Q1 Teamname

0 Points

NULL

Q2 Commands

5 Points

List the commands used in the game to reach the ciphertext.

go,go,go,go,give,read

Q3 Analysis

50 Points

Give a detailed description of the cryptanalysis used to figure out the password. (Explain in less than 100 lines and use Latex wherever required. If your solution is not readable, you will lose marks. If necessary, the file upload option in this question must be used TO SHARE IMAGES ONLY.)

1. Understanding the encryption algorithm

The problem statement was to decrypt the encrypted message which was encrypted using a procedure which is similar to SHA-3 (which was given to us as C code). We analyzed the encryption algorithm and obtained the following inferences about its working:

- (a) The encryption algorithm pads the message with zeroes until its length becomes 576 bits.
- (b) The algorithm maintains a state (which is 5*5*64 array) which gets updated as we proceed through the algorithm.
- (c) The state is initialized such that the first 576 values in the array (in row major order) are initialized to the corresponding bits of the padded message and the remaining bits are initialized to zero.
- (d) In each round, The algorithm applies theta, Pi, Chi operation once on the current state and there are 24 such rounds.

The code for theta, Pi, chi operations are given below

```
for(k = 0; k < 64; ++k){
                state[i][j][k] ^= column_parity[(i+4)%5][k] ^ column_parity[(i+1)%5][k];
                tempstate[i][j][k] = state[i][j][k];
          }
     }
//pi operation
for(i = 0; i < 5; ++i)
     for(j = 0; j < 5; ++j)
           for(k = 0; k < 64; ++k)
                state[j][((2 * i) + (3 * j)) \% 5][k] = tempstate[i][j][k];
//chi operation
for(i = 0; i < 5; ++i)
     for(j = 0; j < 5; ++j)
           for(k = 0; k < 64; ++k)
                tempstate[i][j][k] = state[i][j][k];
for(i = 0; i < 5; ++i)
     for(j = 0; j < 5; ++j)
           for(k = 0; k < 64; ++k)
                state[i][j][k] = tempstate[i][j][k] ^ ("tempstate[i][(j+1)%5][k] & tempstate[i][(j+2)%5]
[k]);
```

(e) The encrypted message is obtained by taking the first 512 bits of the final state (in row major order).

2. Breaking the algorithm

The main observation which enabled us to break the encryption is the following:

Let state, new state be the states before and after applying one round of theta,pi and chi operations.

For all $0 \le i \le 4, 0 \le j \le 4, 0 \le k \le 63$ the value of newstate[i][j][k] only depends on the set of values $S = \{state[i'][j'][k]: 0 \le i' \le 4, 0 \le j' \le 4\}$. This can be seen by carefully observing the code given above.

The observation essentially implies that to calculate the value of a cell (i,j,k) in the final state after 24 rounds, we only need to know the values of cells with same value of the third coordinate in the initial state.

So our goal is to find the initial state given the first 512 bits (above) of the final state (after applying 24 rounds). Also, the password was given to be no more than 16 characters, so we only need to find the first 128 bits of the initial state (and the rest are all zeroes).

Our strategy was to use brute force combined with above observation to find the password. Using the above observation we can do the following:

For each k from 0 to 63:

Let $S_k=\{(i,j,k): 0\leq i\leq 4, 0\leq j\leq 4, i*64*5+j*64+k<128\}$ which is the set of all cells such that the third coordinate equal to k and is within the first 128 cells. It can be clearly seen that $|S_k|=2$ owing to the way in which the state is initialized. we try all $2^{|S_k|}$ possibilities for the values of these cells in the initial state and assign the one which gives the correct values for all the cells $(i',j',k), 0\leq i'\leq 4, 0\leq j'\leq 4$ in the final state(which is given above).

The correctness of the above algorithm directly follows from the observation. Using the above procedure, we obtained the password "mjpkfhauegjy" which cleared the level.

No files uploaded

Q4 Password

25 Points

What was the final command used to clear this level?

