

## Group Assignment: PFG Bank (aka Capital One): Credit Card Design (4-8 hours)

● Graded

### Group

Gaetan Rieben

Albara Altoukhi

Mohannad Alsaegh

...and 1 more

[✎ View or edit group](#)

### Total Points

30 / 35 pts

### Autograder Score

0.0 / 0.0

### Question 2

1. Why does Customer Lifetime Value vary with BK score? Why does Customer Lifetime Value vary by product? 3 / 3 pts

✓ - 0 pts Correct

### Question 3

2. Are predictive models estimated on historical data useful in this case? If so, why? If not, why not? 4 / 4 pts

✓ - 0 pts Correct

### Question 4

3. Is there a "best product" that will likely be preferred by all customers? If so, what is it? 3 / 3 pts

✓ - 0 pts Correct

### Question 5

4. Describe and justify your testing strategy 10 / 10 pts

✓ - 0 pts Correct

### Question 6

5. Performance 7 / 10 pts

✓ + 7 pts Performance score

### Question 7

6. Usage of Gen AI 3 / 5 pts

✓ + 3 pts Solid discussion of your teams Gen AI approach

## Autograder Results

This assignment does not have an autograder configured.

## Submitted Files

▼ .github/workflows/run-code.yml		Download
1	name: GitHub Case - PFG Bank (CI)	
2	on: [push, pull_request, fork]	
3	jobs:	
4	build:	
5	runs-on: self-hosted	
6	container:	
7	image: vnijs/rsm-msba-intel:2.9.2	
8	options: --user root	
9	steps:	
10	- uses: actions/checkout@v2	
11	- name: Upgrade pyrsn	
12	run: pip install --upgrade pyrsn	
13	- name: Evaluate notebook	
14	run: jupyter nbconvert --execute --to html pfg-bank.ipynb	
▼ .gitignore		Download
1	.Rproj.user	
2	.Rhistory	
3	.RData	
4	.Ruserdata	
5	.DS_Store	
6	*.pyc	
▼ data/exhibits.xls		Download
1	Binary file hidden. You can download it using the button above.	
▼ data/test.xlsx		Download
1	Binary file hidden. You can download it using the button above.	

Attributes and levels:

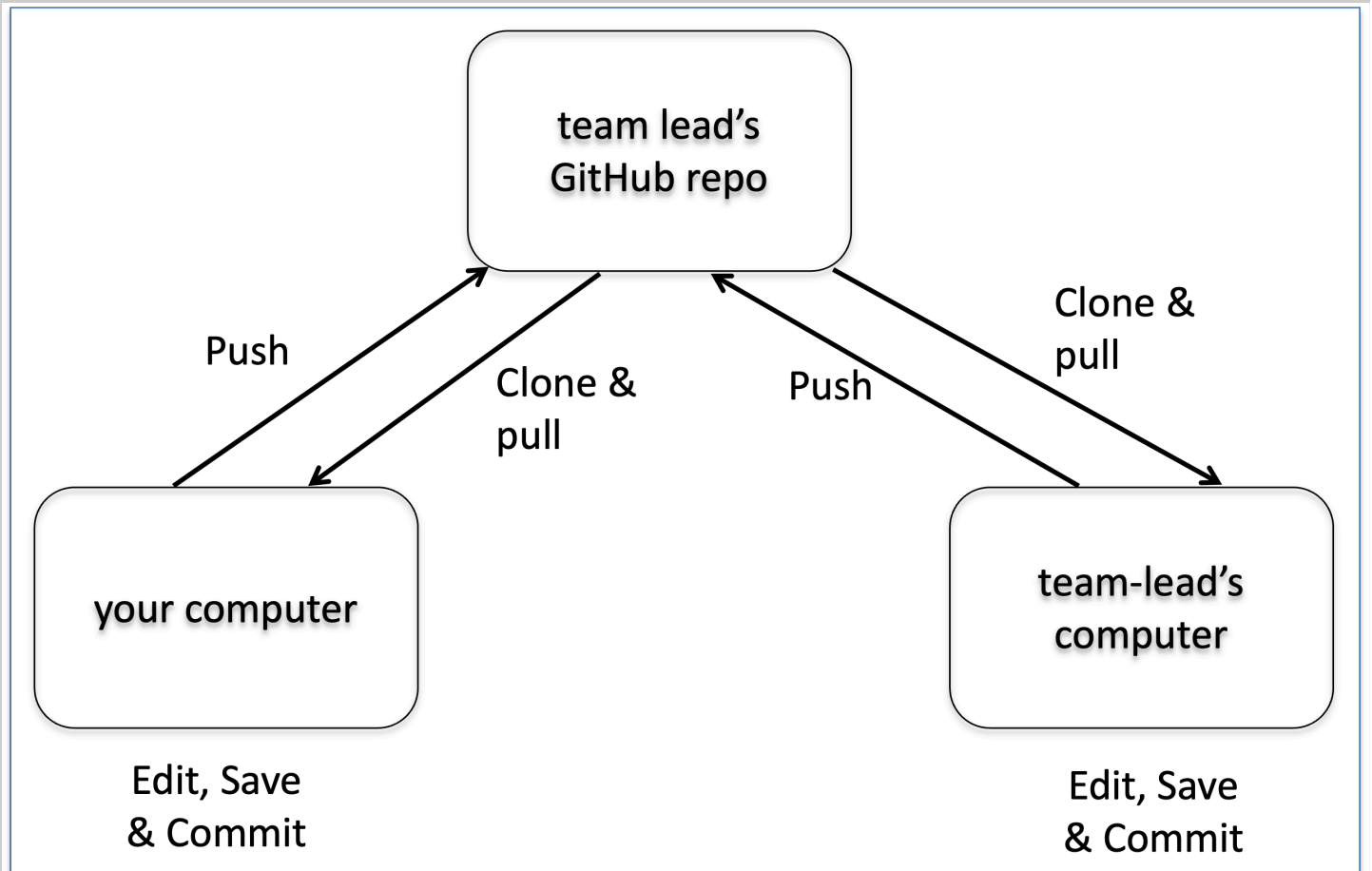
APR: 14.9, 16.8, 19.8

Fee: Yes, No

rate: fixed, variable

Design efficiency:

Trials	D-efficiency	Balanced
5	0.135	FALSE
6	0.819	TRUE
7	0.670	FALSE
8	0.819	FALSE
9	0.705	FALSE
10	0.651	FALSE
11	0.565	FALSE
12	1.000	TRUE



## Partial factorial design correlations:

**\*\* Note: Variables are assumed to be ordinal \*\***

	APR	Fee	rate
APR	1	0.0	0.0
Fee	0	1.0	-0.5
rate	0	-0.5	1.0

Summary

## Partial factorial design:

trial	APR	Fee	rate
2	14.9	Yes	variable
3	14.9	No	fixed
5	16.8	Yes	fixed
8	16.8	No	variable
10	19.8	Yes	variable
11	19.8	No	fixed

 Analyze Final Results

## Round 1 Results

Solicitation Development	\$15,000	Round 1 Number Sent	66,312
Mailing Costs	\$800	Round 1 Number of Responses	1,152
Cost of Pieces Mailed	\$33,156	Total Response Value	\$55,542
Total Cost of Mailing	\$48,956		
		Total Profit	\$6,586

## Round 2 Results

		Round 2 Number Sent	683,688
Mailing Costs	\$800	Round 2 Number of Responses	23,989
Cost of Pieces Mailed	\$341,844	Total Response Value	\$1,011,378
Total Cost of Mailing	\$342,644		
		Total Profit	\$668,734

## Cumulative Results

Solicitation Development	\$15,000	Round 1 Number of Responses	1,152
Mailing Costs	\$1,600	Round 2 Number of Responses	23,989
Cost of Pieces Mailed	\$375,000	Total Response Value	\$1,066,920
Total Cost of Mailing	\$391,600		
		Total Profit	\$675,320

## Summary

**Menu: Design > Sample****Tool: Sample size (compare)**☐ Mean ☒ Proportion

Sample size (n1):

Sample size (n2):

Proportion 1 (p1):

Proportion 2 (p2):

Confidence level:

Power:

Alternative hypothesis:

☐ Show plot

Sample size calculation for comparison of proportions

Sample size 1 : 1,842

Sample size 2 : 1,842

Total sample size: 3,684

Proportion 1 : 0.018

Proportion 2 : 0.0305

Effect size : 0.0819456

Confidence level : 0.95

Power : 0.8

Alternative : less

Your browser does not support PDF previews. You can [download the file instead.](#)

## PFG Bank: Credit Card Design

- Team-lead GitHub userid: rsm-xyz123
- Group name: Group 5
- Team member names:
  - Gaetan Rieben
  - Albara Altoukhi
  - Mohib Mohyuddin
  - Mohannad Alsaegh

## Setup

Please complete this python notebook with your group by answering the questions in `pfg-bank-msba.pdf`.

