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### Indexing.

Disk with block size =  $B = 512$  bytes.

Pointer  $p = 6$  bytes long.

record pointer is  $R = 7$  bytes.

A file has  $r = 30,000$  EMPLOYEE records of fixed length.

Name (30 bytes)

SSN (9 bytes)

Department code (9 bytes)

Address (40 bytes)

Phone (9 bytes)

Birthdate (8 bytes)

Sex (1 byte)

Job code (6 bytes)

Salary (4 bytes, real numbers)

a) Record length = sum of all bytes used to save data.

$$= (30 + 9 + 9 + 40 + 9 + 8 + 1 + 4 + 4) + 1$$

$$= \underline{\underline{115 \text{ bytes}}}$$

(additional byte)

b) Blocking factor bfr.

$$\text{Blocking factor} = \text{floor} \left( \frac{\text{Block size}}{\text{record size}} \right)$$

$$= \text{floor} \left( \frac{512}{115} \right)$$

$$= 4.45 \approx \underline{\underline{4 \text{ records} / \text{block}}}$$

c) i) Index record size  $R_i = [\text{SSN} + \text{pointer (P)}]$

$$= 9 + 6$$

$$= 15 \text{ bytes.}$$

$$\text{Index blocking factor bfr}_i = f_0 = \text{floor} \left( \frac{\text{Block size}}{\text{record size}} \right)$$

$$= \text{floor} \left( \frac{512}{15} \right) = \underline{\underline{34}}$$

ii) number of first level index entries ( $r_1$ )

$$= \text{number of file blocks } b = 7500 \text{ entries,}$$

$$\text{i.e. blocks needed for file} = \text{ceiling} \left( \frac{\text{Record}}{\text{blocking factor}} \right)$$

$$= \text{ceiling} \left( \frac{20000}{4} \right)$$

$$= \underline{\underline{7500}}$$

Number of first level index blocks

$$= \text{ceiling} \left( \frac{n}{\text{bfr}_i} \right) = \text{ceiling} \left( \frac{7500}{34} \right) = \underline{\underline{221 \text{ blocks}}}$$

iii) For multi level.

Number of second-level index <sup>entries</sup> ~~blocks~~  $r_2$  = number of first-level blocks  $b_1$ .

$$= 221 \text{ entries.}$$

Number of second-level index blocks  $b_2$  =  $\text{ceiling} \left( \frac{r_2}{bfr} \right)$   
 $= \text{ceiling} \left( \frac{221}{36} \right)$   
 $= 7 \text{ entries.}$

Number of third-level index <sup>entries</sup> ~~blocks~~  $r_3$  = number of <sup>sec</sup> ~~first~~ level index blocks  
 $= 7 \text{ entries.}$

Number of third level index blocks  $b_3$  =  $\text{ceiling} \left( \frac{r_3}{bfr} \right) = \text{ceiling} \left( \frac{7}{36} \right) = 1$

Hence index has  $X = 3$  levels.

iv) Total number of blocks for the index  $b = b_1 + b_2 + b_3$   
 $= 221 + 7 + 1$   
 $= \underline{229 \text{ blocks}}$

v) Number of blocks for the index record =  $X + 1 = 3 + 1 = \underline{4}$   
Accesses to search for

d) i) Index record size  $R_i = \text{ssn} + \text{pointer} = 9 + 6 = 15 \text{ bytes}$

Index blocking factor  $bfr = (\text{fan-out})_{to} = \text{floor} \left( \frac{\text{Block size}}{\text{Record size}} \right)$   
 $= \text{Floor} \left( \frac{512}{15} \right)$

$= \underline{34 \text{ Index records per block.}}$

ii) Number of first-level index entries  $r_1 = \text{number of records}$   
 $r = 300000$

Number of first-level index blocks  $b_1 = \text{ceiling} \left( \frac{r_1}{bfr} \right)$   
 $= \text{ceiling} \left( \frac{300000}{34} \right)$   
 $= \underline{883 \text{ blocks}}$

iii) We can calculate the number of levels as follows.

Number of second-level index entries  $r_2 = \text{number of first-level index blocks } b_1 = 883$   
 entries.

Number of second-level index blocks  $b_2 = \text{ceiling} \left( \frac{r_2}{bfr} \right) = \text{ceiling} \left( \frac{883}{34} \right)$   
 $= 26 \text{ blocks.}$



Number of third level index entries  $r_3 =$  Number of second-level index blocks  $b_2 = 26$  entries.

$$\text{Number of third-level index blocks } b_3 = \text{ceiling} \left( \frac{r_2}{b_{fr}} \right) = \text{ceiling} \left( \frac{26}{34} \right) = 1.$$

Since third-level index block has only one block, it is the top index level.

