OpenMP

Multithreaded Parallelization for Shared-Memory Machines

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1-Introduction	
1.1 – History	
$1.2 - General \ concepts \ \ldots \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $	
1.3 - OpenMP structure	
$1.4 - OpenMP \text{ versus MPI} \dots 15$	
1.5 - Bibliography	
2 – Principles	
2.1 – General syntax of a directive	
2.2 – Parallel region building	
2.3 - Parallel region extent	
2.4 - Argument-passing case	
$2.5 - Static variables case \dots 28$	
2.6 – The dynamic demory allocation case	
2.7 – The equivalence case	
2.8 – Additions	
3 – Worksharing	
3.1 – Parallel loop	
3.1.1 - SCHEDULE clause	



3.1.2 – An ordered execution case	
3.1.3 – A reduction case	1
3.1.4 - Additions	:
3.2 - Parallel sections	ı
3.2.1 - SECTIONS construct	
3.2.2 - Additions	ı
3.3 - WORKSHARE construct	l
$3.4 - \text{Exclusive execution} \dots \dots$	i
3.4.1 - SINGLE construct)
3.4.2 - MASTER construct	ı
3.5 – Orphaned procedures	ı
3.6 - Summary	ı
4 – Synchronizations	J
4.1 – Barrier	ī
4.2 – Atomic updating	ı
4.3 - Critical regions	Į.
4.4 - Directive FLUSH	
4.5 - Summary	



5-Traps	70
$6 - Performance \dots \dots$	73
$6.1 - Good performance rules \dots \dots \dots \dots \dots \dots \dots \dots$	74
$6.2 - Time measurements \dots \dots$	77
6.3 - Speedup	78
7 - Conclusion	80
8 – Annexes	81

$\Rightarrow ullet$	Introduction	7
	History	
	General concepts	
	OpenMP structure	
	OpenMP versus MPI	
	Bibliography	
•	Principles	19
•	Worksharing	36
•	Synchronizations	60
•	Traps	70
•	Performance	73
•	Conclusion	80
	Annexes	81

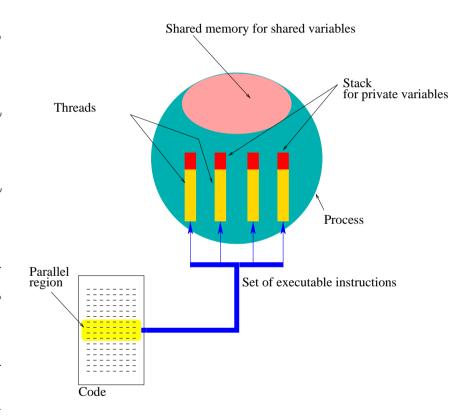
1 – Introduction

1.1 – History

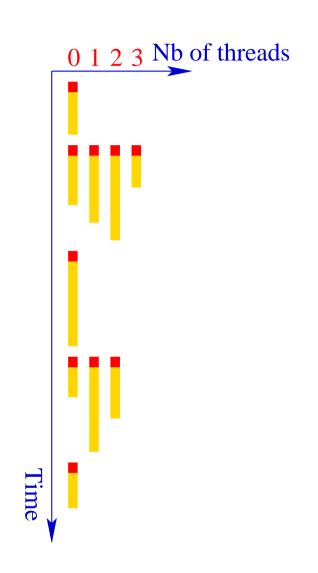
- Directive-based multithreaded parallelization existed for a long time at some constructors (ex. CRAY, NEC, IBM, ...), but each one had its own set of directives.
- The resurgence of shared-memory multiprocessor machines urged to define a standard.
- The standardization attempt of PCF (Parallel Computing Forum) was never adopted by the official authorities of standardization.
- On the 28th of October 1997, a vast majority of industrialists and constructors adopted OpenMP (Open Multi Processing) as an "industrial" standard.
- The specifications of OpenMP now belong to the ARB (Architecture Review Board), the only organization in charge of its development.
- An OpenMP-2 version was finished in November 2000. It brings especially extensions related to the parallelization of some Fortran 95 constructions.
- The latest OpenMP-3 version dates back to May 2008, it introduces basically the concept of tasks (it will be treated in a forthcoming version of this course).

1.2 – General concepts

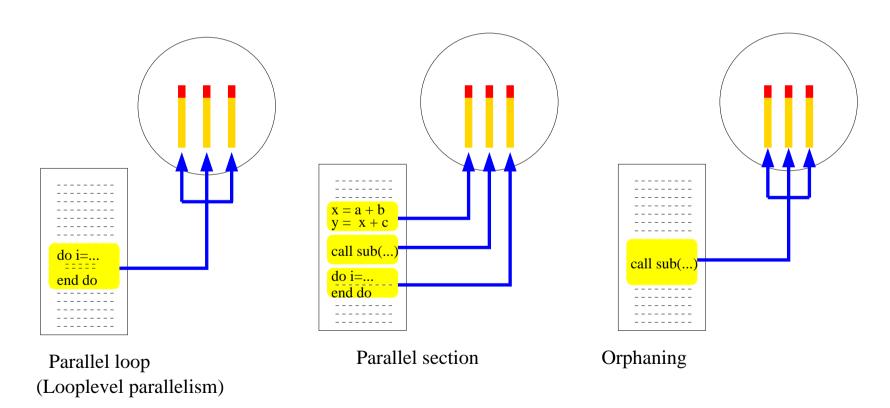
- An OpenMP program is executed by one process.
- This process activates light-weight processes (threads) at the entry of a parallel region.
- Each thread executes a task comprised of a group of instructions.
- During the execution of a task by a thread, a variable can be read and/or updated in memory.
 - It can be defined either in the stack (local memory space) of a thread : we refer to this as a private variable,
 - or in a shared-memory space accessible by all the threads: we refer to this as a shared variable.



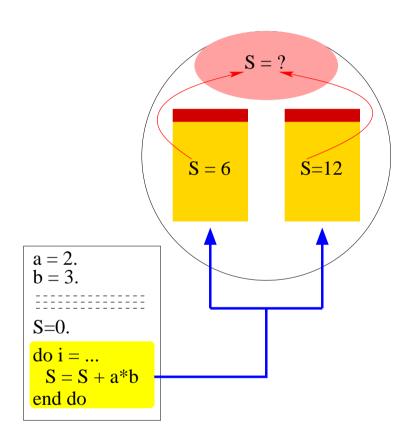
- An OpenMP program is an alternation of sequential regions and parallel regions.
- A sequential region is always executed by the MASTER thread, the one whose rank equals 0.
- A parallel region can be executed by many threads at once.
- Threads can share the work contained in the parallel region.



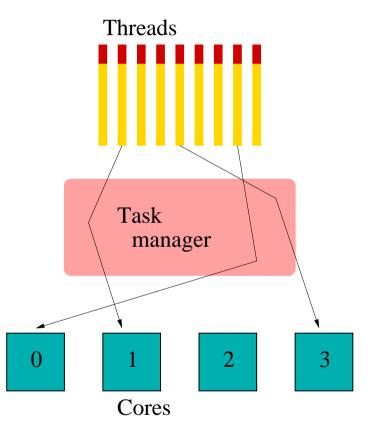
- The work-sharing consists mainly of:
 - ⇒ executing a loop by dividing up iterations between the threads;
 - ⇒ executing many code sections but only one per thread;
 - executing many occurrences of the same procedure by different threads (orphaning).



It is sometimes compulsory to introduce a synchronization between the concurrent threads to avoid, for example, that they update in any order the value of the same shared variable (case of reduction operations).