Create a Notebook with all your results and comments and push the Notebook to GitHub when your team is done. Make sure to connect the GitHub repo to GradeScope before the due date. All results MUST be reproducible (i.e., the TA and I must be able to recreate your output from the Jupyter Notebook without changes or errors). This means that you should NOT use any python-packages that are not part of the RSM-MSBA docker container.

Note: Please do not install any packages as part of your Jupyter Notebook submission

This is a group assignment and you will be using Git and GitHub. If two people edit the same file at the same time you could get what is called a "merge conflict". This is not something serious but you should realize that Git will not decide for you who's changes to accept. The team-lead will have to determine the edits to use. To avoid merge conflicts, **always** "pull" changes to the repo before you start working on any files. Then, when you are done, save and commit your changes, and then push them to GitHub. Make "pull first" a habit!

If multiple people are going to work on the assignment at the same time I recommend you work in different notebooks. You can then `%run ...` these "sub" notebooks from the main assignment file. You can see an example of this in action below for the `model1.ipynb` notebook

Some group work-flow tips:

- Pull, edit, save, stage, commit, and push



- Schedule who does what and when
- Try to avoid working simultaneously on the same file
- If you are going to work simultaneously, do it in different notebooks, e.g.,
  - model1.ipynb, question1.ipynb, etc.
- Use the `%run ...` command to bring different pieces of code together into the main jupyter notebook
- Put python functions in modules that you can import from your notebooks. See the example below for the `example` function defined in `utils/functions.py`

A graphical depiction of the group work-flow is shown below:



```
In [1]: import pandas as pd
import pyrsm as rsm
rsm.__version__ # should be 0.9.23 or newer
```

```
Out [1]: '0.9.24'
```

## Question answers

Why does Customer Lifetime Value vary with BK score? Why does Customer Lifetime Value vary by product? (See Exhibit 2 to help answer these questions)

Banks limit exposure to high bk/credit risk customers by offering them products with higher interest rates, lower credit limits, or more stringent repayment terms which impacts their CLV. Also, banks are typically conservative; minimize potential losses through management of the account rather than maximizing revenue through upselling or cross-selling additional products and services. Banks incur additional cost for defaulting customers which includes collections, account monitoring, and legal proceedings which can diminish the net CLV overtime. Finally, customers with lower scores may exhibit more cautious financial behavior, affecting their utilization of banking products and services. Conversely, those with better scores may be more financially active, using a broader range of products and engaging in more transactions, potentially increasing their CLV.

In [12]:

```
###Loading past data
import pandas as pd
import pyrsm as rsm

exh1 = pd.read_excel('data/exhibits.xls', sheet_name='exhibit1', dtype=
{'apr':'category','fixed_var':'category', 'annual_fee':'category', 'visamc':'category',
'nr_mailed':'int', 'non_resp':'int', 'resp':'int', 'bk_score':'category', 'average_bk':
'category'})
```

In [13]:

```
exh_melt = pd.melt(
    exh1,
    id_vars=['apr', 'fixed_var', 'annual_fee', 'bk_score'],
    value_vars=['resp', 'non_resp'],
    var_name='resp',
    value_name='freq'
)
```

In [14]:

exh\_melt

Out [14]:

	apr	fixed_var	annual_fee	bk_score	resp	freq
0	16.8	Fixed	20	200	resp	1533
1	16.8	Fixed	0	200	resp	2896
2	19.8	Fixed	20	200	resp	590
3	19.8	Fixed	0	200	resp	2052
4	14.9	Fixed	20	250	resp	4329
5	14.9	Variable	20	250	resp	3004
6	16.8	Fixed	20	250	resp	2983
7	19.8	Fixed	20	250	resp	175
8	16.8	Fixed	0	250	resp	2516
9	19.8	Fixed	0	250	resp	2115
10	14.9	Fixed	20	150	resp	1761
11	14.9	Fixed	0	150	resp	2451
12	14.9	Variable	20	150	resp	708
13	16.8	Fixed	20	150	resp	373
14	16.8	Fixed	20	200	non_resp	165467
15	16.8	Fixed	0	200	non_resp	78104
16	19.8	Fixed	20	200	non_resp	142410
17	19.8	Fixed	0	200	non_resp	97948
18	14.9	Fixed	20	250	non_resp	172671
19	14.9	Variable	20	250	non_resp	166996
20	16.8	Fixed	20	250	non_resp	252017
21	19.8	Fixed	20	250	non_resp	34825
22	16.8	Fixed	0	250	non_resp	62484
23	19.8	Fixed	0	250	non_resp	92885
24	14.9	Fixed	20	150	non_resp	80239
25	14.9	Fixed	0	150	non_resp	47549

```
26 14.9 Variable      20   150 non_resp 49292
27 16.8   Fixed       20   150 non_resp 49627
```

In [24]:

```
lr = rsm.model.logistic(
    data={'exh_melt': exh_melt},
    rvar='resp',
    lev='resp',
    evar=['apr', 'fixed_var', 'annual_fee', 'bk_score'],
    weights='freq')
```

In [26]:

```
lr.summary()
```

Logistic regression (GLM)

Data : exh\_melt

Response variable : resp

Level : resp

Explanatory variables: apr, fixed\_var, annual\_fee, bk\_score

Weights used : freq

Null hyp.: There is no effect of x on resp

Alt. hyp.: There is an effect of x on resp

	OR	OR%	coefficient	std.error	z.value	p.value
Intercept	0.060	-94.0%	-2.81	0.016	-175.303	< .001 ***
apr[16.8]	0.471	-52.9%	-0.75	0.019	-39.875	< .001 ***
apr[19.8]	0.257	-74.3%	-1.36	0.024	-57.254	< .001 ***
fixed_var[Variable]	0.741	-25.9%	-0.30	0.021	-14.336	< .001 ***
annual_fee[20]	0.290	-71.0%	-1.24	0.015	-84.443	< .001 ***
bk_score[200]	1.232	23.2%	0.21	0.024	8.519	< .001 ***
bk_score[250]	1.425	42.5%	0.35	0.019	18.388	< .001 ***

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Pseudo R-squared (McFadden): 0.033

Pseudo R-squared (McFadden adjusted): 0.033

Area under the RO Curve (AUC): 0.662

Log-likelihood: -132938.55, AIC: 265891.101, BIC: 265976.74

Chi-squared: 9185.877, df(6), p.value < 0.001

Nr obs: 1,520,000

In [27]:

```
dct = rsm.levels_list(exh_melt[['apr', 'fixed_var', 'annual_fee', 'bk_score']])
dct

exh1_mult_expand = rsm.expand_grid(dct)
exh1_mult_expand
```

Out [27]:

```
apr fixed_var annual_fee bk_score
0 16.8   Fixed      20      200
```

1	16.8	Fixed	20	250
2	16.8	Fixed	20	150
3	16.8	Fixed	0	200
4	16.8	Fixed	0	250
5	16.8	Fixed	0	150
6	16.8	Variable	20	200
7	16.8	Variable	20	250
8	16.8	Variable	20	150
9	16.8	Variable	0	200
10	16.8	Variable	0	250
11	16.8	Variable	0	150
12	19.8	Fixed	20	200
13	19.8	Fixed	20	250
14	19.8	Fixed	20	150
15	19.8	Fixed	0	200
16	19.8	Fixed	0	250
17	19.8	Fixed	0	150
18	19.8	Variable	20	200
19	19.8	Variable	20	250
20	19.8	Variable	20	150
21	19.8	Variable	0	200
22	19.8	Variable	0	250
23	19.8	Variable	0	150
24	14.9	Fixed	20	200
25	14.9	Fixed	20	250
26	14.9	Fixed	20	150
27	14.9	Fixed	0	200
28	14.9	Fixed	0	250
29	14.9	Fixed	0	150
30	14.9	Variable	20	200
31	14.9	Variable	20	250
32	14.9	Variable	20	150
33	14.9	Variable	0	200
34	14.9	Variable	0	250
35	14.9	Variable	0	150

