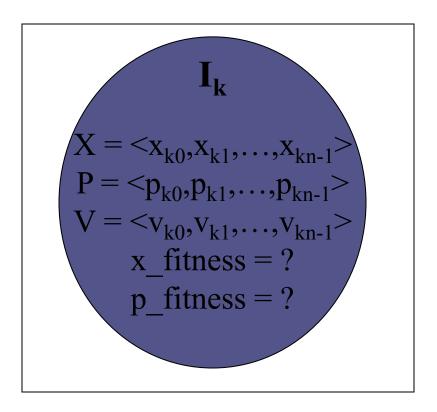
Particle Swarm Optimization

- Particle Swarm Optimization (PSO) applies the concept of social interaction to problem solving.
- It was developed in 1995 by James Kennedy and Russ Eberhart [Kennedy, J. and Eberhart, R. (1995). "Particle Swarm Optimization", Proceedings of the 1995 IEEE International Conference on Neural Networks, pp. 1942-1948, IEEE Press.] (http://dsp.jpl.nasa.gov/members/payman/swarm/kennedy95-ijcnn.pdf)
- It has been applied successfully to a wide variety of search and optimization problems.
- In PSO, a swarm of n individuals communicate either directly or indirectly with one another search directions (gradients).
- PSO is a simple but powerful search technique.

Particle Swarm Optimization: The Anatomy of a Particle

- A particle (individual) is composed of:
 - Three vectors:
 - The x-vector records the current position (location) of the particle in the search space,
 - The p-vector records the location of the best solution found so far by the particle, and
 - The v-vector contains a gradient (direction) for which particle will travel in if undisturbed.
 - Two fitness values:
 - The x-fitness records the fitness of the x-vector, and
 - The p-fitness records the fitness of the p-vector.



Particle Swarm Optimization: Swarm Search

- In PSO, particles never die!
- Particles can be seen as simple agents that fly through the search space and record (and possibly communicate) the best solution that they have discovered.
- So the question now is, "How does a particle move from on location in the search space to another?"
- This is done by simply adding the v-vector to the x-vector to get another x-vector $(X_i = X_i + V_i)$.
- Once the particle computes the new Xi it then evaluates its new location. If x-fitness is better than p-fitness, then $P_i = X_i$ and p-fitness = x-fitness.

Particle Swarm Optimization: Swarm Search

Actually, we must adjust the v-vector before adding it to the x-vector as follows:

```
 - v_{id} = v_{id} + \phi 1*rnd()*(p_{id}-x_{id}) 
 + \phi 2*rnd()*(p_{gd}-x_{id}); 
 - x_{id} = x_{id} + v_{id};
```

- Where i is the particle,
- $\phi 1$, $\phi 2$ are learning rates governing the **cognition** and **social** components
- Where g represents the index of the particle with the best pfitness, and
- Where **d** is the dth dimension.

Particle Swarm Optimization: Swarm Search

 Intially the values of the velocity vectors are randomly generated with the range [-Vmax, Vmax] where Vmax is the maximum value that can be assigned to any v_{id}.

Particle Swarm Optimization: Swarm Types

- In his paper, [Kennedy, J. (1997), "The Particle Swarm: Social Adaptation of Knowledge", Proceedings of the 1997 International Conference on Evolutionary Computation, pp. 303-308, IEEE Press.]
- Kennedy identifies 4 types of PSO based on ϕ 1 and ϕ 2.

• Given:
$$v_{id} = v_{id} + \phi 1 * rnd() * (p_{id} - x_{id}) + \phi 2 * rnd() * (p_{gd} - x_{id});$$

$$x_{id} = x_{id} + v_{id};$$

- Full Model $(\phi 1, \phi 2 > 0)$
- Cognition Only $(\phi 1 > 0 \text{ and } \phi 2 = 0)$,
- Social Only $(\phi 1 = 0 \text{ and } \phi 2 > 0)$
- Selfless $(\phi 1 = 0, \phi 2 > 0, \text{ and } g \neq i)$

Particle Swarm Optimization: Related Issues

- There are a number of related issues concerning PSO:
 - Controlling velocities (determining the best value for Vmax),
 - Swarm Size,
 - Neighborhood Size,
 - Updating X and Velocity Vectors,
 - Robust Settings for (ϕ 1 and ϕ 2),
 - An Off-The-Shelf PSO
- Carlisle, A. and Dozier, G. (2001). "An Off-The-Shelf PSO", *Proceedings of the 2001 Workshop on Particle Swarm Optimization*, pp. 1-6, Indianapolis, IN. (http://antho.huntingdon.edu/publications/Off-The-Shelf_PSO.pdf)

Particle Swarm: Controlling Velocities

- When using PSO, it is possible for the magnitude of the velocities to become very large.
- Performance can suffer if Vmax is inappropriately set.
- Two methods were developed for controlling the growth of velocities:
 - A dynamically adjusted inertia factor, and
 - A constriction coefficient.

Particle Swarm Optimization: The Inertia Factor

 When the inertia factor is used, the equation for updating velocities is changed to:

$$-v_{id} = \omega^*v_{id} + \phi1*rnd()*(p_{id}-x_{id}) + \phi2*rnd()*(p_{qd}-x_{id});$$

• Where ω is initialized to 1.0 and is gradually reduced over time (measured by cycles through the algorithm).

Particle Swarm Optimization: The Constriction Coefficient

• In 1999, Maurice Clerc developed a constriction Coefficient for PSO.

$$- v_{id} = K[v_{id} + \phi1*rnd()*(p_{id}-x_{id}) + \phi2*rnd()*(p_{gd}-x_{id})];$$

$$- Where K = 2/|2 - \phi - sqrt(\phi^2 - 4\phi)|,$$

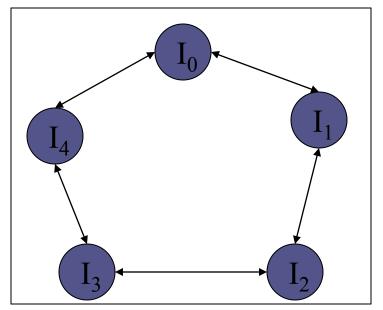
- $\varphi = \varphi 1 + \varphi 2$, and
- $\phi > 4$.

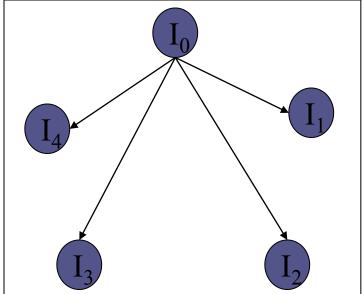
Particle Swarm Optimization: Swarm and Neighborhood Size

- Concerning the swarm size for PSO, as with other ECs there is a trade-off between solution quality and cost (in terms of function evaluations).
- Global neighborhoods seem to be better in terms of computational costs. The performance is similar to the ring topology (or neighborhoods greater than 3).
- There has been a lot of research on the effects of swarm topology on the search behavior of PSO/
 - Varies with the problem

Particle Swarm Optimization: Swarm Topology

- In PSO, there have been two basic topologies used in the literature
 - Ring Topology (neighborhood of 3)
 - Star Topology (global neighborhood)





Particle Swarm Optimization: Particle Update Methods

- There are two ways that particles can be updated:
 - Synchronously
 - Asynchronously
- Asynchronous update allows for newly discovered solutions to be used more quickly