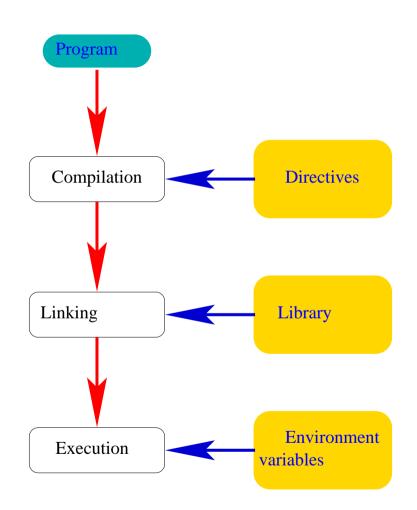


- The threads are mapped onto the execution cores by the operating system. Different cases can occur:
 - at best, at each moment, there is a thread per execution core with as many threads as dedicated execution cores during all the work time;
 - ⇒ at worst, all the threads are processed sequentially by only one execution core;
 - in reality, for operational reasons on a machine whose execution cores are not dedicated, the situation is generally intermediate.



1.3 – OpenMP structure

- Compilation Directives and Clauses:
 - work-sharing, the synchronization and the data-sharing attribute of variables (shared or private);
 - they are considered by the compiler as comment lines unless specifying an appropriate option of compilation in order for them to be interpreted.
- **2** Functions and Routines: they are part of a loaded library at link.
- **3** Environment Variables: once set, their values are taken into account at execution.



Here are the compilation options to force the interpretation of OpenMP directives by some Fortran compilers:

on a IBM machine: -qsmp=omp

```
xlf_r -qsuffix=f=f90 -qnosave -qsmp=omp prog.f90 # Compilation and loading export OMP_NUM_THREADS =4 # Number of threads a.out # Execution
```

on a NEC machine: -Popenmp

```
f90 -Popenmp prog.f90 # Compilation and loading export OMP_NUM_THREADS=4 # Number of threads a.out # Execution
```

on a machine with an Intel compiler: -openmp

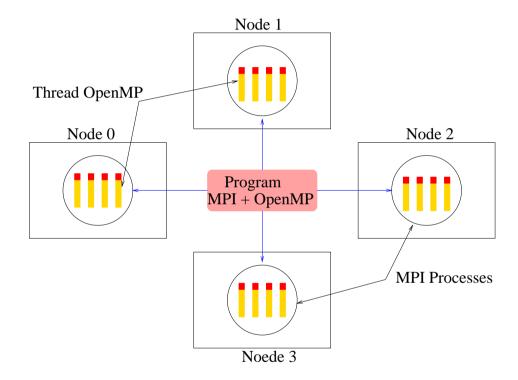
```
ifort -openmp prog.f90 # Compilation and loading export OMP_NUM_THREADS = 4 # Number of threads # Execution
```

1.4 – OpenMP versus MPI

They are two complementary models of parallelization.

- TopenMP, as MPI, has a Fortran, C and C++ interface.
- MPI is a multiprocess model whose communication mode between the processes is explicit (the management of communications is the responsibility of the user).
- © OpenMP is a mutithreaded model whose communication mode between the threads is implicit (the management of communications is the responsibility of the compiler).

- MPI is generally used on distributedmemory multiprocessor machines.
- © OpenMP is used on shared-memory multiprocessor machines.
- On a cluster of independent shared-memory multiprocessor machines (SMP nodes), the implementation of parallelization with both MPI and OpenMP in the same program can be a major advantage for the parallel performances of the code.



1.5 – Bibliography

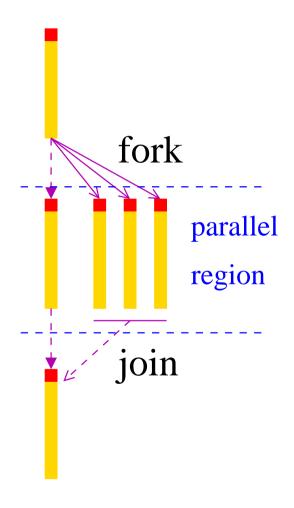
- First book on OpenMP: R. Chandra & al., Parallel Programming in OpenMP, éd. Morgan Kaufmann Publishers, oct. 2000.
- More recent book on OpenMP: B. Chapman & al., Using OpenMP, MIT Press, 2008.
- ▼ Validated 3.0 specifications of the OpenMP standard: http://www.openmp.org/
- Website dedicated to the OpenMP users: http://www.compunity.org/

\sqrt{ullet}	Introduction	7
$\Rightarrow ullet$	Principles	19
	General syntax of a directive	
	Parallel region building	
	Parallel region extent	
	Argument-passing case	
	Static variables case	
	The dynamic demory allocation case	
	The equivalence case	
	Additions	
•	Worksharing	36
•	Synchronizations	60
•	Traps	70
•	Performance	73
•	Conclusion	80
•	Annexes	81



2 – Principles

- It is the responsibilty of the developer to introduce OpenMP directives in its code (at least in the absence of automatic parallelization tools).
- At the program execution, the operating system creates a parallel region on the "fork-join" model.
- At the entry of a parallel region, the Master thread creates/activates (fork) a team of « child » threads which disappear/hibernate at the end of the parallel region (join) while the Master thread alone continues the execution of the program until the entry of the next parallel region.



2.1 – General syntax of a directive

An OpenMP directive has the following general form:

```
sentinel directive-name [clause[ clause]...]
```

- It is a comment line that has to be ignored by the compiler if the option that allows the interpretation of OpenMP directives is not specified.
- The sentinel is a string of characters whose value depends on the used language.
- There is an OMP_LIB Fortran 95 module and a C/C++ omp.h include file which define the prototype of all the OpenMP functions. It is mandatory to include them in each OpenMP program unit that uses any OpenMP functions.

For Fortran, in free format:

```
!$ use OMP_LIB
...
!$OMP PARALLEL PRIVATE(a,b) &
    !$OMP FIRSTPRIVATE(c,d,e)
    ...
!$OMP END PARALLEL! It's a comment
```

For Fortran, in fixed format:

```
!$ use OMP_LIB
...
C$OMP PARALLEL PRIVATE(a,b)
C$OMP1 FIRSTPRIVATE(c,d,e)
...
C$OMP END PARALLEL
```

For C and C++:

```
#include <omp.h>
...
#pragma omp parallel private(a,b) firstprivate(c,d,e)
{ ... }
```

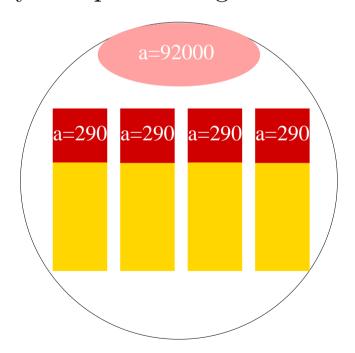
2.2 – Parallel region building

- In a parallel region, by default, the data-sharing attribute of the variables is shared.
- Within a single parallel region, all the concurrent threads execute the same code.
- There is an implicit synchronization barrier at the end of the parallel region.
- A program that branches into or out of a parallel region is non-conforming.