In [28]:

```
exh1_mult_expand['pred'] = lr.predict(data=exh1_mult_expand)['prediction']
exh1_mult_expand
```

Out [28]:

	apr	fixed_var	annual_fee	bk_score	pred
0	16.8	Fixed	20	200	0.010029
1	16.8	Fixed	20	250	0.011581
2	16.8	Fixed	20	150	0.008156
3	16.8	Fixed	0	200	0.033799
4	16.8	Fixed	0	250	0.038884
5	16.8	Fixed	0	150	0.027609
6	16.8	Variable	20	200	0.007448
7	16.8	Variable	20	250	0.008604
8	16.8	Variable	20	150	0.006054
9	16.8	Variable	0	200	0.025257

10	16.8	Variable	0	250	0.029096
11	16.8	Variable	0	150	0.020598
12	19.8	Fixed	20	200	0.005496
13	19.8	Fixed	20	250	0.006351
14	19.8	Fixed	20	150	0.004466
15	19.8	Fixed	0	200	0.018725
16	19.8	Fixed	0	250	0.021593
17	19.8	Fixed	0	150	0.015252
18	19.8	Variable	20	200	0.004077
19	19.8	Variable	20	250	0.004712
20	19.8	Variable	20	150	0.003312
21	19.8	Variable	0	200	0.013938
22	19.8	Variable	0	250	0.016084
23	19.8	Variable	0	150	0.011342
24	14.9	Fixed	20	200	0.021044
25	14.9	Fixed	20	250	0.024258
26	14.9	Fixed	20	150	0.017148
27	14.9	Fixed	0	200	0.069096
28	14.9	Fixed	0	250	0.079057
29	14.9	Fixed	0	150	0.056822
30	14.9	Variable	20	200	0.015673
31	14.9	Variable	20	250	0.018083
32	14.9	Variable	20	150	0.012759
33	14.9	Variable	0	200	0.052115
34	14.9	Variable	0	250	0.059786
35	14.9	Variable	0	150	0.042719

In [34]:

```
# Convert the list of dictionaries to a pandas DataFrame
df = pd.DataFrame(exh1_mult_expand)

# Filter the DataFrame for bk_score = 200 and find the row with the maximum
pred value
filtered_df = df[df['bk_score'] == 200]
max_pred_row_alternative = filtered_df.loc[filtered_df['pred'].idxmax()]
print(max_pred_row_alternative)
```

```
apr          14.9
fixed_var    Fixed
annual_fee      0
bk_score      200
pred      0.069096
Name: 27, dtype: object
```

In [35]:

```
# Filter the DataFrame for bk_score = 200 and find the row with the maximum
pred value
filtered_df = df[df['bk_score'] == 250]
max_pred_row_alternative = filtered_df.loc[filtered_df['pred'].idxmax()]
print(max_pred_row_alternative)
```

```
apr          14.9
fixed_var    Fixed
annual_fee    0
bk_score     250
pred         0.079057
Name: 28, dtype: object
```

In [36]:

```
# Filter the DataFrame for bk_score = 200 and find the row with the maximum
pred value
filtered_df = df[df['bk_score'] == 200]
max_pred_row_alternative = filtered_df.loc[filtered_df['pred'].idxmax()]
print(max_pred_row_alternative)
```

```
apr          14.9
fixed_var    Fixed
annual_fee    0
bk_score     150
pred         0.056822
Name: 29, dtype: object
```

Based on the logistic regression conducted on previous data, we can see that the offering should be the same for each BK\_score customers. As far as we can see, the lowest APR, with a fixed interest rate and no annual fee is the best offering that maximize the likelihood of conversion. However, it might be useful to check if those offering are the one who maximize profitability (CLV \* probability).

Although this product might not be the highest profitability, this product is preferred by all customers as per this past data analysis ( *Answer to question 3* ). This makes sense as this product has the lowest (and fixed) interest rate with no annual fee. This is by far the most affordable product for the clients. It might be interesting to compare this offering with the ones from competitors.

## Our testing strategy

Given the fact that these mailing has been sent in the past but the situation has evolved, we believe that the customer responses might has changed given the market. Indeed, many factors beyond PFG's control had changed and could affect customers' responses. Several of PFG's competitors had launched major marketing campaigns during the holiday season. One competitor was aggressively marketing no-fee cards and a second was offering a substantial rebate program. (Answer question 2). Furthermore, the data are not representative of experiments/design nuances. The

experiment design was not balanced. For instance, in September, they have sent offers only with a fixed rate. They haven't tried with variable rate. As such, we want to design the experiments properly.

Therefore, we are willing to conduct a test mailing and analyze the results from it. But first, as we want to design the most optimal one, we want to use a partial factor design that would allow us to select the most balanced offerings. To do so, we use radiant



From the result, we can see that only 2 solutions might be balanced. The one with 6 trials, or the one with 12 trials. As such, as we want to minimize cost, we decided to select the one with a D-Efficiency closer to 0.8. We will go with 6 trials. See below the product designs to be tested



## Calculate sample size

In my opinion, we should check the response rate of previous mailings, and set a higher response rate that we are willing to achieve in order to compute the sample size for our tests

```
In [40]: resp = exh_melt[exh_melt['resp']=='resp']  
non_resp = exh_melt[exh_melt['resp']=='non_resp']
```

```
In [43]: total_resp = sum(resp['freq'])  
total_send = sum(resp['freq']) + sum(non_resp['freq'])
```

```
In [45]: response_rate = total_resp / total_send  
print(response_rate)
```

```
0.018082894736842107
```

The current response rate is 1.80%. We will check what response rate we would need considering the CLV's. As such, we plan to take the average CLV across all products and all BK scores and use this average to compute the breakeven

```
In [169]: exh2 = pd.read_excel('data/exhibits.xls', sheet_name='exhibit2', dtype=
{'offer':'category', 'apr':'category', 'fixed_var':'category', 'annual_fee':'category',
'clv150':'int', 'clv200':'int', 'clv250':'int'})
clv150, clv200, clv250= exh2[['clv150', 'clv200', 'clv250']].mean()
clv150
```

Out [169]: 95.16666666666667

```
In [170]: mean = (clv150 + clv200 + clv250) / 3
mean
```

Out [170]: 71.83333333333333

```
In [171]: fixed = 10000+1600+6000
cost_per_customer = fixed/750000
breakeven = cost_per_customer + 0.50 / mean
breakeven
```

Out [171]: 0.03042722351121423

As per the analysis above, we should go from a response rate of 1.80% to 3.05%. Using this number, we use radiants to estimate the sample size for our test mailing



Now that we have estimated the sample size to launch our test, we have to decide if we send a test mailing to everyone or only a few product offerings. As per our idea, we want to produce the most efficient test campaign at the lowest cost. Hence, we will send a test campaign with our 6 product design to each of the BK\_score, with a sample size as above.

