

# ASSIGNMENT 8: REGRESSION

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## (a) Brief Summary of the Project:

In this project, we have to implement different regression methods to classify a given image as face or background. There are two datasets consisting of both face and background images which we have to use for training and testing. Regression is a statistical process of estimating relationships among variables. Different regression models should be implemented for classifying the images. Also, for each method, we need to learn the parameters from the training dataset and infer the label of test images (face or background).

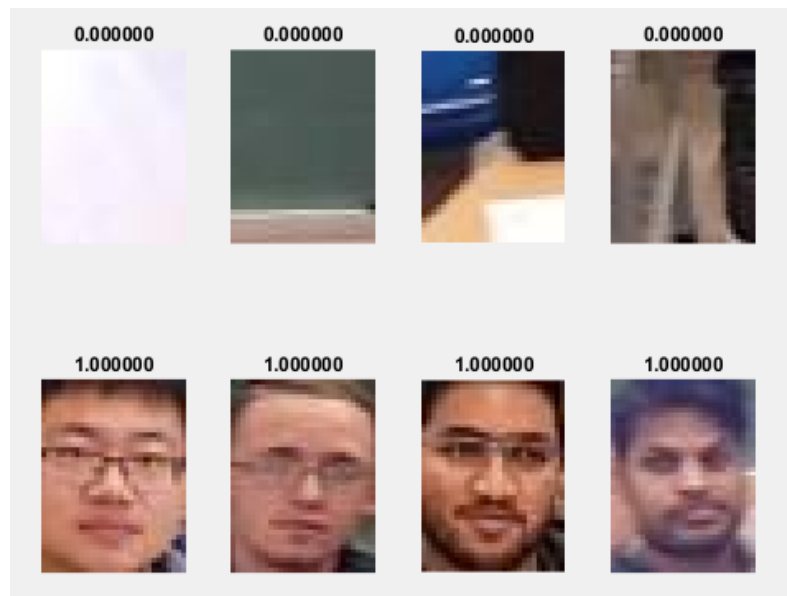
## (b) Outline of the algorithmic approach:

We have to implement different regression models as following for the detection process:

1. Logistic Regression: First we perform the Logistic Regression, where the output is characterized as a function of the input images with corresponding weights as coefficients to these images. One or more elements determine this output. We have to generate a matrix of all the face and background images and determine the  $\phi$  vector. We have to infer the classification of the test images using these  $\phi$  values.
2. Bayesian Logistic Regression: Next method is same as the logistic regression, in addition, a prior probability distribution for the  $\phi$  is considered and then the conditional probability of  $\phi$  is represented with a normal pdf to employ Laplace approximation. After learning the  $\phi$  values, the inference is made possible.
3. Dual Logistic Regression: Here, the value of  $\phi$  is factorized into a product of  $X$  and  $\psi$ , where  $\psi$  has a dimension of the length of the input images whereas  $\phi$  is of length of pixels in each input image. Using  $\psi$ , we can handle input images which are very big in size and have complex calculations.
4. Dual Bayesian Logistic Regression: In the next task, we have to find the coefficients to get the inference on test images. For this, we combine the prior and the  $\psi$  approach.
5. Kernel Logistic Regression: In this approach, we need to find the kernel. Using Logistic Regression, we compute the dot product of input image with itself.
6. Relevance Vector Logistic Regression: Here again use the previous technique along with an additional parameter  $\nu$ . Later the predictions are used to classify the images.

### (c) Pictures of intermediate or final results

The Miss Detection values of the regression models should be closer to zero for better classification and accordingly the performance of the Dual Logistic and Bayesian Logistic regressions should be better than the logistic regression. But as you can see from the output results, the miss detection value of Bayesian is worse than Logistic Regression and that of Dual approach is almost the same as Logistic Regression. The reason behind it might be due to the zero initialized Psi.