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4
> a.out
```

```
A = 92290.; p = T
```

- It is possible, with the **DEFAULT** clause, to change the default data-sharing attribute of the variables in a parallel region.
- FRIVATE), it will be stored in the stack of each thread. Its value in this case is indeterminate at the entry of a parallel region.



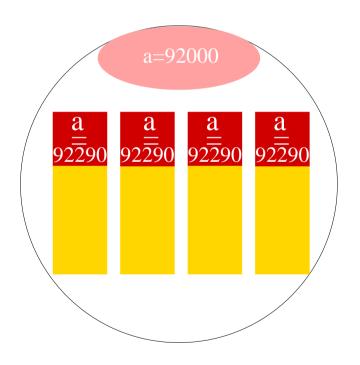
```
program parallel
  implicit none
  real :: a

a = 92000.
  !$OMP PARALLEL DEFAULT(PRIVATE)
  a = a + 290.
    print *,"A = ",a
  !$OMP END PARALLEL
end program parallel
```

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4
> a.out
```

```
A = 290.
A = 290.
A = 290.
A = 290.
```

However, with the **FIRSTPRIVATE** clause, it is possible to force the initialization of this private variable with the last value it had before the entry in the parallel region.



```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4
> a.out
```

```
A = 92290.

A = 92290.

A = 92290.

A = 92290.

Hors region, A = 92000.
```

2.3 – Parallel region extent

- The extent of an OpenMP construct is the range of its influence in the program.
- The influence (or the scope) of a parallel region extends to the code lexically contained in this region (static extent), as well as to the code of the called routines. The union of the two represents "the dynamic extent".

```
program parallel
  implicit none
  !$OMP PARALLEL
    call sub()
  !$OMP END PARALLEL
end program parallel
subroutine sub()
  !$ use OMP_LIB
  implicit none
  logical :: p
  !$ p = OMP_IN_PARALLEL()
  !$ print *,"Parallele ?:", p
end subroutine sub
```

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4;a.out
```

```
Parallele ? : T
Parallele ? : T
Parallele ? : T
Parallele ? : T
```

In a called routine inside a parallel region, the local and automatic variables are implicitly private to each thread (they are stored in the stack of each thread).

```
program parallel
  implicit none
  ! $OMP PARALLEL DEFAULT(SHARED)
    call sub()
  !$OMP END PARALLEL
end program parallel
subroutine sub()
  !$ use OMP_LIB
  implicit none
  integer :: a
  a = 92290
  a = a + OMP_GET_THREAD_NUM()
  print *,"A = ",a
end subroutine sub
```

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4;a.out
```

```
A = 92290
A = 92291
A = 92292
A = 92293
```

2.4 – Argument-passing case

In a called routine, all the dummy arguments passed by reference inherit the data-sharing attribute of the associated actual argument.

```
program parallel
 implicit none
 integer :: a, b
 a = 92000
   $OMP PARALLEL SHARED(a) PRIVATE(b)
    call sub(a, b)
    print *,"B = ",b
 ! $OMP END PARALLEL
end program parallel
subroutine sub(x, y)
 !$ use OMP_LIB
 implicit none
 integer :: x, y
y = x + OMP_GET_THREAD_NUM()
end subroutine sub
```

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4
> a.out
```

```
B = 92002
B = 92003
B = 92001
B = 92000
```

2.5 – Static variables case

- A variable is static if its location in memory is defined at declaration by the compiler.
- The state of the variables that appear in COMMON or contained in a MODULE or declared SAVE or initialized at declaration (ex. PARAMETER, DATA, etc.).
- By default, a static variable is a shared variable.

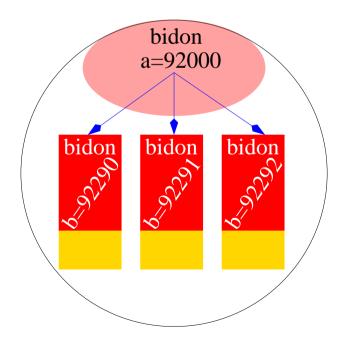
```
module var_stat
  real :: c
end module var_stat
```

```
program parallel
  use var stat
  implicit none
  real :: a
  common /bidon/a
  ! $OMP PARALLEL
    call sub()
  ! $OMP END PARALLEL
end program parallel
subroutine sub()
  use var_stat
  use OMP LIB
  implicit none
  real :: a, b=10.
  integer :: rank
  common /bidon/a
  rank = OMP_GET_THREAD_NUM()
  a=rank; b=rank; c=rank
  !$OMP BARRIER
  print *, "values of A, B and C: ",a,b,c
end subroutine sub
```

```
> xlf_r ... -qsmp=omp var_stat.f90 prog.f90
> export OMP_NUM_THREADS=2;a.out
```

```
values of A, B and C : 0.0 1.0 1.0 values of A, B and C : 0.0 1.0 1.0
```

- The use of the **THREADPRIVATE** directive can privatize a static instance (variables are replicated, each thread having its own copy) and make it persistant from one parallel region to another.
- If, in addition, the **COPYIN** clause is specified then the initial value of the static instance is sent to all the threads.



```
program parallel
 !$ use OMP_LIB
 implicit none
 integer :: a
 common/bidon/a
 ! $OMP THREADPRIVATE(/bidon/)
 a = 92000
 ! $OMP PARALLEL COPYIN(/bidon/)
   a = a + OMP_GET_THREAD_NUM()
   call sub()
 ! $OMP END PARALLEL
print*, "Out of region, A = ",a
end program parallel
subroutine sub()
 implicit none
 integer :: a, b
 common/bidon/a
 ! $OMP THREADPRIVATE(/bidon/)
 b = a + 290
print *,"B = ",b
end subroutine sub
```

```
B = 92290
B = 92291
B = 92292
B = 92293
Out of region, A = 92000
```

2.6 – The dynamic demory allocation case

- The dynamic memory allocation/deallocation operations can be made within a parallel region.
- If the operation involves a private variable, the latter will be local for each thread.
- If the operation involves a shared variable, then it is more wise that only one thread (ex. the master thread) takes the responsibility for this operation.
- Restriction: an allocatable array having the private status must have the " not currently allocated "state at the entry and the exit of the construct, otherwise the behaviour is undefined.

```
program parallel
  !$ use OMP LIB
  implicit none
  integer
                                    :: n,i_start,i_end,rank,nb_threads,i
  real, allocatable, dimension(:) :: a
  n=1024; nb threads=4
  allocate(a(n*nb_threads))
   ! $OMP PARALLEL DEFAULT(NONE) PRIVATE(i_start,i_end,rank,i) &
        ! $OMP SHARED(a,n) IF(n .gt. 512)
     rank=OMP GET THREAD NUM()
     i start=rank*n+1
     i end=(rank+1)*n
     do i = i_start, i_end
        a(i) = 92290. + real(i)
     end do
     print *, "Rank : ", rank, "; A(", i_start, "), ..., A(", i_end, ") : ", a(i_start), ", ..., ", a(i_
  ! $OMP END PARALLEL
  deallocate(a)
end program parallel
```

```
Rank: 3; A(3073), ..., A(4096): 95363., ..., 96386.
Rank: 2; A(2049), ..., A(3072): 94339., ..., 95362.
Rank: 1; A(1025), ..., A(2048): 93315., ..., 94338.
Rank: 0; A(1), ..., A(1024): 92291., ..., 93314.
```

2.7 – The equivalence case

- The original of the same data-sharing attribute can be put into equivalence.
- If not, the result is undefined.
- These remarks remain valid in the case of an association between variables by POINTER.

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4;a.out
```

```
B = -0.3811332074E+30
B = 0.0000000000E+00
B = -0.3811332074E+30
B = 0.0000000000E+00
```

2.8 – Additions

- The construct of a parallel region allows two other clauses:

 - NUM_THREADS: it can be used to specify the required number of threads at the entry of a parallel region in the same way as a call to OMP_SET_NUM_THREADS routine would do.
- From one parallel region to another, the number of concurrent threads can change if we wish. In order to do this, just use the OMPLSET_DYNAMIC routine or set the OMPLDYNAMIC environment variable to true.

```
program parallel
  implicit none

!$OMP PARALLEL NUM_THREADS(2)
    print *,"Hello !"
!$OMP END PARALLEL

!$OMP PARALLEL NUM_THREADS(3)
    print *,"Hi !"
!$OMP END PARALLEL
end program parallel
```

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4;
> export OMP_DYNAMIC=true; a.out
```

```
Hello !
Hello !
Hi !
Hi !
Hi !
```

Nested parallel regions are possible, but this has no effect unless this mode has been activated by a call to the OMP_SET_NESTED routine or by setting the OMP_NESTED environment variable to true.