## Results from the test

```
In [127]: test = pd.read_excel('data/test.xlsx')
```

```
In [128]: test.head()
```

Out [128]:

	apr	fixed_var	annual_fee	sent_150	responses_150	sent_200	\
0	14.9	Variable	Yes	3684	37	3684	



1	14.9	Fixed	No	3684	144	3684
2	16.8	Fixed	Yes	3684	9	3684
3	16.8	Variable	No	3684	50	3684
4	19.8	Variable	Yes	3684	14	3684

	responses_200	sent_250	responses_250
0	51	3684	63
1	170	3684	228
2	30	3684	23
3	74	3684	76
4	13	3684	12

In [129]:

```
# Melting the DataFrame
sent_melted = test.melt(id_vars=["apr", "fixed_var", "annual_fee"], value_vars=
["sent_150", "sent_200", "sent_250"], var_name="bk_score", value_name="sent")
responses_melted = test.melt(id_vars=["apr", "fixed_var", "annual_fee"],
value_vars=["responses_150", "responses_200", "responses_250"],
var_name="bk_score", value_name="responses")

# Adjusting the bk_score values to reflect just the score
sent_melted['bk_score'] = sent_melted['bk_score'].str.replace('sent_', '')
responses_melted['bk_score'] =
responses_melted['bk_score'].str.replace('responses_', '')

# Merging the melted DataFrames
test = pd.merge(sent_melted, responses_melted, on=["apr", "fixed_var",
"annual_fee", "bk_score"])

print(test)
```

	apr	fixed_var	annual_fee	bk_score	sent	responses
0	14.9	Variable	Yes	150	3684	37
1	14.9	Fixed	No	150	3684	144
2	16.8	Fixed	Yes	150	3684	9
3	16.8	Variable	No	150	3684	50
4	19.8	Variable	Yes	150	3684	14
5	19.8	Fixed	No	150	3684	51
6	14.9	Variable	Yes	200	3684	51
7	14.9	Fixed	No	200	3684	170
8	16.8	Fixed	Yes	200	3684	30
9	16.8	Variable	No	200	3684	74
10	19.8	Variable	Yes	200	3684	13
11	19.8	Fixed	No	200	3684	48
12	14.9	Variable	Yes	250	3684	63
13	14.9	Fixed	No	250	3684	228
14	16.8	Fixed	Yes	250	3684	23
15	16.8	Variable	No	250	3684	76
16	19.8	Variable	Yes	250	3684	12
17	19.8	Fixed	No	250	3684	59

```
In [130]: test['no_resp'] = test['sent'] - test['responses']
```

```
In [131]: test
```

```
Out [131]:      apr fixed_var annual_fee bk_score  sent  responses  no_resp
0  14.9  Variable      Yes    150 3684     37    3647
1  14.9   Fixed      No    150 3684    144    3540
2  16.8   Fixed     Yes    150 3684     9    3675
3  16.8  Variable      No    150 3684     50    3634
4  19.8  Variable     Yes    150 3684     14    3670
5  19.8   Fixed      No    150 3684     51    3633
6  14.9  Variable     Yes    200 3684     51    3633
7  14.9   Fixed      No    200 3684    170    3514
8  16.8   Fixed     Yes    200 3684     30    3654
9  16.8  Variable      No    200 3684     74    3610
10 19.8  Variable     Yes    200 3684     13    3671
11 19.8   Fixed      No    200 3684     48    3636
12 14.9  Variable     Yes    250 3684     63    3621
13 14.9   Fixed      No    250 3684    228    3456
14 16.8   Fixed     Yes    250 3684     23    3661
15 16.8  Variable      No    250 3684     76    3608
16 19.8  Variable     Yes    250 3684     12    3672
17 19.8   Fixed      No    250 3684     59    3625
```

```
In [132]: test = test.melt(id_vars=["apr", "fixed_var", "annual_fee", "bk_score"], value_vars=
["no_resp", "responses"], var_name="resp", value_name="freq")
```

```
In [133]: test
```

```
Out [133]:      apr fixed_var annual_fee bk_score  resp  freq
0  14.9  Variable      Yes    150  no_resp 3647
1  14.9   Fixed      No    150  no_resp 3540
2  16.8   Fixed     Yes    150  no_resp 3675
3  16.8  Variable      No    150  no_resp 3634
4  19.8  Variable     Yes    150  no_resp 3670
5  19.8   Fixed      No    150  no_resp 3633
6  14.9  Variable     Yes    200  no_resp 3633
7  14.9   Fixed      No    200  no_resp 3514
8  16.8   Fixed     Yes    200  no_resp 3654
9  16.8  Variable      No    200  no_resp 3610
10 19.8  Variable     Yes    200  no_resp 3671
11 19.8   Fixed      No    200  no_resp 3636
12 14.9  Variable     Yes    250  no_resp 3621
13 14.9   Fixed      No    250  no_resp 3456
14 16.8   Fixed     Yes    250  no_resp 3661
15 16.8  Variable      No    250  no_resp 3608
```

16	19.8	Variable	Yes	250	no_resp	3672
17	19.8	Fixed	No	250	no_resp	3625
18	14.9	Variable	Yes	150	responses	37
19	14.9	Fixed	No	150	responses	144
20	16.8	Fixed	Yes	150	responses	9
21	16.8	Variable	No	150	responses	50
22	19.8	Variable	Yes	150	responses	14
23	19.8	Fixed	No	150	responses	51
24	14.9	Variable	Yes	200	responses	51
25	14.9	Fixed	No	200	responses	170
26	16.8	Fixed	Yes	200	responses	30
27	16.8	Variable	No	200	responses	74
28	19.8	Variable	Yes	200	responses	13
29	19.8	Fixed	No	200	responses	48
30	14.9	Variable	Yes	250	responses	63
31	14.9	Fixed	No	250	responses	228
32	16.8	Fixed	Yes	250	responses	23
33	16.8	Variable	No	250	responses	76
34	19.8	Variable	Yes	250	responses	12
35	19.8	Fixed	No	250	responses	59

## Logistic regression on the latest test

In [134]: `test['apr'] = test['apr'].astype('category')`

In [149]: `evan=['apr', 'fixed_var', 'annual_fee', 'bk_score']`

In [151]: `ivar=[f'{e}:bk_score' for e in evan if e != 'bk_score']`  
`ivar`

Out [151]: `['apr:bk_score', 'fixed_var:bk_score', 'annual_fee:bk_score']`

In [155]: `lr = rsm.model.logistic(  
data={'test': test},  
rvar='resp',  
lev='responses',  
evan=['apr', 'fixed_var', 'annual_fee', 'bk_score'],  
weights='freq')`

In [156]: `lr.summary()`

Logistic regression (GLM)  
Data : test

Response variable : resp  
 Level : responses  
 Explanatory variables: apr, fixed\_var, annual\_fee, bk\_score  
 Weights used : freq  
 Null hyp.: There is no effect of x on resp  
 Alt. hyp.: There is an effect of x on resp

