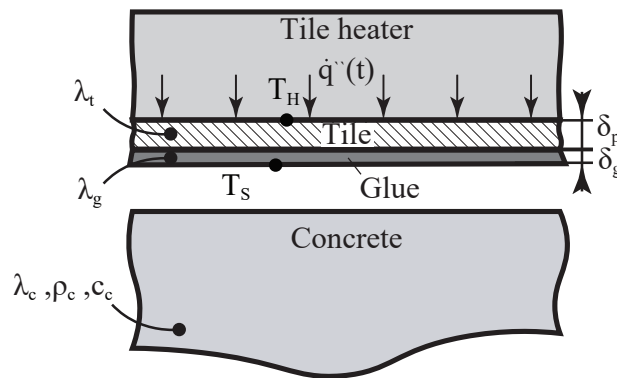


**Exercise II.15** (Tile setting \*\*):

A tile setter employs a modern technique for tile installation, involving preheating the tile and glue before affixing them to the concrete. The tile and glue are heated until they reach a steady-state condition, achieving a uniform heating temperature  $T_H$  and a constant heat flux  $\dot{q}_0''$ . Once these conditions are met, the tile setter places the heated tile and glue on the concrete, maintaining a constant temperature  $T_S$  throughout the process. After reaching a critical temperature  $T_{crit}$  at a distance  $\delta_{crit}$  within the concrete, the heater is removed. Initially, the concrete used to be at a homogeneous temperature  $T_0$ .

**Given parameters:**

- |   |  |
|---|--|
| • Steady-state heat flux:                 | $\dot{q}_0'' = 7.5 \text{ kW/m}^2$     |
| • Thickness of the pile:                  | $\delta_p = 10 \text{ mm}$             |
| • Thickness of the glue:                  | $\delta_g = 2 \text{ mm}$              |
| • Conductivity of the pile:               | $\lambda_p = 1.0 \text{ W/mK}$         |
| • Conductivity of the glue:               | $\lambda_g = 0.35 \text{ W/mK}$        |
| • Conductivity of the concrete:           | $\lambda_c = 2.3 \text{ W/mK}$         |
| • Heat capacity of the concrete:          | $c_c = 1,000 \text{ J/kgK}$            |
| • Density of the concrete:                | $\rho_c = 2,400 \text{ kg/m}^3$        |
| • Initial temperature of the concrete:    | $T_0 = 20 \text{ }^\circ\text{C}$      |
| • Heating temperature of the tile heater: | $T_H = 200 \text{ }^\circ\text{C}$     |
| • Critical temperature:                   | $T_{crit} = 35 \text{ }^\circ\text{C}$ |
| • Critical distance:                      | $\delta_{crit} = 10 \text{ mm}$        |

**Hints:**

- Heat will never penetrate entirely through the concrete.

**Tasks:**

- Derive the differential equation and establish the boundary and/or initial conditions to determine the temperature profile of the concrete. Based on your findings, identify the method that can be employed to determine the temperature at a particular position and time.
- Determine the time  $t_{crit}$  at which the heater can be removed.
- Illustrate the concrete's temperature profile that depicts both temporal and spatial variations.

**Exercise II.16** (Heating and quenching of a sphere ★★★):

A sphere, initially at a homogeneous temperature of  $T_0$ , is put into an oven. The oven temperature remains constant at a homogeneous temperature of  $T_o$ .

**Given parameters:**

- |   |  |
|---|--|
| • Initial temperature of the sphere:      | $T_0 = 25\text{ }^{\circ}\text{C}$       |
| • Intermediate temperature of the sphere: | $T_h = 150\text{ }^{\circ}\text{C}$      |
| • Oven temperature:                       | $T_o = 200\text{ }^{\circ}\text{C}$      |
| • Quenching temperature:                  | $T_q = 30\text{ }^{\circ}\text{C}$       |
| • Heat transfer coefficient:              | $\alpha = 110\text{ W/m}^2\text{K}$      |
| • Radius of the sphere:                   | $r_1 = 1.5\text{ cm}$                    |
| • Thermal conductivity of the sphere:     | $\lambda = 1.52\text{ W/mK}$             |
| • Density the sphere:                     | $\rho = 1.45 \cdot 10^3\text{ kg/m}^3$   |
| • Specific heat capacity the sphere:      | $c_p = 0.88\text{ kJ/kg} \cdot \text{K}$ |

**Hints:**

- Heat radiation can be neglected.
- It always remains that  $Fo > 0.2$

**Tasks:**

- Derive the differential equation and establish the boundary and/or initial conditions to determine the temperature profile of the sphere. Based on your findings, identify the method that can be employed to determine the temperature at a particular position and time.
- Determine the temperature of the center of the sphere after 3 minutes.

After some time the sphere has a hot homogeneous temperature  $T_h$  and is being quenched. During this process, the quenching temperature is constant at  $T_q$ . Further, in time, the center of the sphere has a temperature of  $54\text{ }^{\circ}\text{C}$  and the surface has a temperature of  $44.4\text{ }^{\circ}\text{C}$ .

- Determine the time instant when the center of the sphere has a temperature of  $54\text{ }^{\circ}\text{C}$  and the surface has a temperature of  $44.4\text{ }^{\circ}\text{C}$ .
- Determine the amount of heat dissipated at this time instant.