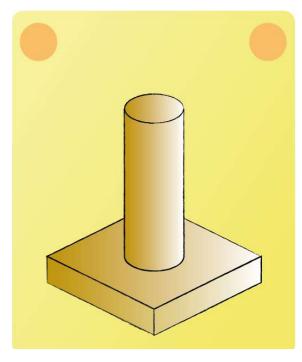


## Lecture 11 - Question 5



One of the possible solutions for the homogeneous differential equations for fins is

$$\theta(x) = A \cdot \sinh(m \cdot x) + B \cdot \cosh(m \cdot x)$$

Consider an sufficiently long fin with no heat exchange at the tip. Futhermore, the base temperature  $T_{\rm B}$  and the environmental temperature  $T_{\rm A}$  are known. Which two boundary conditions can be **directly** used for determining coefficients A and B?

$$\theta\left(0\right) = T_B - T_A$$

Describes directly that the temperature difference between the surface temperature T(x) at x=0 and the ambient temperature  $T_A$  is the difference between the base temperature  $T_B$  and ambient temperature  $T_A$ . Which is a result from the fact that the surface temperature at x=0 equals the base temperature  $T(0)=T_B$ .



$$\left. \frac{d\theta}{dx} \right|_{x=L} = 0$$

Describes directly that, due to the fact that the fin is infinitely long, no heat exchange will take place at x=L. Therefore the gradient of the temperature difference between the surface temperature T(x) at x=L and the ambient temperature  $T_{\rm A}$  is zero. Which is a result from the fact that the surface temperature gradient at x=L approaches zero  $\frac{dT}{dx}\big|_{x=L}=0$