

### Assignment -3

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Let us consider a sample of dataset have one input ( $x, a$ ) and one output ( $y_i^a$ ) and number of samples 4. Develop a simple linear regression model using stochastic gradient descent optimizer.

sample ( $i$ )	$x, a$	$y_i^a$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Step 1:  $x, y, m=1, c=-1, \eta=0.1, \text{epochs}=2, ns=2$

Step 2:  $\text{iter} = 1$

Step 3: sample = 1

$$\text{Step 4: } \frac{\partial E}{\partial M} = -(3.4 - (1)(0.2) - (-1)) 0.2 = 0.84$$

$$\frac{\partial E}{\partial c} = -(3.4 - (1)(0.2) + 1) = -4.2$$

$$\text{step 6: } \Delta m = -(0.1)(0.47) = -0.047$$

$$\Delta c = -(0.1)(-4.73) = 0.473$$

$$\text{step 6: } m = m + \Delta m = 1.084 - 0.047 = 1.037$$

$$c = c + \Delta c = -1.042 + 0.473 = -0.569$$

$$\text{step 7: } \text{sample} = \text{samples} + 1$$

$$= 1 + 1 = 2$$

$$\text{step 8: } \text{if (sample} > \text{ns)}$$

$$\text{goto step 9}$$

$$\text{else goto step 4}$$

$$\text{step 4: } \frac{\partial E}{\partial m} = -(3.8 - (1.084)(0.4) + 0.58)0.4$$

$$= -1.5785$$

$$\frac{\partial E}{\partial c} = -(3.8 - (1.084)(0.4) + 0.58)$$

$$= -3.9464$$

$$\text{step 5: } \Delta m = -(0.1)(-1.5785) = 0.15785$$

$$\Delta c = -(0.1)(-3.9464) = 0.39464$$

$$\text{step 6: } m = m + \Delta m = 1.084 + 0.15785 = 1.24185$$

$$c = c + \Delta c = -0.58 + 0.39464 = -0.18536$$

step 7:  $\text{sample} = \text{sample} + 1$   
 $= 2 + 1 = 3$

step 8: - if ( $\text{sample} > n$ )  
 $3 > 2$

go to step 1

else  
 go to step 4.

step 9:  $\text{iter} = \text{iter} + 1$   
 $= 1 + 1 = 2$

step 10: if ( $\text{iter} > \text{epochs}$ )  
 $2 > 2$   
 go to step 11

else  
 go to step 3.

step 3:  $\text{sample} = 1$

step 4:  $\frac{\partial E}{\partial M} = -[3.4 - (1.2)(0.2) + 0.18] \cdot 0.2$   
 $= -3.4$

$= -0.68$

$\frac{\partial E}{\partial c} = -[3.4 - (1.2)(0.2) + 0.18]$   
 $= -3.34$



$$\text{step 5: } \Delta m = -(0.1)(-0.667) \\ = 0.066$$

$$\Delta c = -(0.1)(-3.34) \\ = +0.33$$

$$\text{step 6: } m = m + \Delta m = 1.24 + 0.066 = 1.3$$

$$c = c + \Delta c = -0.18 + 0.33 = 0.15$$

$$\text{step 7: } \text{sample} = \text{sample} + 1 \\ = 1 + 1 = 2$$

step 8: if (sample > nr)  
                     goto step 9  
                     else step 4

$$\text{step 4: } -\frac{\partial e}{\partial m} = -(3.8 - (1.3)(0.4) - 0.15)0.4 \\ = -1.25$$

$$\frac{\partial c}{\partial c} = -(3.8 - (1.3)(0.4) - 0.15) \\ = -3.13$$

$$\text{step 6: } m = M + m = 1.3 + 0.12 = 1.42$$

$$c = C + c = 0.15 + 0.31 = 0.46$$

$$\text{step 7: } \text{sample} = \text{sample} + 1 \\ = 2 + 1 = 3$$

$$\text{step 8: } \text{if } (\text{sample} > n) \\ 3 > 2 \\ \text{goto step 7} \\ \text{else step 4}$$

$$\text{step 9: } \text{iter} = \text{iter} + 1 \\ = 2 + 1 = 3$$

$$\text{step 10: } \text{if } (\text{iter} > \text{epochs})$$

$$\text{step 11}$$

$$\text{else step 3}$$

$$\text{step 11: } \text{print } m, c$$

$$m = 1.42 \quad c = 0.46$$