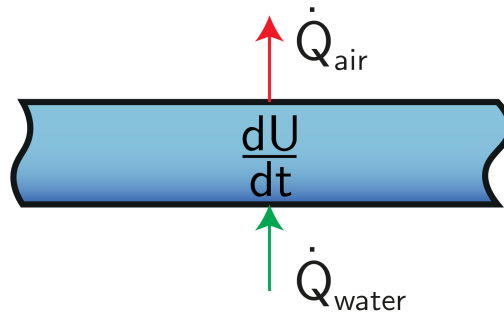


## EB - Cond. - Body 6

Ice is continuously increasing in thickness. Convection occurs on both sides. Derive the differential equation to describe the ice layer thickness  $s(t)$ . The enthalpy of fusion is  $h$ . Take  $T_2 > T_w > T_1$ . The cooling of the ice, contrary to freezing, is energetically negligible,  $c_i \cdot \Delta T \ll h$ .



**Energy balance:**

$$\frac{dU}{dt} = \dot{Q}_{water} - \dot{Q}_{air}$$

The heat transfer can be classified as transient, for that reason the change of internal energy over time equals the sum of the in and outgoing fluxes.

**Change of internal energy over time:**

$$\frac{dU}{dt} = -\rho A h \frac{ds}{dt}$$

The internal energy can be described by use of the enthalpy of fusion. This is denoted with a negative sign, since solidification of water costs energy.

**Heat fluxes:**

$$\dot{Q}_{water} = \alpha_2 A (T_2 - T_w)$$

$$\dot{Q}_{air} = (T_w - T_1) A \frac{1}{\frac{1}{\alpha_1} + \frac{s(t)}{\lambda}}$$