



بِالْعِلْمِ نَنْتَقِي



CFG

Example

2nd Semester 2020-2021
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Lec #10

Examples

$$L = \{\lambda\}$$

G:

$$S \rightarrow \lambda$$

$$\Sigma = \{a, b\}$$

$$L = \{a, b\}$$

G:

$$S \rightarrow a \mid b$$

$$\Sigma = \{a, b\}$$

$$L = \{\lambda, a, b\}$$

G:

$$S \rightarrow a$$

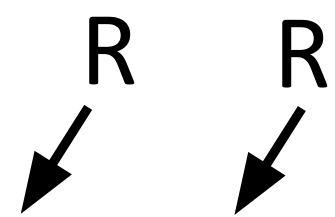
$$S \rightarrow b$$

$$S \rightarrow \lambda$$

G:

$$S \rightarrow a \mid b \mid \lambda$$

$$\Sigma = \{a, b\}$$

$$L = \{aa, ab, ba, bb\} \equiv (a+b)(a+b)$$


G:

$$S \rightarrow aa \mid ab \mid ba \mid bb$$

OR

G:

$$S \rightarrow RR$$

$$R \rightarrow a \mid b$$

$$\Sigma = \{a, b\}$$

$$L = \{a^n \in \{a, b\}^* : n \geq 0\}$$

$$L = \{\lambda, a, aa, aaa, \dots\}$$

$$S \rightarrow aS \mid \lambda$$

G:

$$S \rightarrow Sa \mid \lambda$$

n=0

λ

n=1

λa a

n=2

aa

n=3

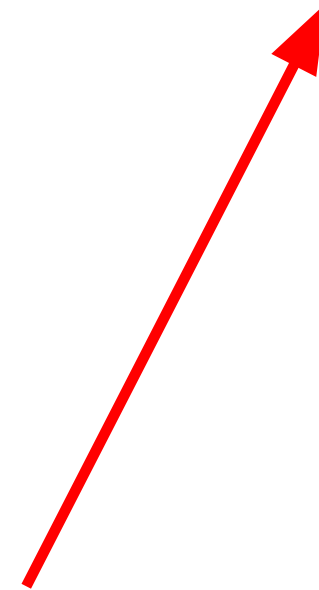
aaa

n=4

aaaa



Red part >>> A



$$\Sigma = \{a, b\}$$

$$L = \{a^n \in \{a, b\}^*: n \geq 1\}$$

$$L = \{a, aa, aaa, \dots\}$$

n=1

a

n=2

aa

n=3

aaa

n=4

aaaa

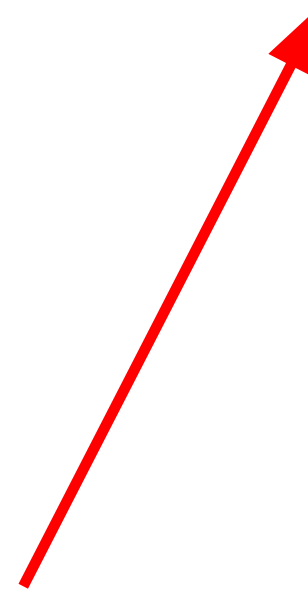


Red part >>> S

$$S \rightarrow aS \mid a$$

G:

$$S \rightarrow Sa \mid a$$



$$\Sigma = \{a, b\}$$

$L = \{w \in \{a, b\}^* : w \text{ contains any number of } a\text{'s and } b\text{'s}\}$

$L = \{\lambda, a, b, aa, ab, ba, bb, aaa, \dots\}$

$(a+b)^*$

G:

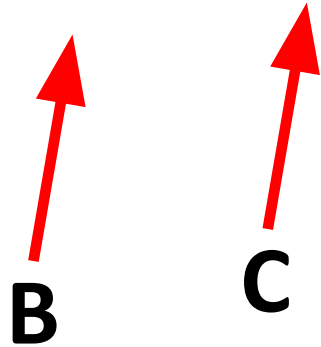
$S \rightarrow aS \mid bS \mid \lambda$

$$\Sigma = \{a, b\}$$

$$L = \{w \in \{a, b\}^*: |w| \text{ is at least } 2\}$$

$$L = \{aa, ab, ba, bb, aaa, \dots\}$$

$$(a+b)(a+b)(a+b)^*$$



G:

$$S \rightarrow BBC$$

$$B \rightarrow a \mid b$$

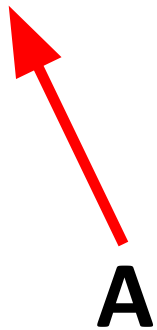
$$C \rightarrow aC \mid bC \mid \lambda$$

$$\Sigma = \{a, b\}$$

$$L = \{w \in \{a, b\}^*: |w| \text{ is at most } 2\}$$

$$L = \{\lambda, a, b, aa, ab, ba, bb\}$$

$$(\lambda + a + b) (\lambda + a + b)$$



A

G:

