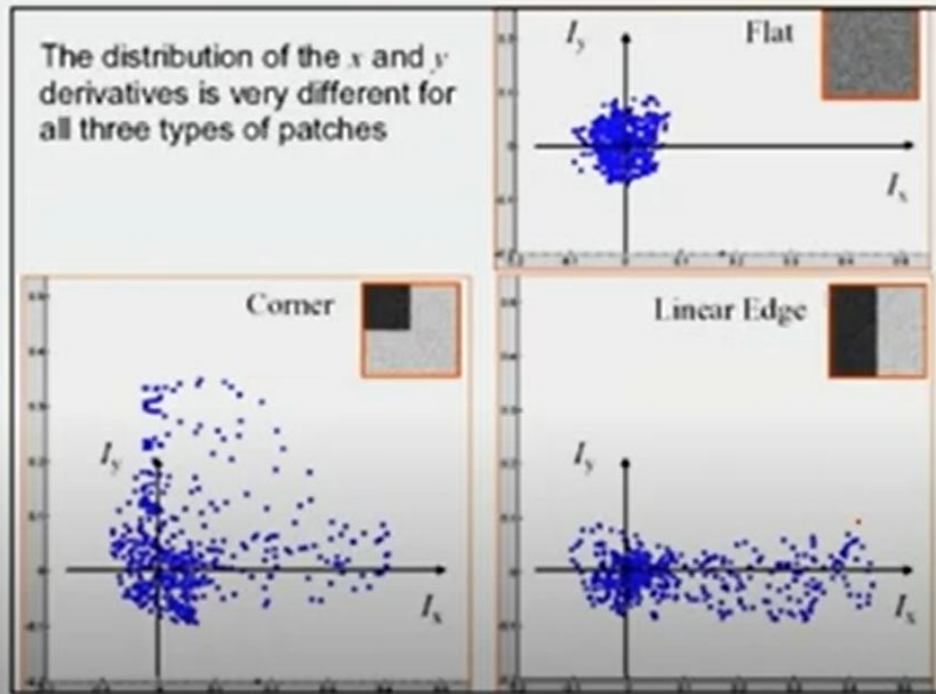


Plotting Derivatives as 2D Points



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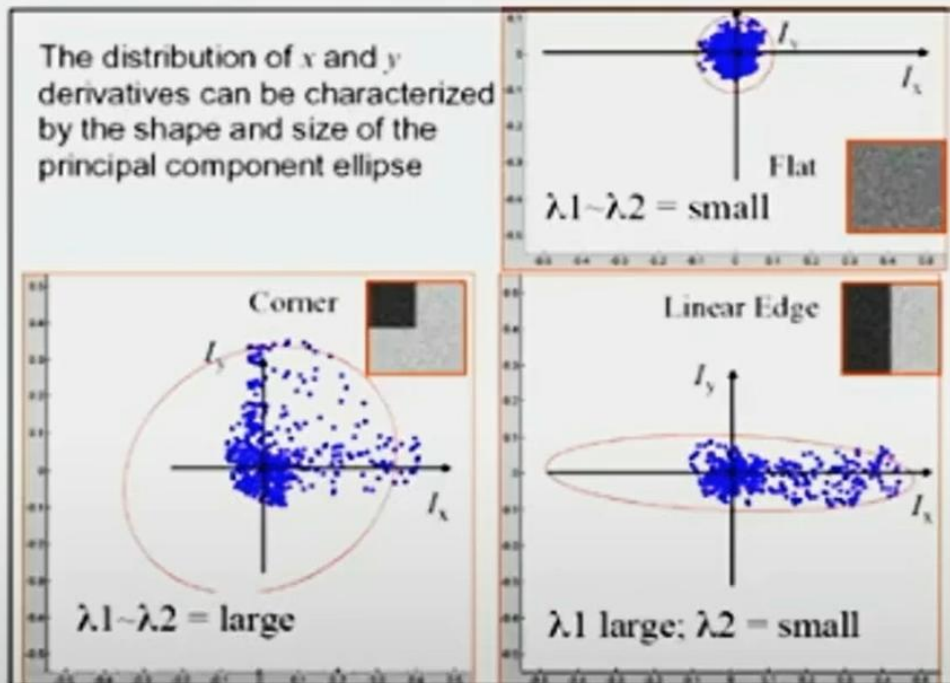


17:00 / 39:58



Fitting Ellipse to each Set of Points

The distribution of x and y derivatives can be characterized by the shape and size of the principal component ellipse