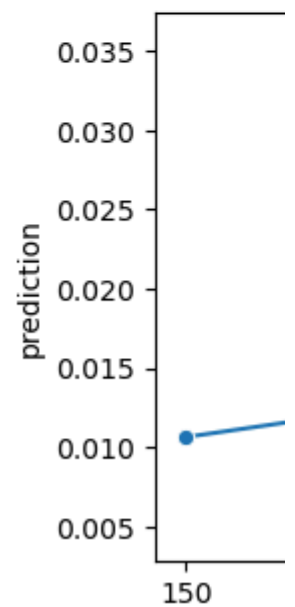
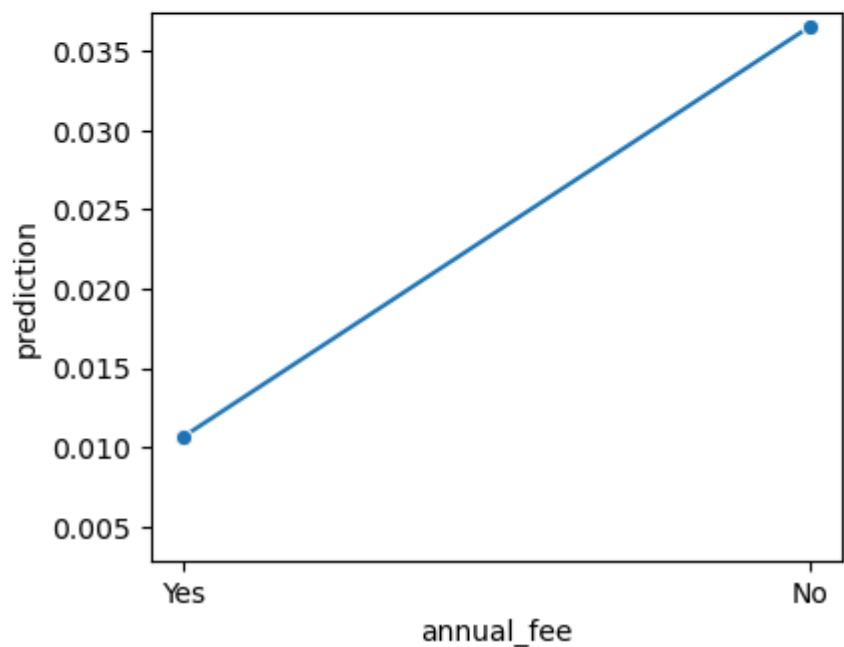
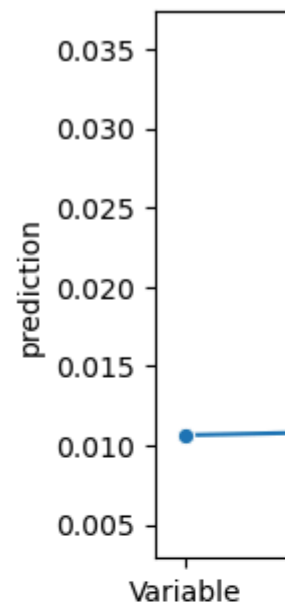
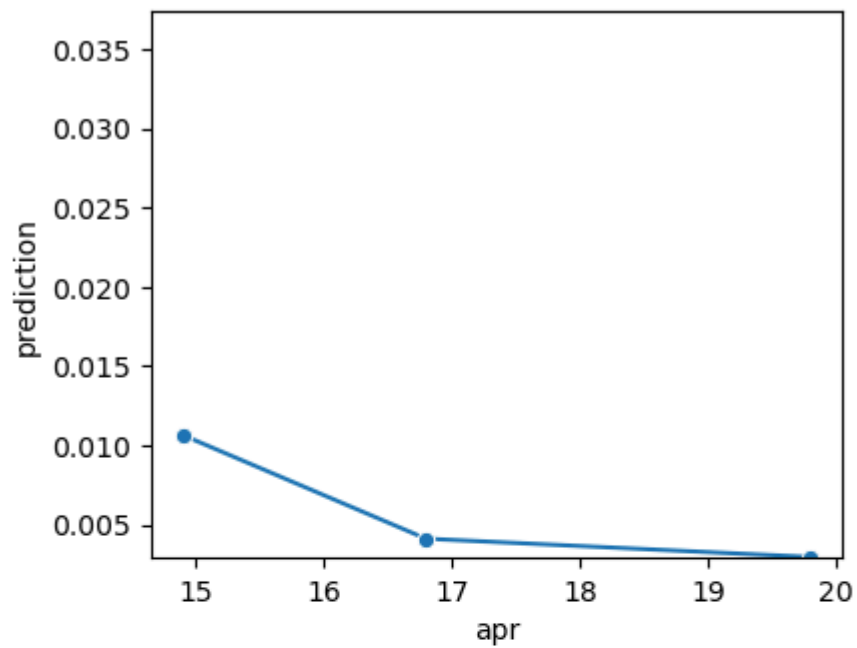
	OR	OR%	coefficient	std.error	z.value	p.value	
Intercept	0.041	-95.9%	-3.20	0.065	-48.807	< .001	***
apr[16.8]	0.383	-61.7%	-0.96	0.086	-11.167	< .001	***
apr[19.8]	0.275	-72.5%	-1.29	0.082	-15.815	< .001	***
fixed_var[Variable]	0.927	-7.3%	-0.08	0.084	-0.906	0.365	
annual_fee[Yes]	0.284	-71.6%	-1.26	0.084	-15.025	< .001	***
bk_score[200]	1.274	27.4%	0.24	0.078	3.118	0.002	**
bk_score[250]	1.531	53.1%	0.43	0.075	5.685	< .001	***

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Pseudo R-squared (McFadden): 0.068  
 Pseudo R-squared (McFadden adjusted): 0.067  
 Area under the RO Curve (AUC): 0.726  
 Log-likelihood: -5415.446, AIC: 10844.892, BIC: 10908.607  
 Chi-squared: 790.793, df(6), p.value < 0.001  
 Nr obs: 66,312

In [159]:

```
lr.plot('pred')
```



We want to try interactions to see if it has an influence on the logistic regression

In [157]:

```
lr_ivar = rsm.model.logistic(
    data={'test': test},
    rvar='resp',
    lev='responses',
    evar=['apr', 'fixed_var', 'annual_fee', 'bk_score'],
    ivar=ivar,
    weights='freq')
```

In [158]:

```
lr_ivar.summary()
```

Logistic regression (GLM)

Data : test

Response variable : resp

Level : responses

Explanatory variables: apr, fixed\_var, annual\_fee, bk\_score

Weights used : freq

Null hyp.: There is no effect of x on resp

Alt. hyp.: There is an effect of x on resp

	OR	OR%	coefficient	std.error	z.value	p.value	
Intercept	0.040	-96.0%	-3.21	0.083	-38.745	< .001	***
apr[16.8]	0.284	-71.6%	-1.26	0.202	-6.243	< .001	***
apr[19.8]	0.351	-64.9%	-1.05	0.146	-7.168	< .001	***
fixed_var[Variable]	1.197	19.7%	0.18	0.198	0.910	0.363	
annual_fee[Yes]	0.213	-78.7%	-1.55	0.198	-7.809	< .001	***
bk_score[200]	1.200	20.0%	0.18	0.113	1.617	0.106	
bk_score[250]	1.648	64.8%	0.50	0.106	4.702	< .001	***
apr[16.8]:bk_score[200]	1.762	76.2%	0.57	0.242	2.337	0.019	*
apr[19.8]:bk_score[200]	0.763	-23.7%	-0.27	0.206	-1.311	0.19	
apr[16.8]:bk_score[250]	1.213	21.3%	0.19	0.245	0.789	0.43	
apr[19.8]:bk_score[250]	0.666	-33.4%	-0.41	0.198	-2.053	0.04	*
fixed_var[Variable]:bk_score[200]	0.705	-29.5%	-0.35	0.237	-1.476	0.14	
fixed_var[Variable]:bk_score[250]	0.766	-23.4%	-0.27	0.240	-1.110	0.267	
annual_fee[Yes]:bk_score[200]	1.586	58.6%	0.46	0.237	1.946	0.052	.
annual_fee[Yes]:bk_score[250]	1.283	28.3%	0.25	0.240	1.038	0.299	

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Pseudo R-squared (McFadden): 0.069

