------------|------------|-------------|
| | Euclidean | Manhattan | Mahalanobis | Euclidean | Manhattan | Mahalanobis |
| 5 | 0.274193548 | 0.279569892 | 0.38172043 | 0.5 | 0.5 | 0.5 |
| 10 | 0.360215054 | 0.435483871 | 0.52688172 | 0.6071429 | 0.60714286 | 0.60714286 |
| 15 | 0.387096774 | 0.47311828 | 0.564516129 | 0.6785714 | 0.67857143 | 0.67857143 |
| 20 | 0.403225806 | 0.505376344 | 0.580645161 | 0.5714286 | 0.57142857 | 0.57142857 |
| 25 | 0.403225806 | 0.510752688 | 0.623655914 | 0.7142857 | 0.71428571 | 0.71428571 |
| 30 | 0.408602151 | 0.516129032 | 0.586021505 | 0.5 | 0.5 | 0.5 |
| 35 | 0.408602151 | 0.521505376 | 0.548387097 | 0.5357143 | 0.53571429 | 0.53571429 |
| 40 | 0.408602151 | 0.543010753 | 0.575268817 | 0.6428571 | 0.64285714 | 0.64285714 |
| 45 | 0.408602151 | 0.532258065 | 0.580645161 | 0.6785714 | 0.67857143 | 0.67857143 |
| 50 | 0.408602151 | 0.537634409 | 0.532258065 | 0.6428571 | 0.64285714 | 0.64285714 |
| 55 | 0.408602151 | 0.543010753 | 0.510752688 | 0.5714286 | 0.57142857 | 0.57142857 |
| 60 | 0.408602151 | 0.548387097 | 0.505376344 | 0.5357143 | 0.53571429 | 0.53571429 |
| 65 | 0.408602151 | 0.559139785 | 0.489247312 | 0.5 | 0.5 | 0.5 |
| 70 | 0.408602151 | 0.548387097 | 0.47311828 | 0.5357143 | 0.53571429 | 0.53571429 |
| 75 | 0.408602151 | 0.548387097 | 0.462365591 | 0.6071429 | 0.60714286 | 0.60714286 |
| 80 | 0.408602151 | 0.548387097 | 0.435483871 | 0.6071429 | 0.60714286 | 0.60714286 |
| 85 | 0.408602151 | 0.559139785 | 0.424731183 | 0.5357143 | 0.53571429 | 0.53571429 |
| 90 | 0.408602151 | 0.559139785 | 0.408602151 | 0.5714286 | 0.57142857 | 0.57142857 |
| 95 | 0.408602151 | 0.564516129 | 0.397849462 | 0.5357143 | 0.53571429 | 0.53571429 |
| 100 | 0.408602151 | 0.564516129 | 0.392473118 | 0.5357143 | 0.53571429 | 0.53571429 |

Observations: We can observe the following accuracy patterns of different metrics in different colour spaces using different K values.

Euclidean: As the number of features increases, the accuracy of recognizing the face initially increases and then remains constant.

Manhattan: As the number of features increases, the initial accuracy grows rapidly and then keeps on growing at a slower rate.

Mahalanobis: As the number of features increase, the accuracy increases for a certain period and then drops after a certain point.