```
> xlf_r ... -qsmp=nested_par prog.f90
> export OMP_DYNAMIC=true
> export OMP_NESTED=true; a.out
```

```
My rank in region 1 : 0

My rank in region 2 : 1

My rank in region 2 : 0

My rank in region 2 : 1

My rank in region 2 : 0

My rank in region 1 : 1

My rank in region 2 : 0

My rank in region 2 : 0

My rank in region 2 : 1
```

\sqrt{ullet}	Introduction	7
\sqrt{ullet}	Principles	19
$\Rightarrow ullet$	Worksharing	36
	Parallel loop	
	Parallel sections	
	WORKSHARE construct	
	Exclusive execution	
	Orphaned procedures	
	Summary	
•	Synchronizations	60
•	Traps	70
•	Performance	73
•	Conclusion	80
	Anneyes	81

3 – Worksharing

- In principle, the parallel region construct and the use of some OpenMP routines are enough alone to parallelize a code portion.
- But it is, in this case, the responsibility of the programmer to distribute both the work and the data and to manage the synchronization of threads.
- Fortunately, OpenMP proposes three directives (DO, SECTIONS and WORKSHARE) which make it easily possible to control finely the work and data distribution simultaneously with the synchronization within a parallel region.
- In addition, there are other OpenMP constructs which enable the exclusion of all the threads except for one thread in order to execute a code portion located in a parallel region.

3.1 – Parallel loop

- A parallel loop is a loop for which all iterations are independent of each other.
- Tt's a parallelism by distribution of loop iterations.
- The parallelized loop is the one which comes immediately after the **DO** directive.
- The "infinite" loops and do while are not parallelizable with OpenMP.
- The distribution mode of the iterations can be specified with the **SCHEDULE** clause.
- The choice of the distribution mode allows a better control of the load-balancing between the threads.
- The loop indices are private integer variables.
- By default, a global synchronization is done at the end of a **END DO** construct unless the **NOWATT** clause is specified.
- It is possible to introduce as many DO constructs as we want (one after another) in a parallel region.

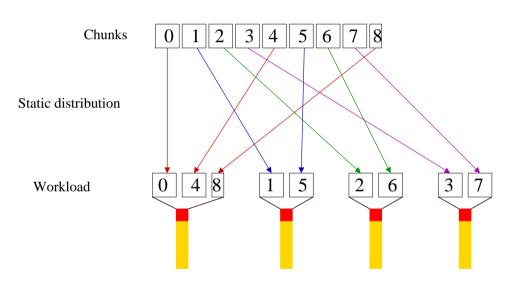
3.1.1 – SCHEDULE clause

```
program parallel
 !$ use OMP LIB
 implicit none
 integer, parameter :: n=4096
 real, dimension(n) :: a
         :: i, i_min, i_max, rank, nb_threads
 integer
 ! $OMP PARALLEL PRIVATE(rank,nb_threads,i_min,i_max)
  rank=OMP_GET_THREAD_NUM(); nb_threads=OMP_GET_NUM_THREADS(); i_min=n; i_max=0
   ! $0MP DO SCHEDULE(STATIC,n/nb_threads)
     do i = 1. n
       a(i) = 92290. + real(i) ; i_min=min(i_min,i) ; i_max=max(i_max,i)
     end do
   ! SOMP END DO NOWAIT
  print *,"Rank : ",rank,"; i_min :",i_min,"; i_max :",i_max
 ! $OMP END PARALLEL
end program parallel
```

```
> xlf_r ... -qsmp=omp prog.f90 ; export OMP_NUM_THREADS=4 ; a.out
```

```
Rank: 1; i_min: 1025; i_max: 2048
Rank: 3; i_min: 3073; i_max: 4096
Rank: 0; i_min: 1; i_max: 1024
Rank: 2; i_min: 2049; i_max: 3072
```

The **STATIC** distribution consists of dividing the iterations into chunks according to a given size (except perhaps for the last one). The chunks are then assigned to the threads in a round-robin fashion, in the order of the thread number.



- We could have postponed the scheduling of iteration distribution at runtime by using the **OMP_SCHEDULE** environment variable.
- The scheduling of loop iteration distribution can be a major contribution for the load-balancing on a machine whose processors are not dedicated.
- Fig. It is important to mention that for performance reasons, parallelizing the loops referring to the first dimension of a multi-dimensional array has to be avoided in Fortran.

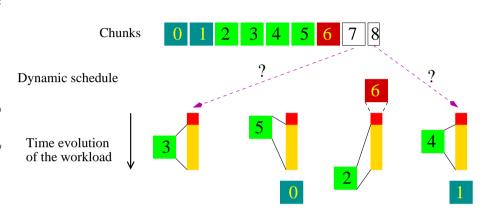
```
program parallel
 !$ use OMP LIB
 implicit none
 integer, parameter :: n=4096
 real, dimension(n) :: a
 integer :: i, i_min, i_max
 ! $OMP PARALLEL DEFAULT(PRIVATE)
                              SHARED(a)
  i_min=n ; i_max=0
   ! $OMP DO SCHEDULE(RUNTIME)
     do i = 1, n
       a(i) = 92290. + real(i)
       i_min=min(i_min,i)
       i_max=max(i_max,i)
     end do
  !$OMP END DO
  ! $OMP END PARALLEL
end program parallel
```

```
> export OMP_NUM_THREADS = 2
> export OMP_SCHEDULE = "STATIC, 1024"
> a.out
```

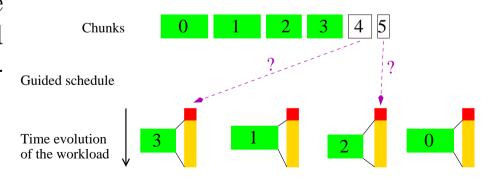
```
Rank: 0 ; i_min: 1 ; i_max: 3072
Rank: 1 ; i_min: 1025 ; i_max: 4096
```

- In addition to the **STATIC** schedule, there are two other ways to distribute the loop iterations:
 - DYNAMIC: the iterations are divided into chunks according to a given size. Once a thread completes its chunk of iterations, another chunk is assigned to it;
 - chunks whose size decreases exponentially. All the chunks have a size superior or equal to a given value except for the last one whose size can be inferior. Once a thread finishes its chunk, another chunk of iterations is assigned to it.

> export OMP_SCHEDULE = "DYNAMIC, 480"
> export OMP_NUM_THREADS = 4 ; a.out



> export OMP_SCHEDULE="GUIDED,256"
> export OMP_NUM_THREADS=4; a.out



3.1.2 – An ordered execution case

- It is sometimes useful (when debugging) to execute a loop in an orderly way.
- The order of iterations will be then identical to the one occurring during a sequential execution.

```
program parallel
 !$ use OMP_LIB
 implicit none
 integer, parameter :: n=9
 integer
                     :: i,rank
 ! $OMP PARALLEL DEFAULT(PRIVATE)
   rank = OMP_GET_THREAD_NUM()
   ! $OMP DO SCHEDULE(RUNTIME) ORDERED
     do i = 1, n
      !$OMP ORDERED
        print *,"Rank :",rank,"; iteration :",i
      ! $OMP END ORDERED
     end do
   ! $OMP END DO NOWAIT
 ! $OMP END PARALLEL
end program parallel
```

```
> export OMP_SCHEDULE="STATIC,2"
> export OMP_NUM_THREADS=4; a.out
```

```
Rank:
          : iteration :
Rank:
         : iteration :
Rank:
          : iteration :
Rank:
         : iteration :
Rank:
       2 ; iteration :
       2 ; iteration :
Rank:
       3 : iteration :
Rank:
Rank:
       3 : iteration :
         : iteration :
Rank:
```

3.1.3 – A reduction case

- A reduction is an associative operation applied to a shared variable.
- The operation can be:
 - \Rightarrow arithmetic: +, -, \times ;
 - ⇒ logical: .AND., .OR., .EQV., .NEQV.;
 - ⇒ an intrinsic function : MAX, MIN, IAND, IOR, IEOR.
- Each thread computes a partial result independently of the others. They are then synchronized in order to update the final result.