$$S \rightarrow AA$$

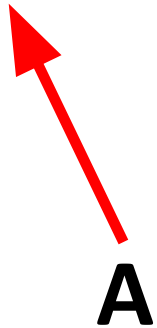
$$A \rightarrow a \mid b \mid \lambda$$

$$\Sigma = \{a, b\}$$

$$L = \{w \in \{a, b\}^*: w \text{ starts with } a \text{ and ends with } b\}$$

$$L = \{ab, aab, abb, aaab, \dots\}$$

$$a(a+b)^*b$$



G:

$$S \rightarrow aAb$$

$$A \rightarrow aA \mid bA \mid \lambda$$

$$\Sigma = \{a, b\}$$

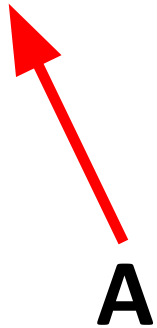
$L = \{w \in \{a, b\}^* : w \text{ starts and ends with different symbols} \}$

$L = \{ab, ba, aab, baa, aaab, \dots\}$

$a(a+b)^*b + b(a+b)^*a$ G:

$S \rightarrow aAb \mid bAa$

$A \rightarrow aA \mid bA \mid \lambda$



$$\Sigma = \{a, b\}$$

$$L = \{w \in \{a, b\}^* : |w| \text{ is even}\}$$

$$L = \{\lambda, ab, aa, ab, bb, aaaa, \dots\}$$

$$((a+b)(a+b))^*$$



B

G:

$$S \rightarrow AS \mid \lambda$$

$$A \rightarrow BB$$

$$B \rightarrow a \mid b$$

$$\Sigma = \{a, b\}$$

$$L = \{a^n b^n \in \{a, b\}^* : n \geq 0\}$$

$$L = \{\lambda, ab, aabb, aaabbb, \dots\}$$

G:

$$S \rightarrow aSb \mid \lambda$$

n=0

λ

n=1

ab

n=2

aabb

n=3

aaabbb

n=4

aaaabbbb

S



$$\Sigma = \{a, b\}$$

$$L = \{ww^R : w \in \{a, b\}^*\}$$

$$W = aaba \quad w^R = abaa \quad ww^R = aabaabaa$$

G:

$$S \rightarrow aSa \mid bSb \mid \lambda$$

$$\Sigma = \{a, b\}$$

$$L = \{a^n b^m \in \{a, b\}^*: n, m \geq 1\}$$

ab, abb, aaaabb

$$L = L1 L2$$

$$L1 = \{a^n \in \{a, b\}^*: n \geq 1\}$$

$$L2 = \{b^m \in \{a, b\}^*: m \geq 1\}$$

G1:

$$A \rightarrow aA \mid a$$

G2:

$$B \rightarrow bB \mid b$$

G:

$$S \rightarrow AB$$

$$A \rightarrow aA \mid a$$

$$B \rightarrow bB \mid b$$

$$\Sigma = \{a, b\}$$

$$L = \{a^n b^n c^m \in \{a, b\}^*: n, m \geq 1\}$$

abc, abcc, aabbccccc

$$L = L1 L2$$

$$L1 = \{a^n b^n \in \{a, b\}^*: n \geq 1\}$$

$$L2 = \{c^m \in \{a, b\}^*: m \geq 1\}$$

G1:

$$A \rightarrow aAb \mid ab$$

G2:

$$B \rightarrow cB \mid c$$

G:

$$S \rightarrow AB$$

$$A \rightarrow aAb \mid ab$$

$$B \rightarrow cB \mid c$$

$$\Sigma = \{a, b\}$$

$$L = \{a^n b^m c^n \in \{a, b\}^* : n, m \geq 1\}$$

abc, abbc, aabbbbcc

G:

$$S \rightarrow aSc \mid aAc$$

$$A \rightarrow bA \mid b$$

n=1

abc

n=2

aabcc

n=3

aaabbccc

n=4

aaaabbbcccc

n=5

aaaaabccccc

$$\Sigma = \{a, b\}$$

$$L = \{a^n b^n c^m d^m \in \{a, b\}^*: n, m \geq 1\}$$

abcd, aabbcd, aabbccdd

$$L = L1 \ L2$$

$$L1 = \{a^n b^n \in \{a, b\}^*: n \geq 1\}$$

$$L2 = \{c^m d^m \in \{a, b\}^*: m \geq 1\}$$

G1:

$$A \rightarrow aAb \mid ab$$

G2:

$$B \rightarrow cBd \mid cd$$

G:

$$S \rightarrow AB$$

$$A \rightarrow aAb \mid ab$$

$$B \rightarrow cBd \mid cd$$

$$\Sigma = \{a, b\}$$

$$L = \{a^n b^{2n} \in \{a, b\}^* : n \geq 1\}$$

abb, aabbbb, ...

G:

$$S \rightarrow aSbb \mid abb$$

$$\Sigma = \{a, b\}$$

$$L = \{a^n b^m c^m d^n \in \{a, b\}^*: n, m \geq 1\}$$

abc, abbc, aabbbbcc

G:

$$S \rightarrow aSd \mid aAd$$

$$A \rightarrow bAc \mid bc$$