Hence, the index has 3 levels ( $X$ ).

$$\begin{aligned} \text{iv) Total number of blocks for index} &= b_1 + b_2 + b_3 \\ &= 883 + 26 + 1 \\ &= \underline{\underline{910}} \end{aligned}$$

$$\begin{aligned} \text{v) Number of blocks accesses to search for a record} \\ &= X + 1 = 3 + 1 = \underline{\underline{4}} \end{aligned}$$

e) i) Index record  $R = (\text{department code} + \text{pointer})$   
 $= 9 + 6 = 15 \text{ bytes.}$

Index blocking factor  $bfr = (\text{fan-out}) \times b = \text{floor}\left(\frac{\text{Block size}}{\text{Record size}}\right)$   
 $= \text{floor}\left(\frac{512}{15}\right)$

$= \underline{\underline{34 \text{ index records per block.}}}$

ii) There are 1000 distinct values of department code,  
 so average number of record for each value is  $1/1000$

$= \frac{30000}{1000} = \underline{\underline{30}}$

Since a record pointer size = 7 bytes.

number of bytes needed at the level of indirection for  
 each value of department code is  $7 \times 30 = 210 \text{ bytes.}$

which fits in one block.

$\therefore$  1000 blocks are needed for level of indirection.

iii) number of first-level index entries  $r_1 = \text{number of } \overset{\text{distinct values}}{\text{first-level block}}$   
 of department code = 1000 entries.

number of first-level index blocks  $b_1 = \text{ceiling}(r_1 / bfr) = \text{ceiling}(1000 / 34)$   
 $= \underline{\underline{30 \text{ blocks.}}}$

iv) we can calculate the number of level as follows

$$\begin{aligned}\text{Number of first-level index blocks } b_1 &= \text{ceiling}(n/bfr) \\ &= \text{ceiling}(6000/36) \\ &= \underline{\underline{30 \text{ blocks}}}\end{aligned}$$

$$\begin{aligned}\text{Number of second-level index entries } r_2 &= \text{Number of first level} \\ &\quad \text{Index block, } b_1 \\ &= 30 \text{ entries.}\end{aligned}$$

$$\begin{aligned}\text{Number of second-level index-blocks } b_2 &= \text{ceiling}(r_2/bfr) \\ &= 30/36 = 1\end{aligned}$$

Hence index has  $x = 2$  levels.

$$\begin{aligned}\text{v) Total number of blocks for index} &= b_1 + b_2 + b_{\text{indirection}} \\ &= 30 + 1 + 1000 \\ &= \underline{\underline{1031 \text{ blocks}}}\end{aligned}$$

$$\begin{aligned}\text{vi) Number of block accesses to search for and retrieve} \\ \text{the blocks containing the record pointers at the level of} \\ \text{indirection} &= x + 1 \\ &= 2 + 1 = \underline{\underline{3 \text{ block accesses}}}\end{aligned}$$

for 30 records are distributed over 30 distinct blocks.  
 we need 30 additional block accesses to retrieve ~~all~~ all 30 records.

Hence total block accesses needed on avg. to retrieve all records with given value of dept code.

$$= X+1+30$$

$$= \underline{\underline{33}}$$

f). ii) Index record size  $R =$  department code + pointer  
 $= 9+6 = 15 \text{ bytes.}$

Index blocking factor  $bfr =$  fan-out ( $fo$ )  $= \text{floor} \left( \frac{\text{block size}}{\text{records}} \right)$

$$= 812/15 = 34 \text{ index records per block.}$$

iii) number of first-level index entries  $r_1$

$$= \text{number of first-level index blocks } b_1.$$

$$= \text{ceiling} \left( \frac{r_1}{bfr} \right)$$

$$= \text{ceiling} \left( \frac{1000}{34} \right) = \underline{\underline{30 \text{ blocks.}}}$$



③

Number of Second-level Index blocks  $b_2 = \text{ceiling} \left( \frac{r_2}{bfr} \right) = \text{ceiling} \left( \frac{30}{24} \right)$

Since Second level has one block, it is the top Index level. 2

Hence index has  $X = \underline{\underline{2}}$  levels.

iv) total number of blocks for the Index  $= b_1 + b_2 = 30 + 1$   
31 blocks

v) Number of block accesses to search for the first block  
in the cluster of blocks  $= X + 1$   
 $= 2 + 1 = \underline{\underline{3}}$

The 30 records are clustered in  $\text{ceiling} \left( \frac{30}{bfr} \right) = \text{ceiling} \left( \frac{30}{4} \right)$   
8 blocks