```
> export OMP_NUM_THREADS=4
> a.out
```

```
s = 5; p = 32; r = 243
```

3.1.4 - Additions

- The other clauses of the **DO** directive are:
 - PRIVATE: to assign a private data-sharing attribute to a variable;
 - FIRSTPRIVATE: privatizes a shared variable in the extent of the DO construct and assigns to it the last affected value before the entry of the loop;
 - riable in the extent of the DO construct and allows to return, at the exit of this construct, the value computed by the thread executing the last loop iteration.

```
program parallel
 !$ use OMP LIB
 implicit none
 integer, parameter :: n=9
 integer
                     :: i, rank
 real
                     :: res
 ! $OMP PARALLEL PRIVATE(rank)
   ! $OMP DO LASTPRIVATE(res)
      do i = 1, n
        res = real(i)
      end do
   !$OMP END DO
   rank=OMP GET THREAD NUM()
   print *,"Rank:",rank,";res=",res
 ! $OMP END PARALLEL
end program parallel
```

```
> export OMP_NUM_THREADS=4 ; a.out
```

```
Rank: 2; res= 9.0
Rank: 3; res= 9.0
Rank: 1; res= 9.0
Rank: 0; res= 9.0
```

- The PARALLEL DO directive is a combination of the PARALLEL and DO directives with the union of their respective clauses.
- The termination directive END PARALLEL DO includes a global synchronization barrier and cannot admit the NOWAIT clause.

3.2 – Parallel sections

- The **SECTIONS** construct is a worksharing construct that contains a set of structured blocks that are to be distributed among and executed by the threads. Each structured block is executed once by one of the threads in the team.
- Several structured blocks can be defined by the user by using the **SECTION** directive within a **SECTIONS** construct.
- The goal is to be able to distribute the execution of many independent code portions (structured blocks) on different threads.
- The **NOWAIT** clause is allowed at the end of the **END SECTIONS** construct to remove the implicit synchronization barrier.

3.2.1 – SECTIONS construct

```
program parallel
 implicit none
 integer, parameter
                      :: n=513, m=4097
 real, dimension(m,n) :: a, b
 real, dimension(m)
                      :: coord x
 real, dimension(n)
                      :: coord_y
 real
                      :: step_x, step_y
                      :: i
 integer
 ! $OMP PARALLEL
  !$OMP SECTIONS
   ! $OMP SECTION
   call read_initial_x(a)
   !$OMP SECTION
   call read_initial_y(b)
   ! $OMP SECTION
   step_x = 1./real(m-1)
   step_y = 2./real(n-1)
   coord_x(:) = (/ (real(i-1)*step_x,i=1,m) /)
   coord_y(:) = (/ (real(i-1)*step_y,i=1,n) /)
  ! $OMP END SECTIONS NOWAIT
 ! $OMP END PARALLEL
end program parallel
```

```
subroutine read_initial_x(x)
implicit none
integer, parameter :: n=513, m=4097
real, dimension(m,n) :: x

call random_number(x)
end subroutine read_initial_x

subroutine read_initial_y(y)
implicit none
integer, parameter :: n=513, m=4097
real, dimension(m,n) :: y

call random_number(y)
end subroutine read_initial_y
```

3.2.2 - Additions

- All the **SECTION** directives have to appear in the lexical extent of the **SECTIONS** construct.
- The clauses allowed for the **SECTIONS** construct are the ones which we already know:
 - **PRIVATE**;
 - ►→ FIRSTPRIVATE;
 - □→ LASTPRIVATE;
 - **P**→ REDUCTION.
- The **PARALLEL SECTIONS** directive is a combination of **PARALLEL** and **SECTIONS** directives with the union of their respective clauses.
- The termination directive **END PARALLEL SECTIONS** includes a global synchronization barrier and cannot admit the **NOWAIT** clause.

3.3 – WORKSHARE construct

- The WORKSHARE construct divides the execution of the enclosed structured block into separate units of work, each one being executed only once by one thread.
- Tt can only be specified within a parallel region.
- It is useful to distribute the work of Fortran 95 constructs such as:
 - → array and scalar assignments;
 - ►→ FORALL and WHERE constructs;
 - ► transformational array intrinsic functions : MATMUL, DOT_PRODUCT, SUM, PRODUCT, MAXVAL, MINVAL, COUNT, ANY, ALL, SPREAD, PACK, UNPACK, RESHAPE, TRANSPOSE, EOSHIFT, CSHIFT, MINLOC and MAXLOC;
 - ⇒ user-defined functions called "ELEMENTAL".
- It admits only the **NOWAIT** clause at the end of the construct (**END WORKSHARE**).

- Only the instructions or Fortran 95 blocks specified in the lexical extent will have their work distributed among the threads.
- The work unit is the element of an array. There is no other way to change this default behavior.
- The additional costs caused by such a work distribution can be significant.

```
program parallel
 implicit none
 integer, parameter :: m=4097, n=513
 integer
                       :: i, j
 real, dimension(m,n) :: a, b
 call random number(b)
 a(:,:) = 1.
 ! $OMP PARALLEL
   !$OMP DO
     do j=1,n
       do i=1,m
          b(i,j) = b(i,j) - 0.5
       end do
     end do
   !$OMP END DO
   ! $OMP WORKSHARE
     WHERE(b(:,:) >= 0.) a(:,:)=sqrt(b(:,:))
     $OMP END WORKSHARE NOWAIT
 ! $OMP END PARALLEL
end program parallel
```

The PARALLEL WORKSHARE construct is a combination of PARALLEL and WORKSHARE constructs with the union of their clauses and their respective constraints, with the exception of the NOWATT clause at the end of the construct.

```
program parallel
  implicit none
  integer, parameter :: m=4097, n=513
  real, dimension(m,n) :: a, b

call random_number(b)
  !$OMP PARALLEL WORKSHARE
  a(:,:) = 1.
  b(:,:) = b(:,:) - 0.5
  WHERE(b(:,:) >= 0.) a(:,:)=sqrt(b(:,:))
  !$OMP END PARALLEL WORKSHARE
end program parallel
```

3.4 – Exclusive execution

- Sometimes, in a parallel region, we want to execute some code portions excluding all the threads except one.
- In order to do this, OpenMP offers two directives **SINGLE** and **MASTER**.
- Although the purpose is the same, the behavior induced by these two constructs remains basically different.

3.4.1 – SINGLE construct

- The **SINGLE** construct makes it possible to execute a code portion by one and only one thread without being able to specify which one.
- In general, it is the thread which comes first on the **SINGLE** construct, but this is not specified in the standard.
- All the threads that do not execute the **SINGLE** region wait, at the end of the construct (**END SINGLE**), for the termination of the one which is in charge of the work, unless a **NOWAIT** clause is specified.

```
program parallel
!$ use OMP_LIB
implicit none
integer :: rank
real :: a

!$OMP PARALLEL DEFAULT(PRIVATE)
a = 92290.