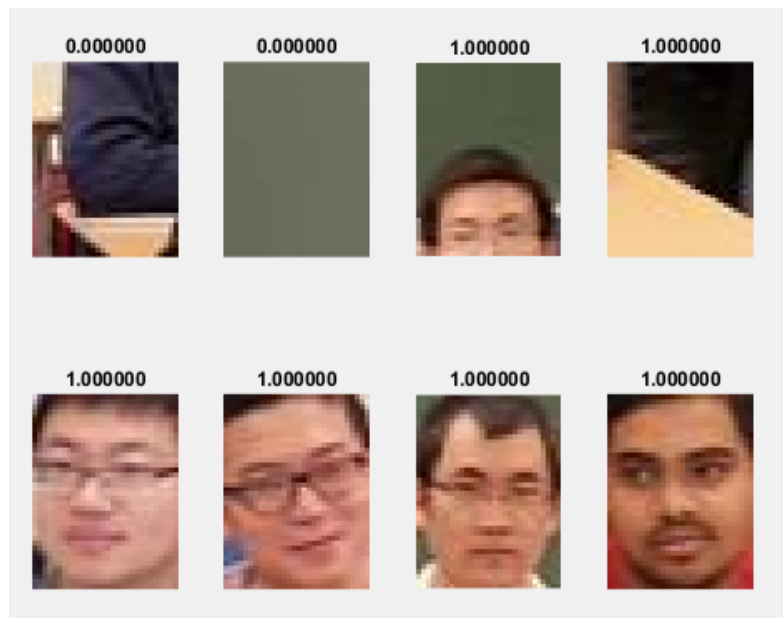


Logistic Regression

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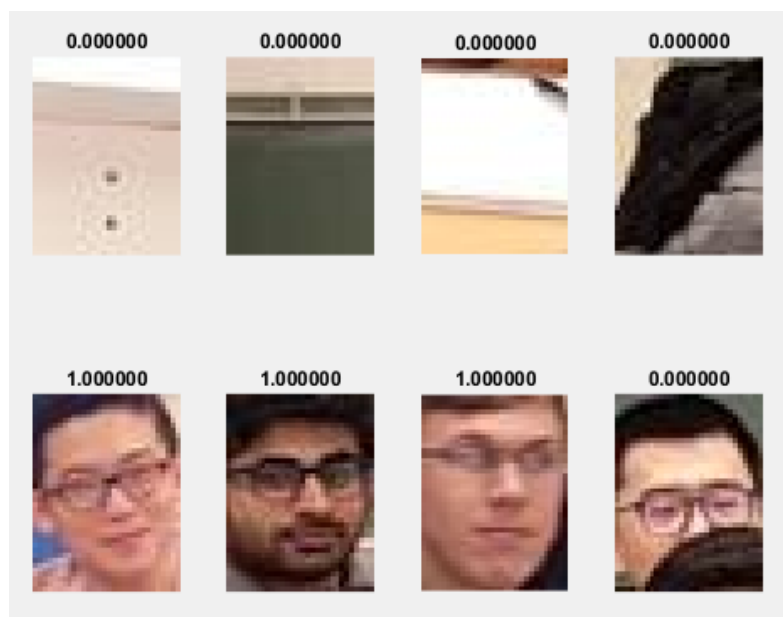
Miss Detection Rate: 0.025126

False Alarm Rate: 0.156977

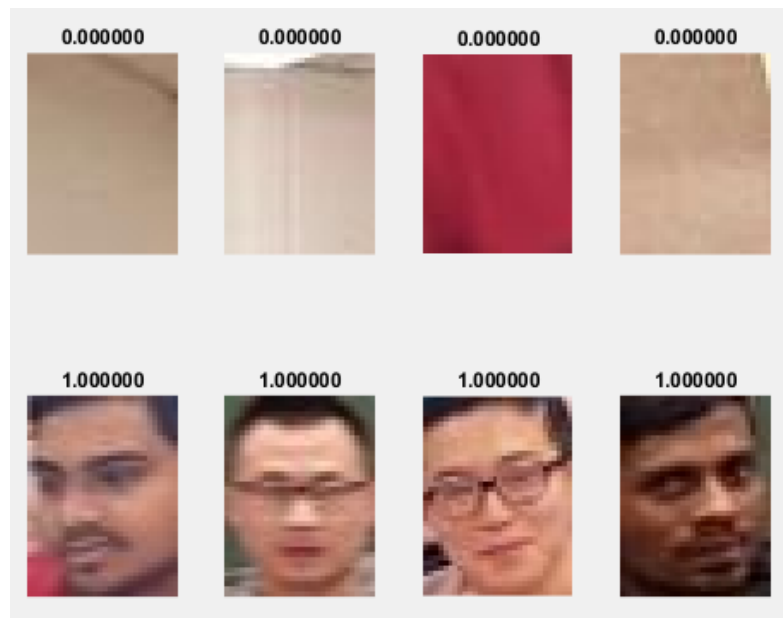


Bayesian Logistic Regression  
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 Miss Detection Rate: 0.050251  
 False Alarm Rate: 0.203488

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Dual Logistic Regression  
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 Miss Detection Rate: 0.025126  
 False Alarm Rate: 0.162791