Pseudo R-squared (McFadden adjusted): 0.067

Area under the RO Curve (AUC): 0.728

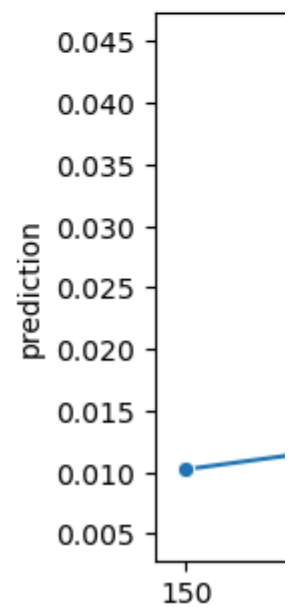
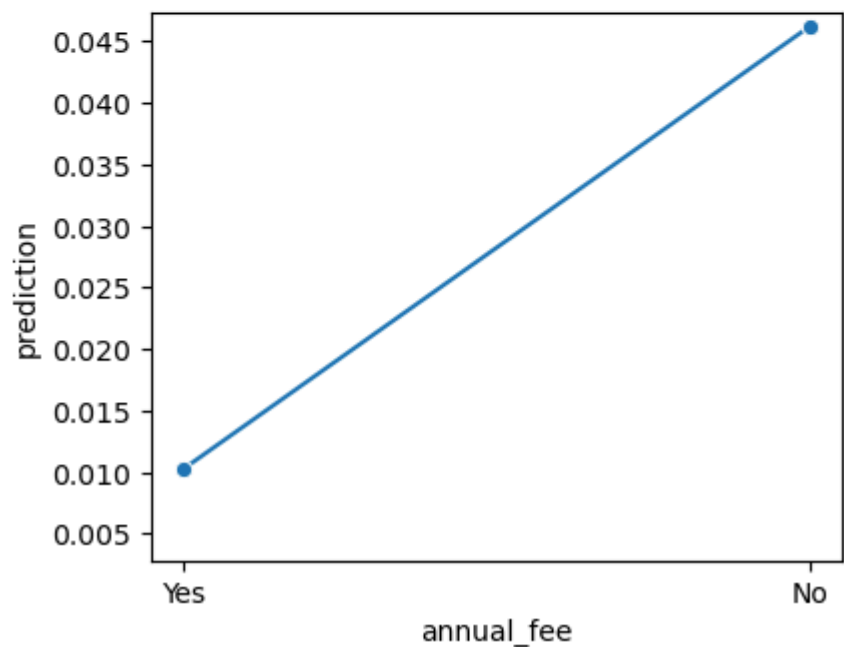
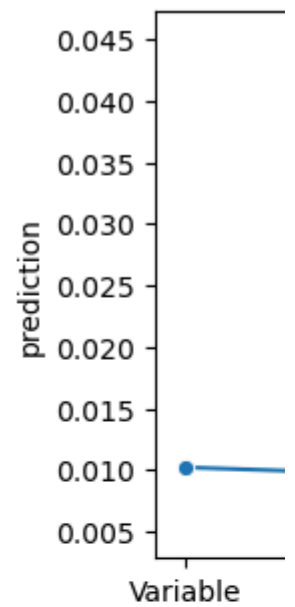
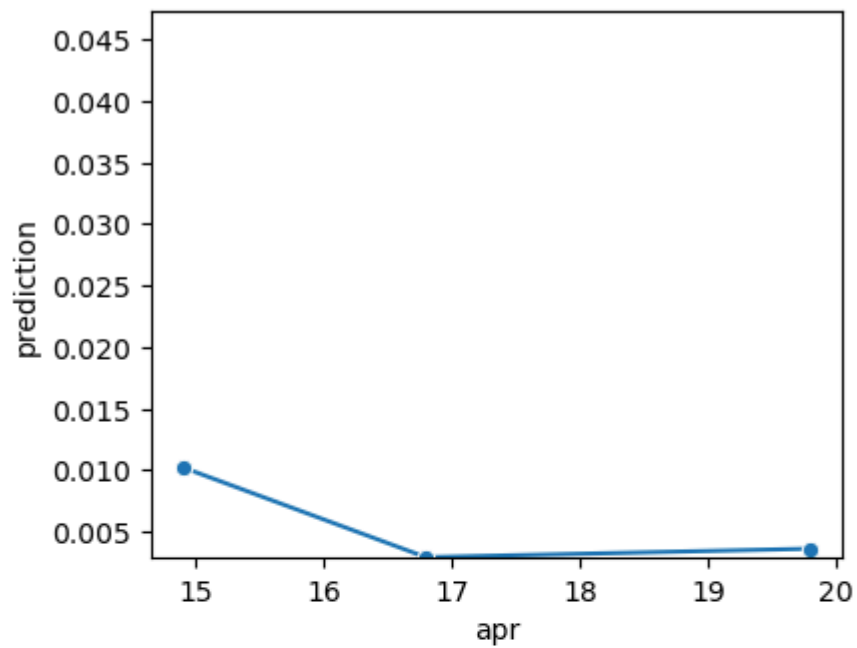
Log-likelihood: -5407.927, AIC: 10845.853, BIC: 10982.385

Chi-squared: 805.832, df(14), p.value < 0.001

Nr obs: 66,312

In [160]:

```
lr_ivar.plot('pred')
```



In [137]:

```
dct = rsm.levels_list(test[['apr', 'fixed_var', 'annual_fee', 'bk_score']])
dct

test_mult_expand = rsm.expand_grid(dct)
test_mult_expand
```

Out [137]:

	apr	fixed_var	annual_fee	bk_score
0	14.9	Variable	Yes	150
1	14.9	Variable	Yes	200
2	14.9	Variable	Yes	250
3	14.9	Variable	No	150
4	14.9	Variable	No	200
5	14.9	Variable	No	250
6	14.9	Fixed	Yes	150
7	14.9	Fixed	Yes	200

8	14.9	Fixed	Yes	250
9	14.9	Fixed	No	150
10	14.9	Fixed	No	200
11	14.9	Fixed	No	250
12	16.8	Variable	Yes	150
13	16.8	Variable	Yes	200
14	16.8	Variable	Yes	250
15	16.8	Variable	No	150
16	16.8	Variable	No	200
17	16.8	Variable	No	250
18	16.8	Fixed	Yes	150
19	16.8	Fixed	Yes	200
20	16.8	Fixed	Yes	250
21	16.8	Fixed	No	150
22	16.8	Fixed	No	200
23	16.8	Fixed	No	250
24	19.8	Variable	Yes	150
25	19.8	Variable	Yes	200
26	19.8	Variable	Yes	250
27	19.8	Variable	No	150
28	19.8	Variable	No	200
29	19.8	Variable	No	250
30	19.8	Fixed	Yes	150
31	19.8	Fixed	Yes	200
32	19.8	Fixed	Yes	250
33	19.8	Fixed	No	150
34	19.8	Fixed	No	200
35	19.8	Fixed	No	250

```
In [138]: test_mult_expand['pred'] = lr.predict(data=test_mult_expand)['prediction']
df = test_mult_expand.copy()
```

Include CLV's value as per the exhibit 2 depending on the product offering

```
In [140]: print(df.dtypes)
```

```
apr      float64
fixed_var  object
annual_fee  object
bk_score   object
pred      float64
dtype: object
```

```
In [141]: df['apr'] = df['apr'].astype('float')
df['bk_score'] = df['bk_score'].astype('int')
```



In [142]:

```
import numpy as np
# Define the conditions and the respective CLV values
conditions = [
    (df['apr'] == 14.9) & (df['fixed_var'] == "Variable") & (df['annual_fee'] == "Yes") &
    (df['bk_score'] == 150),
    (df['apr'] == 14.9) & (df['fixed_var'] == "Variable") & (df['annual_fee'] == "Yes") &
    (df['bk_score'] == 200),
    (df['apr'] == 14.9) & (df['fixed_var'] == "Variable") & (df['annual_fee'] == "Yes") &
    (df['bk_score'] == 250),
    (df['apr'] == 14.9) & (df['fixed_var'] == "Fixed") & (df['annual_fee'] == "No") &
    (df['bk_score'] == 150),
    (df['apr'] == 14.9) & (df['fixed_var'] == "Fixed") & (df['annual_fee'] == "No") &
    (df['bk_score'] == 200),
    (df['apr'] == 14.9) & (df['fixed_var'] == "Fixed") & (df['annual_fee'] == "No") &
    (df['bk_score'] == 250),
    (df['apr'] == 16.8) & (df['fixed_var'] == "Fixed") & (df['annual_fee'] == "Yes") &
    (df['bk_score'] == 150),
    (df['apr'] == 16.8) & (df['fixed_var'] == "Fixed") & (df['annual_fee'] == "Yes") &
    (df['bk_score'] == 200),
    (df['apr'] == 16.8) & (df['fixed_var'] == "Fixed") & (df['annual_fee'] == "Yes") &
    (df['bk_score'] == 250),
    (df['apr'] == 16.8) & (df['fixed_var'] == "Variable") & (df['annual_fee'] == "No") &
    (df['bk_score'] == 150),
    (df['apr'] == 16.8) & (df['fixed_var'] == "Variable") & (df['annual_fee'] == "No") &
    (df['bk_score'] == 200),
    (df['apr'] == 16.8) & (df['fixed_var'] == "Variable") & (df['annual_fee'] == "No") &
    (df['bk_score'] == 250),
    (df['apr'] == 19.8) & (df['fixed_var'] == "Variable") & (df['annual_fee'] == "Yes") &
    (df['bk_score'] == 150),
    (df['apr'] == 19.8) & (df['fixed_var'] == "Variable") & (df['annual_fee'] == "Yes") &
    (df['bk_score'] == 200),
    (df['apr'] == 19.8) & (df['fixed_var'] == "Variable") & (df['annual_fee'] == "Yes") &
    (df['bk_score'] == 250),
    (df['apr'] == 19.8) & (df['fixed_var'] == "Fixed") & (df['annual_fee'] == "No") &
    (df['bk_score'] == 150),
    (df['apr'] == 19.8) & (df['fixed_var'] == "Fixed") & (df['annual_fee'] == "No") &
    (df['bk_score'] == 200),
    (df['apr'] == 19.8) & (df['fixed_var'] == "Fixed") & (df['annual_fee'] == "No") &
    (df['bk_score'] == 250),
]

choices = [93, 73, 43, 52, 32, 2, 103, 83, 53, 82, 62, 32, 141, 121, 91, 100, 80, 50]

# Applying the conditions to assign values to 'CLV'
df['CLV'] = np.select(conditions, choices) # Using np.nan as default to clearly see
unmatched conditions
```

```
In [143]: df['exp_profit'] = df['pred'] * df['CLV']
```

```
In [144]: df
```

```
Out [144]:
```