!$OMP SINGLE
a = -92290.
!$OMP END SINGLE

rank = OMP_GET_THREAD_NUM()
print *,"Rank :",rank,"; A = ",a
!$OMP END PARALLEL
end program parallel
```

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS = 4 ; a.out
```

```
Rank: 1; A = 92290.

Rank: 2; A = 92290.

Rank: 0; A = 92290.

Rank: 3; = -92290.
```

- An additional clause allowed only by the END SINGLE termination directive is the COPYPRIVATE clause.
- It allows the thread responsible for the **SINGLE** region to distribute to other threads the value of a list of private variables before leaving this region.
- The other clauses of the **SINGLE** construct are **PRIVATE** and **FIRSTPRIVATE**.

```
program parallel
!$ use OMP_LIB
implicit none
integer :: rank
real :: a

!$OMP PARALLEL DEFAULT(PRIVATE)
a = 92290.

!$OMP SINGLE
a = -92290.
!$OMP END SINGLE COPYPRIVATE(a)

rank = OMP_GET_THREAD_NUM()
print *,"Rank :",rank,"; A = ",a
!$OMP END PARALLEL
end program parallel
```

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4 ; a.out
```

```
Rank : 1 ; A = -92290.

Rank : 2 ; A = -92290.

Rank : 0 ; A = -92290.

Rank : 3 ; A = -92290.
```

3.4.2 - MASTER construct

- The MASTER construct enables to execute a code portion by the master thread alone.
- This construct does allow any clause.
- There is no synchronization barrier neither at the start (MASTER) nor at the end of the construct (END MASTER).

```
program parallel
!$ use OMP_LIB
implicit none
integer :: rank
real :: a

!$OMP PARALLEL DEFAULT(PRIVATE)
a = 92290.

!$OMP MASTER
a = -92290.
!$OMP END MASTER

rank = OMP_GET_THREAD_NUM()
print *,"Rank :",rank,"; A =",a
!$OMP END PARALLEL
end program parallel
```

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4 ; a.out
```

```
Rank: 0; A = -92290.
Rank: 3; A = 92290.
Rank: 2; A = 92290.
Rank: 1; A = 92290.
```

3.5 – Orphaned procedures

- A procedure (function or routine) called in a parallel region is executed by all the threads.
- In general, there is no interest unless the work of the procedure is distributed.
- This requires the introduction of OpenMP (DO, SECTIONS, etc.) directives in the body of the procedure if it is called in a parallel region.
- These directives are called "orphans" and, by excess of language, they are referred to as orphaned procedures (orphaning).
- A multi-threaded scientific library parallelized with OpenMP will be constituted of a set of orphaned procedures.

```
> ls
> mat_vect.f90 prod_mat_vect.f90
```

```
program mat_vect
implicit none
integer,parameter :: n=1025
real,dimension(n,n) :: a
real,dimension(n) :: x, y
call random_number(a)
call random_number(x) ; y(:)=0.
! $OMP PARALLEL IF(n.gt.256)
call prod_mat_vect(a,x,y,n)
! $OMP END PARALLEL
end program mat_vect
```

```
subroutine prod_mat_vect(a,x,y,n)
implicit none
integer,intent(in) :: n
real,intent(in),dimension(n,n) :: a
real,intent(in),dimension(n) :: x
real,intent(out),dimension(n) :: y
integer :: i
!$OMP DO
do i = 1, n
    y(i) = SUM(a(i,:) * x(:))
end do
!$OMP END DO
end subroutine prod_mat_vect
```

- Attention, because there are three execution contexts according to the compilation mode of the calling and called program units:
 - At compilation, the **PARALLEL** directive of the calling unit is interpreted (the execution can be **Parallel**) as well as the directives of the called unit (the work can be **D**istributed);
 - At compilation, the **PARALLEL** directive of the calling unit is interpreted (the execution can be Parallel) but not the directives contained in the called unit (the work is Replicated);
 - At compilation, the **PARALLEL** directive of the calling unit is not interpreted. The execution is everywhere Sequential, even if the contained directives in the called unit have been interpreted at compilation.

compiled called unit		without -qsmp=omp
with -qsmp=omp	P + D	P + R
without -qsmp=omp	S	S

Tab. 1 – Execution context according to the compilation mode (example with IBM) Fortran compiler options

3.6 – Summary

	default	shared	private	firstprivate	lastprivate	copyprivate	if	reduction	schedule	ordered	copyin	nowait
parallel	✓	√	√	✓			√	✓			✓	
do			√	✓	✓			√	√	√		√
sections			√	✓	✓			✓				√
workshare												√
single			√	✓		✓						√
master												
threadprivate												

\sqrt{ullet}	Introduction	7
\sqrt{ullet}	Principles	19
\sqrt{ullet}	Worksharing	36
$\Rightarrow ullet$	Synchronizations	60
	Barrier	
	Atomic updating	
	Critical regions	
	Directive FLUSH	
	Summary	
•	Traps	70
•	Performance	73
•	Conclusion	80
	Anneyes	81

4 – Synchronizations

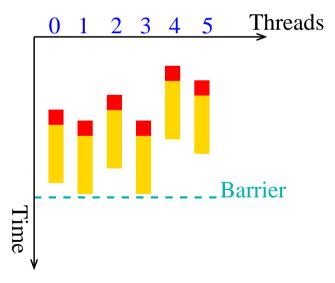
The synchronization becomes necessary in the following situations:

- to make sure that all the concurrent threads have reached the same instruction point in the program (global barrier);
- 2 to order the execution of all the concurrent threads, when these have to execute the same code portion affecting one or many shared variables, whose coherence in memory (read or write) has to be guaranteed (mutual exclusion).
- 3 to synchronize at least two concurrent threads among the others (lock mechanism).

- As we have already indicated, the absence of **NOWATT** clause means that a global synchronization barrier is implicitly applied at the end of some **OpenMP** constructs. However, it is possible to impose explicitly a global synchronization barrier through the **BARRIER** directive.
- The mutual exclusion mechanism (one thread at a time) is found, for example, in the reduction operations (REDUCTION clause) or in the ordered loop execution (ORDERED clause). This mechanism is also implemented in the ATOMIC and CRITICAL directives.
- Finer synchronizations can also be done either by the implementation of lock mechanisms (this requires the call of OpenMP library routines), or by the use of the FLUSH directive.

4.1 – Barrier

- The **BARRIER** directive synchronizes all the concurrent threads within a parallel region.
- Each thread wait until all the other threads reach this point of synchronization in order to continue, together, the program execution.



```
program parallel
 implicit none
 real, allocatable, dimension(:) :: a, b
 integer
                                 :: n, i
n = 5
 ! $OMP PARALLEL
  !$OMP SINGLE
    allocate(a(n),b(n))
  ! $OMP END SINGLE
  !$OMP MASTER
    read(9) a(1:n)
  ! $OMP END MASTER
  !$OMP BARRIER
    $OMP DO SCHEDULE(STATIC)
    do i = 1, n
      b(i) = 2.*a(i)
    end do
   SOMP SINGLE
    deallocate(a)
   $OMP END SINGLE NOWAIT
 ! $OMP END PARALLEL
 print *, "B = ", b(1:n)
end program parallel
```

4.2 – Atomic updating

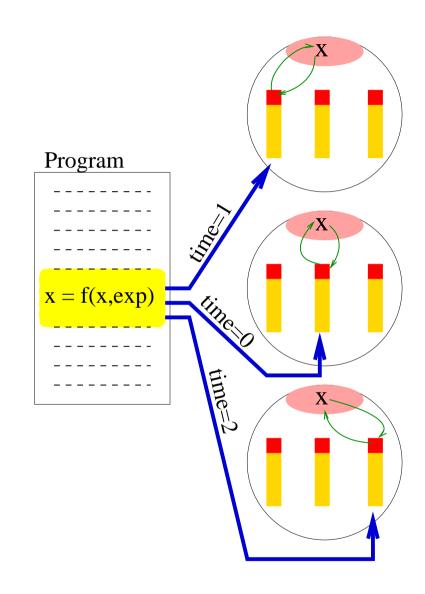
- The ATOMIC update ensures that a shared variable is read and modified in memory by one and only one thread at a time.
- It has a local effect on the instruction which immediately follows the directive.

```
Rank: 1; counter = 92291
Rank: 0; counter = 92292
Rank: 2; counter = 92293
Rank: 3; counter = 92294
In total, counter = 92294
```

The instruction must have one of the following forms:

```
>→ x=x (op) exp;
>→ x=exp (op) x;
>→ x=f(x,exp);
>→ x=f(exp,x).
```

- (op) represents one of the following
 operations:+, -, ×, /, .AND., .OR.,
 .EQV., .NEQV..
- f represents one of the following intrinsic functions: MAX, MIN, IAND, IOR, IEOR.
- exp is any arithmetic expression independent of x.