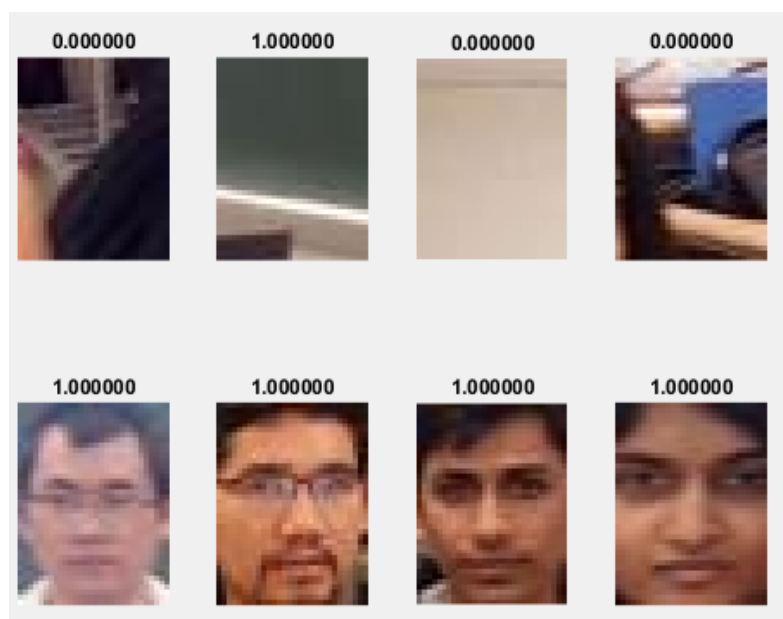


Dual Bayesian Logistic Regression

Miss Detection Rate: 0.025126

False Alarm Rate: 0.156977

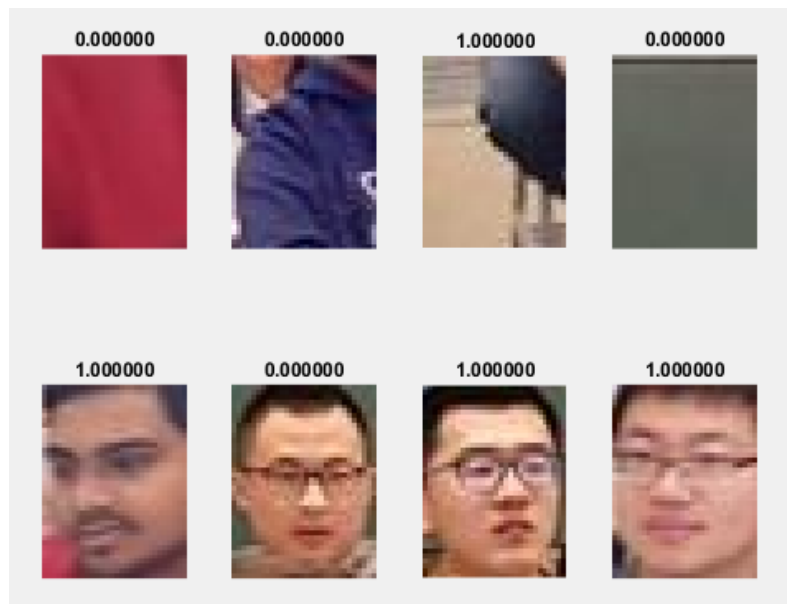
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Kernel Logistic Regression

Miss Detection Rate: 0.040201

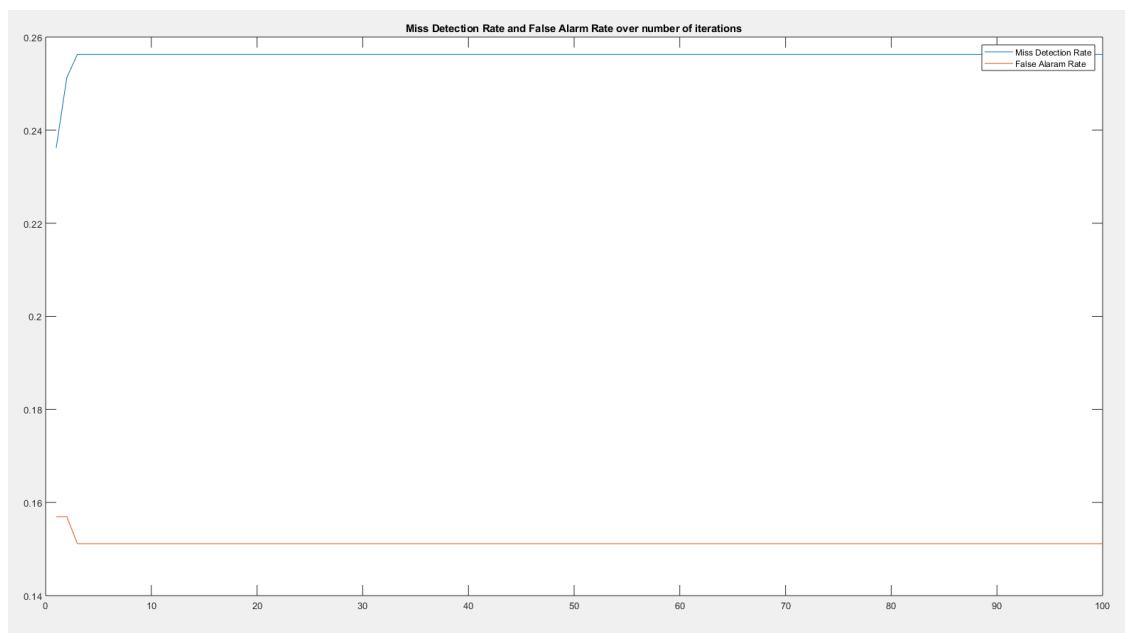
False Alarm Rate: 0.313953



### Relevance Vector Logistic Regression

Miss Detection Rate: 0.256281

False Alarm Rate: 0.151163



**Figure: Miss Detection and False Alarm vs. Iterations**

### Observation:

As the number of iterations increase the miss detection and false alarm values initially start low but later increase and then stabilize. I have tried the last experiment with variable lambda and nu values and I have observed the same pattern in all the cases!