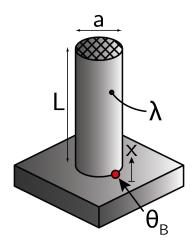


Fins - Flux 1

Calculate the rate of heat transfer for a fin with an adiabatic head.



Given the fin temperature profile:

$$\Theta(x) = \Theta_{\rm B} \frac{\cosh(m(L-x))}{\cosh(mL)}$$

Where
$$\Theta(x) = T(x) - T_{\infty}$$
 and $m = \sqrt{\frac{4\alpha}{\lambda a}}$.

The rate of heat transfer through the fin can be expressed as:

$$\dot{Q} = -\lambda A_{\rm c} \frac{\partial T}{\partial x}|_{x=0} = -\lambda \frac{\pi a^2}{4} \frac{\partial \Theta}{\partial x}|_{x=0}$$

Differentiation of $\Theta(x)$ with respect to x yields:

$$\frac{\partial \Theta}{\partial x} = -m\Theta_{\rm B} \frac{\sinh\left(m\left(L - x\right)\right)}{\tanh\left(mL\right)}$$

There for at x = 0 gives:

$$\frac{\partial \Theta}{\partial x}|_{x=0} = -\Theta_{\rm B} \frac{\sinh{(mL)}}{\cosh{(mL)}} = -\Theta_{\rm B} \cosh{(mL)}$$

Substitution into the expression for the rate of heat transfer yields:

$$\dot{Q} = \lambda \frac{\pi a^2}{4} m \Theta_{\rm B} \tanh \left(mL \right)$$