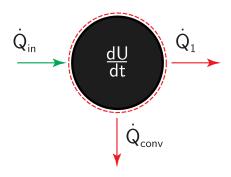


EB - Rad. - Outer 08

Set up the outer energy balance for the sphere that describes the change of its homogeneous temperature T_1 over the course of time. Use view factors and surface brightness whenever possible.



Energy balance:

$$\frac{\partial U}{\partial t} = \sum \dot{Q}_{\rm in} - \sum \dot{Q}_{\rm out}$$
$$\frac{dU}{dt} = \dot{Q}_{\rm in} - \dot{Q}_{\rm conv} - \dot{Q}_{\rm 1}$$

Change of internal energy over time:

$$\frac{dU}{dt} = m_1 c_1 \frac{dT_1}{dt}$$

Heat fluxes:

The rate of heat transfer by radiation toward body 1 can be stated as:

$$\dot{Q}_{\rm in} = \dot{q}'' A_1$$

Rate of heat loss by convection:

$$\dot{Q}_{\rm conv} = \alpha_{\rm conv} A_1 \left(T_1 - T_{\infty} \right)$$

The surface brightness of body 1 will be determined in a separate task and can be stated as \dot{Q}_1 .

Substituting and rewriting:

$$\Rightarrow m_1 c_1 \frac{dT_1}{dt} = \dot{q}'' A_1 - \alpha_{\text{conv}} A_1 \left(T_1 - T_{\infty} \right) - \dot{Q}_1$$