4.3 – Critical regions

- A critical region can be seen as a generalization of the ATOMIC directive, although the underlying mechanisms are distinct.
- The threads execute this region in a non-deterministic order, but only one at a time.
- A critical structured block (region) is defined through the **CRITICAL** directive and applies to a code portion terminated by **END CRITICAL**.
- Tts extent is dynamic.
- For performance reasons, it is not recommended to emulate an atomic instruction by a critical construct.
- An optional name can be used to name a critical construct.
- All the non-explicitly named critical constructs are considered as having the same non-specified name.
- If many critical constructs have the same name, they are considered for the mutual exclusion mechanism as a the same and unique critical construct.

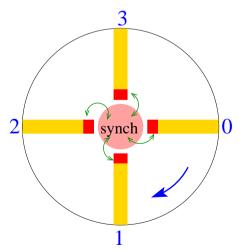
```
program parallel
  implicit none
  integer :: s, p
  s=0
  p=1
  !$OMP PARALLEL
    !$OMP CRITICAL
      s = s + 1
    ! $OMP END CRITICAL
     $OMP CRITICAL (RC1)
      p = p * 2
     $OMP END CRITICAL (RC1)
    !$OMP CRITICAL
      s = s + 1
    ! $OMP END CRITICAL
  ! $OMP END PARALLEL
  print *, "s= ",s, " ; p= ",p
end program parallel
```

```
> xlf_r ... -qsmp=omp prog.f90
> export OMP_NUM_THREADS=4 ; a.out
```

```
s= 8 ; p= 16
```

4.4 – Directive FLUSH

- It is useful in a parallel region to refresh the value of a shared variable in global memory.
- It is especially more useful if the memory hierarchy of a machine has multiple levels of caches.
- It can be used to establish a mechanism of synchronization between two threads.



```
program ring
 !$ use OMP LIB
 implicit none
 integer :: rank,nb_threads,synch=0
 ! $OMP PARALLEL PRIVATE(rank,nb_threads)
   rank=OMP GET THREAD NUM()
   nb_threads=OMP_GET_NUM_THREADS()
   if (rank == 0) then; do
       ! $OMP FLUSH(synch)
       if(synch == nb_threads-1) exit
     end do
   else ; do
       !$OMP FLUSH(synch)
       if(synch == rank-1) exit
     end do
   end if
   print *,"Rank:",rank,";synch:",synch
   synch=rank
   ! $OMP FLUSH(synch)
 ! $OMP END PARALLEL
end program ring
```

```
Rank: 1; synch: 0
Rank: 2; synch: 1
Rank: 3; synch: 2
Rank: 0; synch: 3
```

4.5 – Summary

	default	shared	private	firstprivate	lastprivate	copyprivate	if	reduction	schedule	ordered	copyin	nowait
parallel	√	✓	√	✓			√	✓			√	
do			1	√	✓			√	✓	√		√
sections			1	√	✓			√				√
workshare												√
single			√	✓		✓						√
master												
threadprivate												
atomic												
critical												
flush												

$\sqrt{\bullet}$	Introduction	7
$\sqrt{\bullet}$	Principles	19
$\sqrt{\bullet}$	Worksharing	36
$\sqrt{\bullet}$	Synchronizations	60
$\Rightarrow ullet$	Traps	70
•	Performance	73
•	Conclusion	80
•	Annexes	81

5 – Traps

In the first example shown here, the data-sharing attribute of the variable "s" is incorrect, which produces an indeterminate result. In fact, the data-sharing attribute of "s" has to be **SHARED** in the lexical extent of the parallel region if the LASTPRIVATE clause is specified in the DO directive (it is not the only clause in that case). Here, the two implementations, IBM and NEC, provide two different results. However, neither one of them is in contradiction with the standard, whereas one of the results is correct.

```
IBM SP> export OMP_NUM_THREADS = 3; a.out
s=92290.; a(9)=92290.
s=0.; a(9)=92290.
s=0.; a(9)=92290.
```

```
NEC SX-5> export OMP_NUM_THREADS=3;a.out s=92290.; a(9)=92290. s=92290.; a(9)=92290. s=92290.; a(9)=92290.
```

In the second example shown here, there is a data race between the threads. The "print" instruction does not print the the expected result of the variable "s" whose data-sharing attribute is SHARED. It turns out here that NEC and IBM provide identical results but it is possible and legitimate to obtain a different result on other platforms. One solution is to add, for example, a BARRIER directive just after the "print" instruction.

```
program false_2
implicit none
real :: s
!$OMP PARALLEL DEFAULT(NONE) &
    !$OMP SHARED(s)
!$OMP SINGLE
    s=1.
!$OMP END SINGLE
print *,"s = ",s
    s=2.
!$OMP END PARALLEL
end program faulse_2
```

```
IBM SP> export OMP_NUM_THREADS=3;a.out s = 1.0 s = 2.0 s = 2.0
```

```
NEC SX-5> export OMP_NUM_THREADS = 3; a.out
s = 1.0
s = 2.0
s = 2.0
```

\sqrt{ullet}	Introduction	7
\sqrt{ullet}	Principles	19
\sqrt{ullet}	Worksharing	36
\sqrt{ullet}	Synchronizations	60
\sqrt{ullet}	Traps	70
$\Rightarrow ullet$	Performance	73
•	Speedup Conclusion	80 81

6 – Performance

- In general, the performances depend on the architecture (processors, networks and memory) of the machine and on the OpenMP implementation.
- Nevertheless, there are some rules of "good performances" which are independent of the architecture.
- In the optimization phase with OpenMP, the goal is to reduce the elapsed time of the code and to estimate its speedup relative to a sequential execution.

6.1 – Good performance rules

- Minimize the number of parallel regions in the code.
- Adjust the number of threads to the size of the problem in order to minimize the additional costs of thread management by the system.
- Whenever possible, parallelize the outermost loop.
- Use the **SCHEDULE (RUNTIME)** clause in order to be able to dynamically change the scheduling and the size of the chunk of a parallel loop.
- The **SINGLE** directive and the **NOWAIT** clause can help to decrease the elapsed time at the expense, very often, of an explicit synchronization.
- The ATOMIC directive and the REDUCTION clause are more restrictive, but by far more efficient than the CRITICAL directive.

- Use the IF clause to do a conditionial parallelization (ex. do not parallelize a loop unless its length is sufficiently large).
- Avoid parallelizing the loop which refers to the first dimension of arrays (in Fortran) because it is the one which refers to contiguous elements in memory.

```
program parallel
 implicit none
 integer, parameter
                       :: n=1025
 real, dimension(n,n) :: a, b
 integer
                       :: i, j
 call random number(a)
! $OMP PARALLEL DO SCHEDULE(RUNTIME)&
      !$OMP IF(n.gt.514)
   do i = 2, n-1
     doi = 1, n
        b(i,j) = a(i,j+1) - a(i,j-1)
     end do
   end do
! $OMP END PARALLEL DO
end program parallel
```

- The conflicts between threads can lead to "false sharing" (explosion of cache-misses), which may significantly degrade the performances.
- On a NUMA (Non Uniform Memory Access) machine (ex. SGI-02000), local memory references are faster than non-local references, leading to different behaviours depending on how data are mapped on memory by the system.
- Regardless of the architecture of machines, the quality of the OpenMP implementation can quite significantly affect the scalability of parallel loops and the overall performance.