	apr	fixed_var	annual_fee	bk_score	pred	CLV	exp_profit
0	14.9	Variable	Yes	150	0.010639	93	0.989396
1	14.9	Variable	Yes	200	0.013514	73	0.986538
2	14.9	Variable	Yes	250	0.016195	43	0.696406
3	14.9	Variable	No	150	0.036529	0	0.000000
4	14.9	Variable	No	200	0.046077	0	0.000000
5	14.9	Variable	No	250	0.054859	0	0.000000
6	14.9	Fixed	Yes	150	0.011468	0	0.000000
7	14.9	Fixed	Yes	200	0.014565	0	0.000000
8	14.9	Fixed	Yes	250	0.017451	0	0.000000
9	14.9	Fixed	No	150	0.039298	52	2.043491
10	14.9	Fixed	No	200	0.049532	32	1.585024
11	14.9	Fixed	No	250	0.058932	2	0.117865
12	16.8	Variable	Yes	150	0.004107	0	0.000000
13	16.8	Variable	Yes	200	0.005226	0	0.000000
14	16.8	Variable	Yes	250	0.006273	0	0.000000
15	16.8	Variable	No	150	0.014330	82	1.175090
16	16.8	Variable	No	200	0.018185	62	1.127496
17	16.8	Variable	No	250	0.021773	32	0.696737
18	16.8	Fixed	Yes	150	0.004429	103	0.456195
19	16.8	Fixed	Yes	200	0.005636	83	0.467770
20	16.8	Fixed	Yes	250	0.006765	53	0.358527
21	16.8	Fixed	No	150	0.015444	0	0.000000
22	16.8	Fixed	No	200	0.019592	0	0.000000
23	16.8	Fixed	No	250	0.023451	0	0.000000
24	19.8	Variable	Yes	150	0.002953	141	0.416381
25	19.8	Variable	Yes	200	0.003759	121	0.454855
26	19.8	Variable	Yes	250	0.004514	91	0.410757
27	19.8	Variable	No	150	0.010335	0	0.000000
28	19.8	Variable	No	200	0.013130	0	0.000000
29	19.8	Variable	No	250	0.015736	0	0.000000
30	19.8	Fixed	Yes	150	0.003185	0	0.000000
31	19.8	Fixed	Yes	200	0.004055	0	0.000000
32	19.8	Fixed	Yes	250	0.004868	0	0.000000
33	19.8	Fixed	No	150	0.011141	100	1.114137
34	19.8	Fixed	No	200	0.014151	80	1.132068
35	19.8	Fixed	No	250	0.016956	50	0.847813

```
In [162]: # Filter the DataFrame for bk_score = 200 and find the row with the maximum  
pred value  
filtered_df = df[df['bk_score'] == 200]
```

```
max_pred_row_alternative = filtered_df.loc[filtered_df['exp_profit'].idxmax()]
print(max_pred_row_alternative)
```

```
apr          14.9
fixed_var    Fixed
annual_fee   No
bk_score     200
pred         0.049532
CLV          32
exp_profit   1.585024
Name: 10, dtype: object
```

In [168]:

```
filtered_df = df[df['bk_score'] == 250]
max_pred_row_alternative = filtered_df.loc[filtered_df['exp_profit'].idxmax()]
print(max_pred_row_alternative)
```

```
apr          19.8
fixed_var    Fixed
annual_fee   No
bk_score     250
pred         0.016956
CLV          50
exp_profit   0.847813
Name: 35, dtype: object
```

In [165]:

```
# Filter the DataFrame for bk_score = 200 and find the row with the maximum
pred value
filtered_df = df[df['bk_score'] == 150]
max_pred_row_alternative = filtered_df.loc[filtered_df['exp_profit'].idxmax()]
print(max_pred_row_alternative)
```

```
apr          14.9
fixed_var    Fixed
annual_fee   No
bk_score     150
pred         0.039298
CLV          52
exp_profit   2.043491
Name: 9, dtype: object
```

Our strategy here is to multiply the predictions with the Customer LifeTime Value in order to compute the expected profit per email sent. Once computed, we have to look at the offering that yields the highest expected profit for each customer segment. Also, we made sure that the expected profit is higher than the cost of mailing per customer.

Based on these results, customers with BK scores 150 and 200 should receive the offering with the lowest APR and fixed rate, with no annual fee. The customers with a BK score of 250 should receive the offering with the highest APR, but still a fixed rate and no annual fee.

Please see below the results of the simulation.



## CHATGPT use

Our chat used:

- <https://chat.openai.com/share/f8eb7c1d-a0ec-4b56-bd83-a5f6311ea76a>
- <https://chat.openai.com/share/aef13a4c-ae5a-4435-8522-473e049171da>

In tackling our case study, our team strategically leveraged Generative AI tools, notably ChatGPT, to enhance our research, analysis, and solution formulation processes. Our approach was multifaceted, aiming to capitalize on ChatGPT's capabilities to streamline our workflow, augment our creativity, and bolster our analytical depth.

- Research and Information Gathering:

We initiated our project by using ChatGPT to perform preliminary research. Given ChatGPT's expansive knowledge base, we queried it for background information on customer lifetime value and its relationship with bankruptcy scores in the banking sector. This step provided us with a foundational understanding and pointed us towards relevant financial models and analytical techniques. While ChatGPT offered broad overviews and insights, we noted its limitations in accessing the most current studies or data due to its training cut-off in April 2023. To mitigate this, we complemented AI-generated insights with current research from reputable sources, ensuring our project was informed by the most up-to-date information.

- Strategy Formulation:

Our strategy development greatly benefited from brainstorming sessions with ChatGPT. We discussed various strategic approaches, including predictive modeling and segmentation techniques, to address the case study's objectives. ChatGPT's instant responses to our queries about different strategies allowed us to quickly evaluate the pros and cons of each approach, significantly accelerating our decision-making process. However,

we encountered challenges in assessing the feasibility of certain AI-suggested strategies, requiring us to critically evaluate each suggestion before incorporation into our plan.

- Drafting and Refinement:

For documentation and reporting, ChatGPT was instrumental in drafting sections of our report, generating well-articulated explanations of complex concepts, and suggesting layouts for presenting our findings. It enhanced our productivity by handling routine writing tasks, allowing us to focus on deeper analytical work. We did face challenges in ensuring the accuracy and relevance of AI-generated content, which necessitated thorough reviews and edits to align with our project's specific context.

- Analysis and Simulation:

We explored the potential of using AI for data analysis and simulation, discussing with ChatGPT various statistical techniques and models that could be applied to our data. ChatGPT provided code snippets and explanations for data manipulation and visualization, which we adapted for our analysis. However, the inability to execute code directly or access external databases through ChatGPT limited its utility for hands-on analysis, leading us to use other software tools for actual data processing.

- Maximizing Benefits and Mitigating Limitations:

Our thought process throughout the project was geared towards leveraging ChatGPT's strengths—speed, breadth of knowledge, and versatility—while being mindful of its limitations. We adopted a strategy of using ChatGPT for initial ideation, drafting, and knowledge checks, followed by a rigorous review process where we verified information, refined ideas, and applied professional judgment to ensure the accuracy and appropriateness of our final output.

In conclusion, our experience with using Generative AI tools like ChatGPT in this case study was predominantly positive, significantly enhancing our efficiency and creativity. The key to maximizing benefits from these tools was a balanced approach: leveraging AI for its strengths while critically evaluating its output and supplementing it with detailed research and expert analysis. This approach allowed us to navigate the limitations of AI and produce a comprehensive, informed, and nuanced case study solution.

