

arm - py game

- Given:

$L_1 = 8 \text{ cm}$ (upper arm)

$L_2 = 10 \text{ cm}$ (forearm)

$(x, y) = \text{target point}$

$\theta_1 = \text{shoulder angle}$

$\theta_2 = \text{elbow angle}$

- Distance to target:

$$r^2 = x^2 + y^2$$

$$r = \sqrt{x^2 + y^2}$$

- Law of cosines

$$\cos(\theta_2) = (r^2 - L_1^2 - L_2^2) / (2 L_1 L_2)$$

$$\theta_2 = \arccos((r^2 - L_1^2 - L_2^2) / (2 L_1 L_2))$$

$$\theta_1 = \arctan 2(y, x) - \arctan 2(L_2 \sin(\theta_2), L_1 + L_2 \cos(\theta_2))$$

- Reachability condition:

unreachable if:

$$r > L_1 + L_2 \quad \text{or} \quad r < |L_1 - L_2|$$