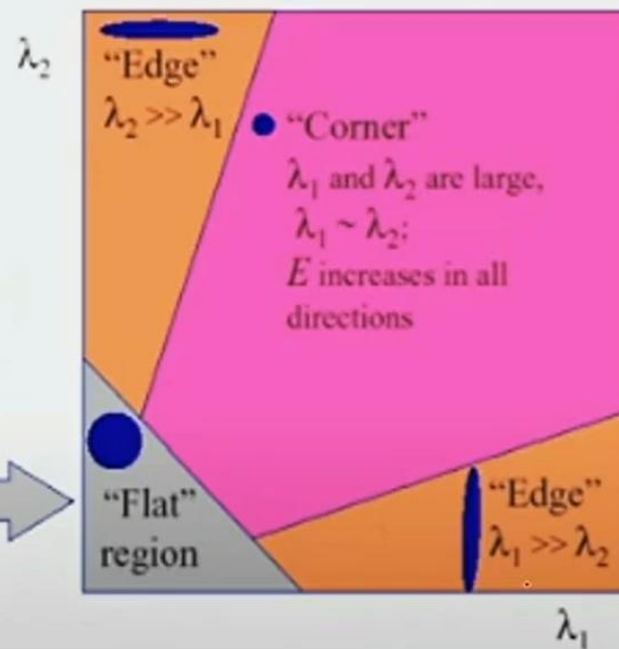


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Classification via Eigenvalues

Classification of
image points using
eigenvalues of M :

λ_1 and λ_2 are small;
 E is almost constant
in all directions



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Corner Response Measure

Measure of corner response:

$$R = \det M - k(\text{trace } M)^2$$

$$\det M = \lambda_1 \lambda_2$$
$$\text{trace } M = \lambda_1 + \lambda_2$$

$$M = \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

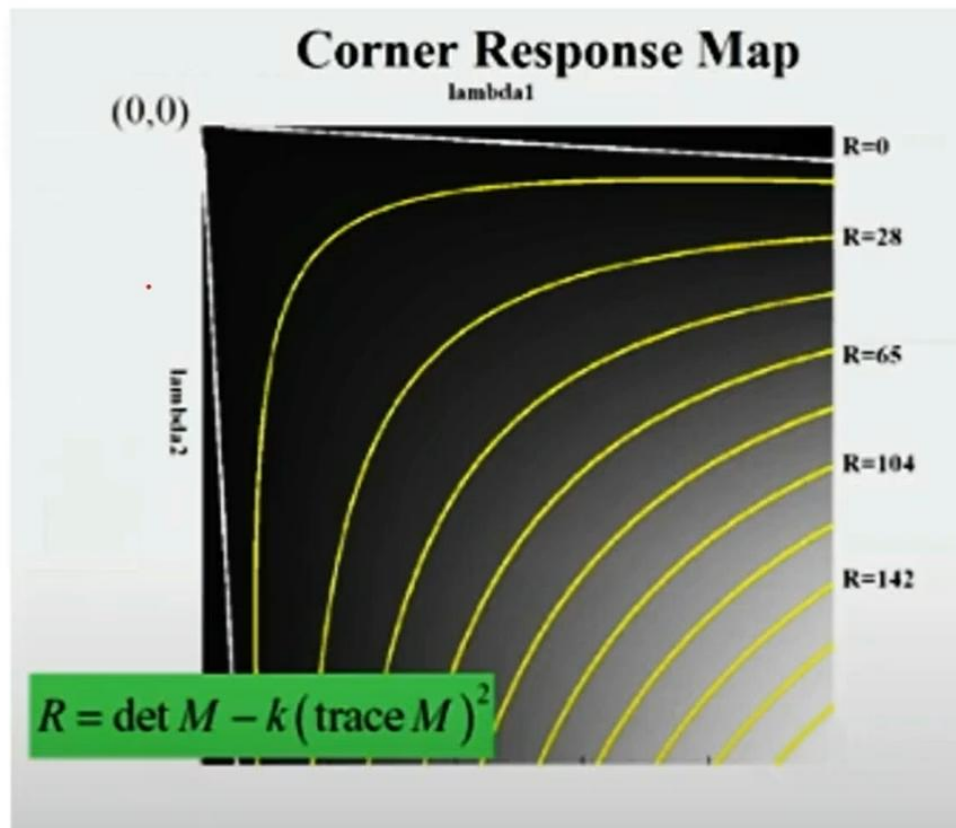
Windowing function - computing a weighted sum (simplest case, $w=1$)

Note: these are just products of components of the gradient, I_x , I_y

(k is an empirically determined constant; $k = 0.04 - 0.06$)



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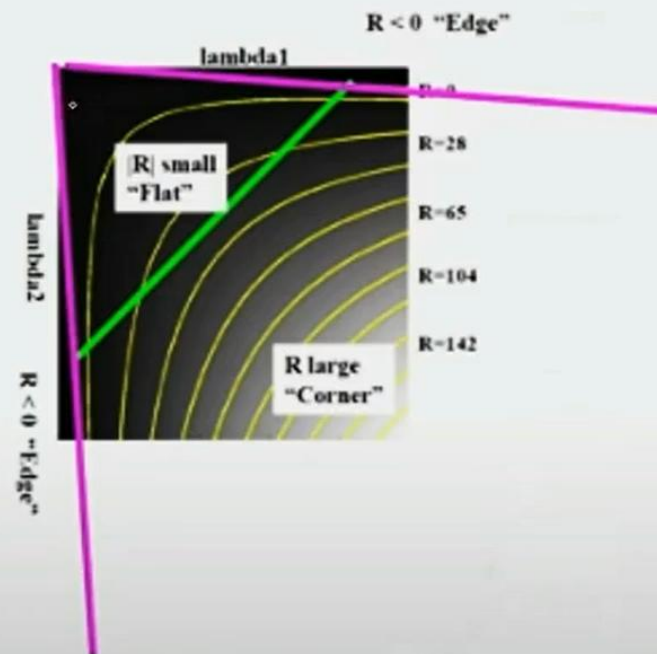
Corner Response Map