In []:

```
print("Add code as needed ...")
```

In [1]: `import pandas as pd`

In [2]: `%reload_ext rpy2.ipynthon`

In [3]: 

```
%%R
result <- radiant.design::sample_size_comp(
  type = "proportion",
  p1 = 0.51,
  p2 = 0.52,
  conf_lev = 0.95,
  power = 0.8
)
summary(result)
```

Sample size calculation for comparison of proportions

Sample size 1 : 39,208

Sample size 2 : 39,208

Total sample size: 78,416

Proportion 1 : 0.51

Proportion 2 : 0.52

Effect size : 0.02000934

Confidence level : 0.95

Power : 0.8

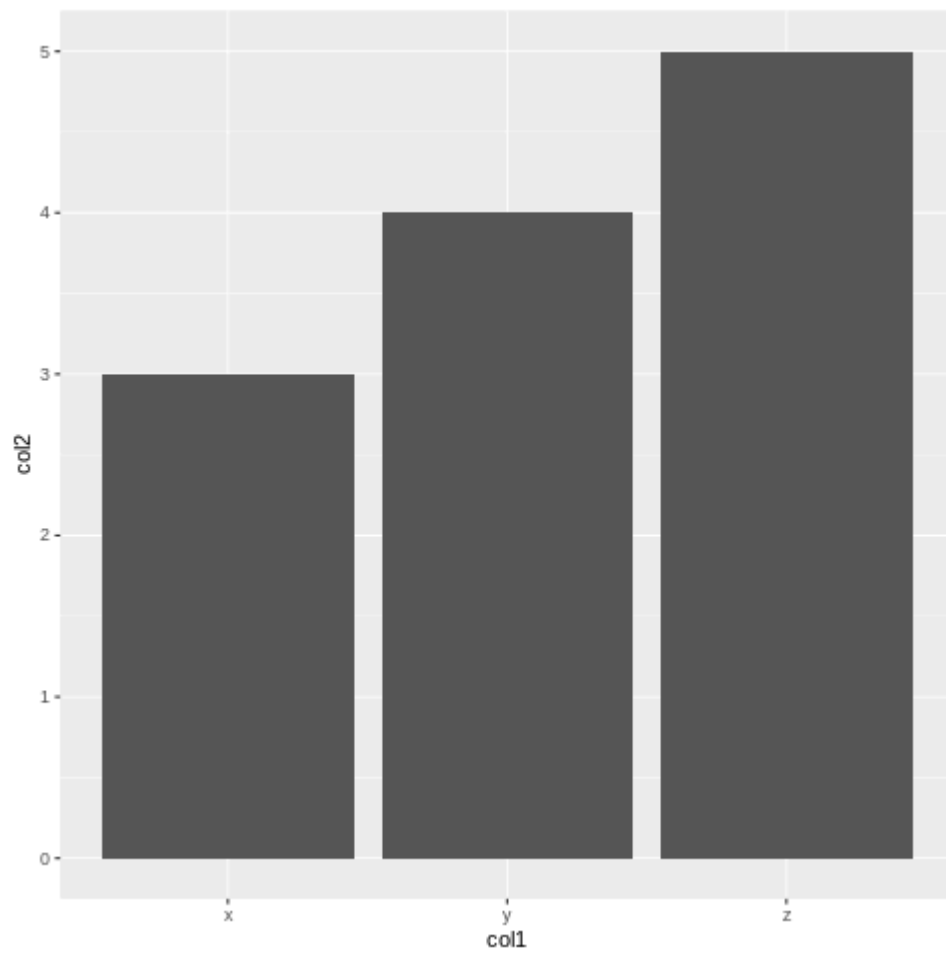
Alternative : two.sided

In [4]: 

```
dframe = pd.DataFrame({
  "col1": ["x", "y", "z"],
  "col2": [3, 4, 5]
})
```

In [5]: 

```
%%R -i dframe
library(ggplot2)
p <- ggplot(dframe, aes(x=col1, y=col2)) + geom_bar(stat="identity")
print(p)
```





```
In [1]: result <- radiant.design::sample_size_comp(  
  type = "proportion",  
  p1 = 0.51,  
  p2 = 0.52,  
  conf_lev = 0.95,  
  power = 0.8  
)  
summary(result)
```

Sample size calculation for comparison of proportions

Sample size 1 : 39,208

Sample size 2 : 39,208

Total sample size: 78,416

Proportion 1 : 0.51

Proportion 2 : 0.52

Effect size : 0.02000934

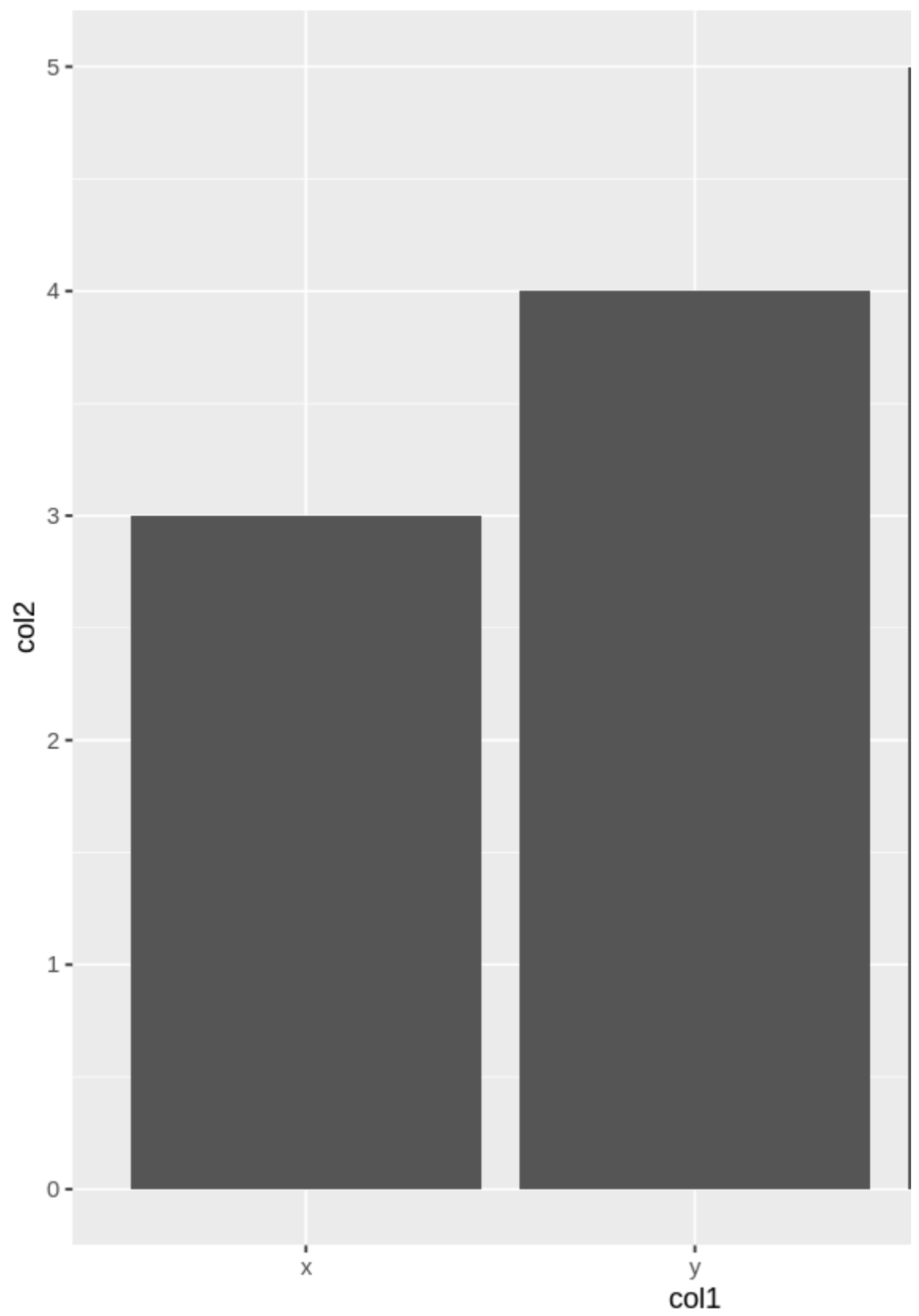
Confidence level : 0.95

Power : 0.8

Alternative : two.sided

```
In [2]: dframe <- data.frame(  
  col1 = c("x", "y", "z"),  
  col2 = c(3, 4, 5)  
)
```

```
In [3]: library(ggplot2)  
p <- ggplot(dframe, aes(x=col1, y=col2)) + geom_bar(stat="identity")  
print(p)
```



```
1 import numpy as np
2 import pyrsm as rsm
3
4
5 def example():
6     text = """
7     You just accessed a function from your first python packages!
8     Change the code in utils/function.py to whatever you need for this assignment
9     Use 'from utils import functions' to get access to your code
10    You can add modules to import from by adding additional .py files to the 'utils' directory
11    Note: If you make changes to the content of this file you will have to restart the notebook kernel to get
12    the updates
13    """
14     print(text)
```