Hence, total block accesses needed on average to retrieve  
all the records with a given department code

$$\begin{aligned} X &= 8 + 2 \\ &= 2 + 8 \\ &= \underline{\underline{10 \text{ block accesses}}} \end{aligned}$$

9) B+ tree of order  $p$ .

following inequality must be satisfied for each internal tree

$$\text{node } (p \times p) + ((p-1) \times \text{SSN}) \leq \text{Block size.}$$

$p$  = pointer length.

$$(p \times 6) + ((p-1) \times 4) \leq 512$$

which gives  $15p \leq 512$

$$\therefore p = \underline{\underline{34}}$$

For leaf nodes, assuming that record pointers are included in the leaf nodes.

the following inequality must be satisfied.

$$(p \times \text{leaf} \times (\text{SSN} + \text{pointer}_{\text{record}})) + p \leq B.$$

$$\therefore [p \times \text{leaf} \times (9+7) + 6] \leq 512.$$

$$16p \times \text{leaf} \leq 506.$$

$$\therefore p \times \text{leaf} = \underline{\underline{31}}$$

ii) Assuming the nodes are 69% of leaf.

$$\therefore 0.69 p \times \text{leaf} = 0.69 \times 31 = \underline{\underline{21.39}}$$

Since the file has 30000 records and hence 30,000 values of SSN. the number of leaf-level nodes (blocks) needed is  $b_1 = \text{ceiling} \left( \frac{30,000}{22} \right) = 1364 \text{ blocks}$  (6)

iii) we can calculate the number of levels as follows.

The avg. fan-out for the internal nodes

$$f_0 = \text{ceiling} (0.68 * p) = \text{ceiling} (0.68 * 34) \\ = \text{ceiling} (23.46) = \underline{\underline{24}}$$

Second-level tree blocks  $b_2 = \text{ceiling} (b_1 / f_0) = \text{ceiling} (1364 / 24) \\ = \underline{\underline{57 \text{ blocks}}}$

Third-level tree blocks  $b_3 = \text{ceiling} (b_2 / f_0) \\ = \text{ceiling} \left( \frac{57}{24} \right) \\ = \underline{\underline{3 \text{ blocks}}}$

Fourth-level tree blocks  $b_4 = \text{ceiling} (b_3 / f_0) = \text{ceiling} (3 / 24) \\ = \underline{\underline{1}}$

Since fourth level has only one block.  
the tree has  $X = 4$  levels

$$\therefore X = \text{ceiling} (\log_{10}(b_1) + 1).$$

$$= \text{ceiling} (\log_{10}(1324) + 1)$$

$$= 3 + 1 = 4 \text{ levels.}$$

ii) Total number of blocks for tree =  $b_1 + b_2 + b_3 + b_4$

$$= 1364 + 57 + 3 + 1$$

$$= \underline{\underline{1425 \text{ blocks}}}$$

v) number of blocks accessed to search for a record

$$= X + 1 = \underline{\underline{4 + 1 = 5}}$$



20.

a)  $P \leftarrow$  address of top level block of index.

for  $j = 0$  to  $j \leq \text{step} - 1$  to 1 do  
begin.

read the index block (at  $j^{\text{th}}$  index level)

whose address is  $P$ .

compare index block ( $j^{\text{th}}$  index level) to next  
index block. ( $(j+1)$  index level block).

$P \leftarrow P[j]$  (picks appropriate pointer at  $j^{\text{th}}$   
index level).

end;

read the data file block whose address

is  $P$ .

b)

$p \leftarrow$  address of top level block of index.

for  $i = 0; i < \text{step} - 1; i++$  do

begin.

read the index block, whose address is  $p$ .

$i[p]$

search block  $p$  for entry  $i$  such that.

$K[i] \leq k < K[i+1]$

if ( $K[i]$  is last entry of the block), it is sufficient to

satisfy  $K[i] \leq k$ !

$p \leftarrow p[i]$

end:

read the data file block whose address is  $p$ .

search block  $p$  for record with  $\text{key} = K$ .

c)

clustering index.

index file: clustering field value & block pointer.

$p \leftarrow$  address of top level block of index.

for  $j \leftarrow \text{step} - 1$  to  $1$  do.

begin.

read the index block: whose address is  $p$ :

$$k_j(i) \leq k \leq k_j(i+1)$$

if  $(k_j(i))$  is last entry in the block.

it is sufficient to satisfy  $k_j(i) \leq k$ :

$p \leftarrow p_j(i)$

end:

read the data file block whose address is  
search block  $p$  for record with key =  $k_j$ .