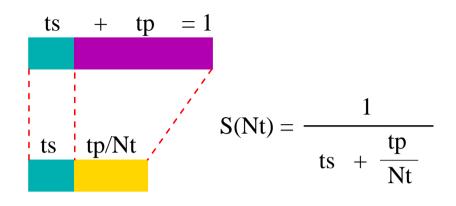
6.2 – Time measurements

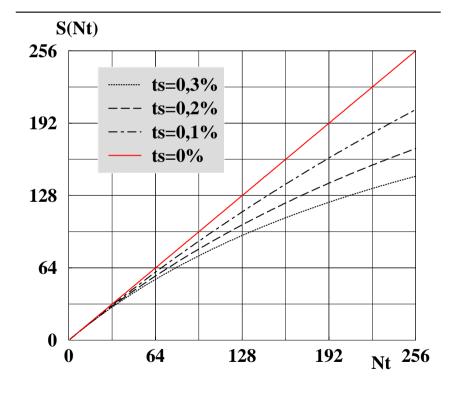
- TopenMP provides two functions:
 - DMP_GET_WTIME in order to measure the elapsed time in seconds;
 - DMP_GET_WTICK in order to get the precision of measurements in seconds.
- What we measure is the elapsed time from an arbitrary reference point of the code.
- This measure can vary from one execution to another according to the machine workload and the distribution of threads on the cores.

```
program mat_vect
 !$ use OMP_LIB
 implicit none
 integer, parameter
                     :: n=1025
 real, dimension(n,n) :: a
 real, dimension(n)
                     :: x, y
 real(kind=8) :: t_ref, t_final
 integer :: rank
 call random number(a)
 call random_number(x) ; y(:)=0.
 !$OMP PARALLEL &
  ! $OMP PRIVATE(rank,t_ref,t_final)
  rank = OMP_GET_THREAD_NUM()
  t_ref=OMP_GET_WTIME()
  call prod_mat_vect(a,x,y,n)
  t_final=OMP_GET_WTIME()
  print *,"Rank :",rank, &
          "; res :",t_final-t_ref
 ! $OMP END PARALLEL
end program mat_vect
```

6.3 – Speedup

- The gain in performance of a parallel code is estimated compared to a sequential execution.
- The ratio between the sequential time T_s and the parallel time T_p on a dedicated machine is already a good indicator of the performance gain. It defines the speedup $S(N_t)$ of the code which depends on the number of threads N_t .
- If we consider $T_s = t_s + t_p = 1$ (t_s represents the relative time of the sequential part and t_p the relative time of the parallelizable part of the code), the "AMDHAL" law $S(N_t) = \frac{1}{t_s + \frac{t_p}{N_t}}$ indicates that $S(N_t)$ is limited by the sequential fraction $\frac{1}{t_s}$ of the program.





\sqrt{ullet}	Introduction	7
\sqrt{ullet}	Principles	19
$\sqrt{\bullet}$	Worksharing	36
$\sqrt{\bullet}$	Synchronizations	60
\sqrt{ullet}	Traps	70
\sqrt{ullet}	Performance	73
	Conclusion	80 81

7 – Conclusion

- TopenMP requires a multi-processor machine with shared memory.
- Parallelization is relatively easy to implement, even when starting from a sequential program.
- Tt allows incremental parallelization.
- The full potential of parallel performances lies in the parallel region.
- Within these parallel regions, the work can be shared through the parallel loops and the parallel sections. But we can also single out a thread for a particular work.
- The orphaned directives allows the development of parallel routines and libraries.
- Point-to-point or global explicit synchronizations are sometimes necessary in the parallel region.
- Particular attention must be payed to the definition of the data-sharing attribute of used variables in a construct.
- The speedup measures the code scalability. It is limited by the sequential fraction of the program and is slowed by the additional costs due to threads management.

8 – Annexes

What we did not (or briefly) cover in this course:

- The lock procedures for point-to-point synchronization;
- Other service routines;
- The MPI & OpenMP hybrid parallelization;
- The new features of OpenMP 3.0 (the tasking concept, the improvements related to the parallel loops and nesting, etc.).

ATOMIC
BARRIER
COPYIN
COPYPRIVATE
CRITICAL61, 65, 66, 74
CRITICAL (RC1)
DEFAULT
DO36, 37, 44, 45, 50, 56, 70
DO LASTPRIVATE
DO REDUCTION
DO SCHEDULE
DO SCHEDULE ORDERED
DYNAMIC
END CDITICAL

END DO	37
END MASTER	.55
END PARALLEL DO	45
END PARALLEL SECTIONS	. 48
END SECTIONS	46
END SINGLE	54
END WORKSHARE	49
END CRITICAL	
END CRITICAL (RC1)	66
END DO	
END DO NOWAIT	42
END MASTER55,	
END ORDERED	42
END PARALLEL 22–29, 31–34, 38, 40, 42–44, 47, 50, 53–56, 62, 63, 66, 67, 70, 71,	77
END PARALLEL DO	75
END PARALLEL WORKSHARE	
END SECTIONS NOWAIT	47



END SINGLE53, 62, 71
END SINGLE COPYPRIVATE54
END SINGLE NOWAIT
END WORKSHARE NOWAIT50
FIRSTPRIVATE
FLUSH
GUIDED
IF
LASTPRIVATE
MASTER
NOWAIT
NUM_THREADS

ORDERED	
PARALLEL22,	25, 28, 43, 45, 47, 48, 50, 51, 57, 62, 66, 77
PARALLEL DO	45
PARALLEL SECTIONS	48
PARALLEL WORKSHARE	
PARALLEL COPYIN	
PARALLEL DEFAULT(NONE)	
PARALLEL DEFAULT(PRIVATE)	23, 42, 53–55, 70
PARALLEL DEFAULT(PRIVATE) SHARED	
PARALLEL DEFAULT(SHARED)	
PARALLEL DO LASTPRIVATE	
PARALLEL DO SCHEDULE	
PARALLEL IF	
PARALLEL NUM_THREADS	33, 34
PARALLEL PRIVATE	21, 32, 38, 44, 63, 67
DADALIDI CHADED DDIMATE	97

PARALLEL WORKSHARE	51
PRIVATE	23, 34, 44, 48, 54, 77
REDUCTION	
SCHEDULE	27 74
SCHEDULE	
SECTION	
SECTIONS	36, 46–48, 56
SHARED	31, 32, 70, 71
SINGLE	52–54, 62, 71, 74
STATIC	
THREADPRIVATE	29
WORKSHARE	36 49-51



omp.h	
OMP_GET_NUM_THREADS	
OMP_GET_THREAD_NUM	26–29, 31, 34, 38, 40, 42, 44, 53–55, 63, 67, 77
OMP_GET_WTICK	
OMP_GET_WTIME	
OMP_IN_PARALLEL	22, 25
OMP_LIB20–22,	25–29, 31, 34, 38, 40, 42, 44, 53–55, 63, 67, 77
OMP_SET_DYNAMIC	
OMP_SET_NESTED	
OMP_SET_NUM_THREADS	

OMP_DYNAMIC33, 34	Ė
OMP_NESTED	Ē
OMP_NUM_THREADS14, 22–28, 32, 33, 38, 40–44, 53–55, 66, 70, 71	
OMP_SCHEDULE	•