mjpkfhauegjy

Q5 Codes

0 Points

It is mandatory that you upload the codes used in the cryptanalysis. If you fail to do so, you will be given 0 marks for the entire assignment.

```
▲ Download
▼ solver.cpp
    #include <bits/stdc++.h>
1
2
    using namespace std;
3
    void prepare(string &s)
4
5
6
         string ans = "";
7
         for (int i = 0; i < s.length(); i++)
8
9
             int x;
             if (s[i] >= '0' \text{ and } s[i] <= '9')
10
11
12
                  x = s[i] - '0';
13
             if (s[i] \ge 'A' \text{ and } s[i] \le 'F')
14
15
                  x = s[i] - 'A' + 10;
16
17
18
19
             for (int j = 0; j < 4; j++)
20
                  if ((x & (1 << j)) != 0)
21
22
                      ans += '1';
23
                  else
                      ans += '0';
24
25
             }
26
27
         s = ans;
28
29
30
     int main()
```

```
31
   {
32
        string s =
    "6A646069000000001018004666168EA6B6FE5ED666168EA010B8584666168EA000A05800000000
33
34
        prepare(s);
35
        uint64_t final_state[5][5][64];
36
37
        assert(int(s.size()) == 512);
38
39
        for (int i = 0, cur = 0; cur < 512; i++)
40
            for (int j = 0; j < 5 and cur < 512; j++)
41
42
43
                for (int k = 0; k < 64 and cur < 512; k++)
44
                {
45
                     final_state[i][j][k] = s[cur++] - '0';
46
                }
47
            }
48
        }
49
50
        uint64_t state[5][5][64], ans[5][5][64];
51
        for (int i = 0; i < 5; i++)
52
            for (int j = 0; j < 5; j++)
53
                for (int k = 0; k < 64; k++)
54
                     state[i][j][k] = ans[i][j][k] = 0;
55
56
        vector<int> adj[64];
57
        for (int i = 0, cur = 0; cur < 128; i++)
58
        {
59
            for (int j = 0; j < 5 and cur < 128; j++)
60
                for (int k = 0; k < 64 and cur < 128; k++)
61
62
63
                     adj[k].push_back(i * 5 + j);
64
                     cur++;
65
                }
66
            }
67
        }
68
69
        for (int kk = 0; kk < 64; kk++)
70
71
            int nn = int(adj[kk].size());
72
            int cnt = 0;
73
            for (int mask = 0; mask < (1 << nn); mask++)
74
75
                for (int i = 0; i < nn; i++)
76
                {
77
                     if ((mask & (1 << i)) != 0)
78
79
                         int ii = adj[kk][i] / 5;
80
                         int jj = adj[kk][i] % 5;
81
                         state[ii][jj][kk] = 1;
82
                         ans[ii][jj][kk] = 1;
83
                    }
84
                }
85
                char hexa[16] = {'0', '1', '2', '3', '4', '5', '6', '7', '8', '9',
86
    'A', 'B', 'C', 'D', 'E', 'F'};
87
                uint64_t b = 1600;
88
89
                uint64 t l = 512;
90
                uint64_t c = 1024;
91
                uint64 t r = 576;
92
                int rounds = 24;
93
                int i, j, k;
94
```

```
95
                  uint64_t tempstate[5][5][64];
96
97
                  uint64_t current_round = 0;
98
                  uint64_t column_parity[5][64];
99
100
                  while (current_round < rounds)</pre>
101
102
                      //theta operation
103
                      for (i = 0; i < 5; ++i)
104
105
                          for (k = 0; k < 64; ++k)
106
107
                               column_parity[i][k] = 0;
108
                              for (j = 0; j < 5; ++j)
109
                                   column_parity[i][k] ^= state[i][j][k];
110
                          }
111
                      }
112
113
                      for (i = 0; i < 5; ++i)
114
                          for (j = 0; j < 5; ++j)
115
116
117
                              for (k = 0; k < 64; ++k)
118
119
                                   state[i][j][k] ^= column_parity[(i + 4) % 5][k] ^
     column_parity[(i + 1) % 5][k];
120
                                   tempstate[i][j][k] = state[i][j][k];
121
122
                          }
123
                      }
124
125
                      //pi operation
126
                      for (i = 0; i < 5; ++i)
127
                          for (j = 0; j < 5; ++j)
128
                               for (k = 0; k < 64; ++k)
129
                                   state[j][((2 * i) + (3 * j)) % 5][k] = tempstate[i]
     [j][k];
130
131
                      //chi operation
132
                      for (i = 0; i < 5; ++i)
133
                          for (j = 0; j < 5; ++j)
                               for (k = 0; k < 64; ++k)
134
135
                                   tempstate[i][j][k] = state[i][j][k];
136
137
                      for (i = 0; i < 5; ++i)
138
                          for (j = 0; j < 5; ++j)
                              for (k = 0; k < 64; ++k)
139
140
                                   state[i][j][k] = tempstate[i][j][k] ^
     (\text{-tempstate}[i][(j + 1) \% 5][k] \& \text{tempstate}[i][(j + 2) \% 5][k]);
141
142
                      ++current_round;
143
                  }
144
145
                  bool ok = 1;
146
                  for (i = 0; i < 5; i++)
147
148
                      for (j = 0; j < 5; j++)
149
150
                          int foo = i * 5 * 64 + j * 64 + kk;
                          if (foo >= 512)
151
152
                          ok &= (final_state[i][j][kk] == state[i][j][kk]);
153
154
                      }
155
156
                  for (i = 0; i < 5; i++)
157
```

```
158
                      for (j = 0; j < 5; j++)
159
160
                          state[i][j][kk] = 0;
161
                          if (!ok)
162
                               ans[i][j][kk] = 0;
163
                      }
164
                  }
165
166
                  if (ok)
167
                  {
168
                      break;
169
                  }
170
171
         }
172
173
         string pass = "";
174
         for (int i = 0, cur = 0; cur < 128; i++)
175
176
             for (int j = 0; j < 5 and cur < 128; j++)
177
178
                  for (int k = 0; k < 64 and cur < 128; k++)
179
180
                      pass += char('0' + ans[i][j][k]);
181
                      cur++;
182
                  }
183
             }
184
         }
185
186
         cout << "The password is ";</pre>
187
         for (int i = 0; i < pass.size(); i += 8)
188
189
             int cur = 0;
190
             for (int j = i; j - i < 8; j++)
191
192
                  cur = (cur << 1) + (pass[j] - '0');
193
             }
194
             if (cur)
195
                  cout << char(cur);</pre>
196
         }
197
         cout << endl;</pre>
198
199
         return 0;
200 }
```

Assignment 7

UNGRADED

GROUP

A5 - SURYADEVARA SAI KRISHNA AJAY PRAJAPATI A11 - GARIMELLA MOHAN RAGHU View or edit group

TOTAL POINTS

- / 80 pts

G	DUESTION 1	
Т	eamname	0 pts
G	DUESTION 2	
C	Commands	5 pts
G	DUESTION 3	
A	Analysis	50 pts
G	DUESTION 4	
F	Password	25 pts
G	DUESTION 5	
	Codes	0 pts