- R depends only on eigenvalues of M
- R is large for a corner
- R is negative with large magnitude for an edge
- $|R|$ is small for a flat region

$$R = \det M - k(\text{trace } M)^2$$

$$\det M = \lambda_1 \lambda_2$$

$$\text{trace } M = \lambda_1 + \lambda_2$$



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Corner Response Example

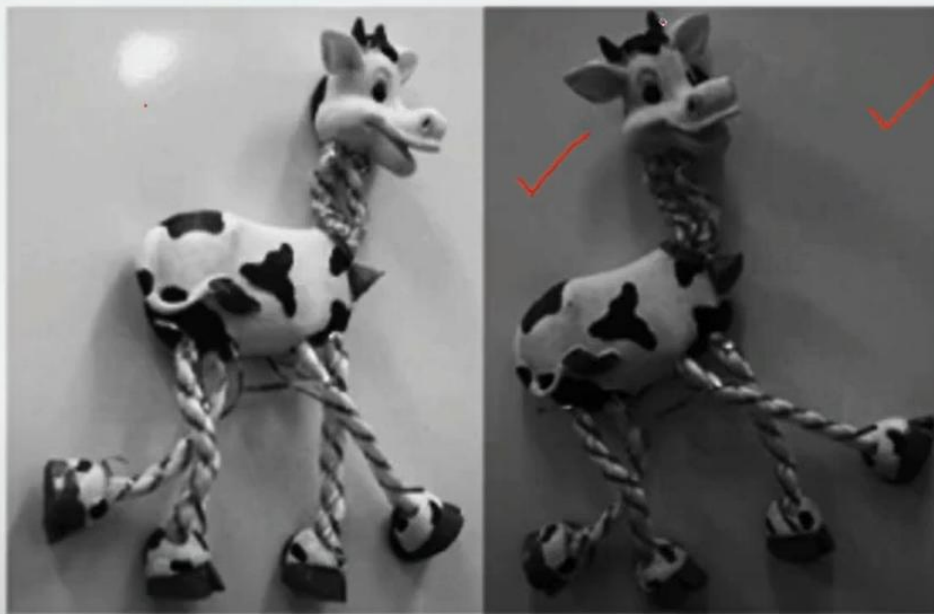


Threshold: > 10000
(corners)



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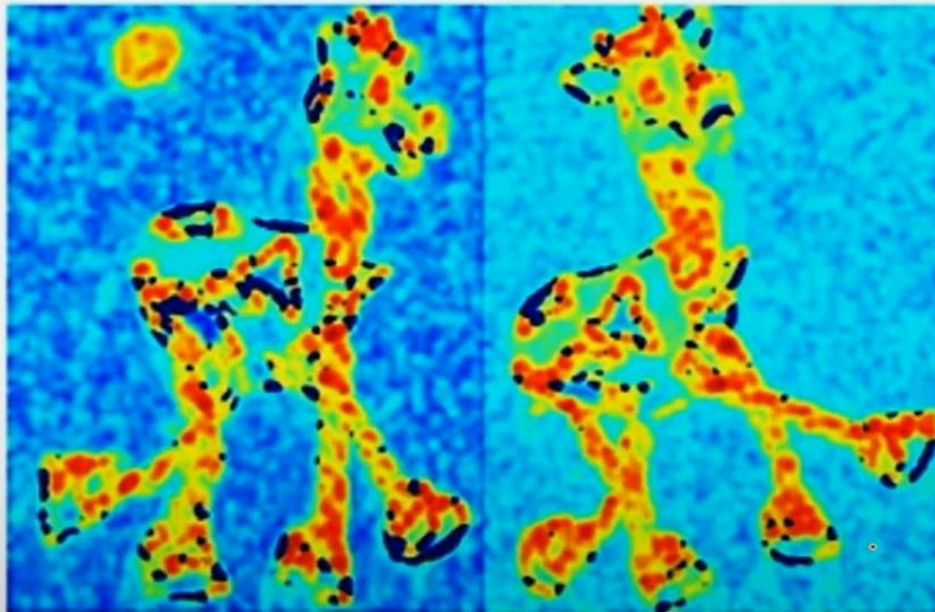
Harris Detector: Workflow



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Harris Detector: Workflow

Compute corner response R



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Harris Detector: Workflow

Find points with large corner response: $R > \text{threshold}$



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Harris Detector: Workflow

Take only the points of local maxima of R



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Harris Detector: Workflow

Find points with large corner response: $R > \text{threshold}$



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Harris Detector: Summary

- Average intensity change in direction $[u, v]$ can be expressed as a bilinear form:

$$E(u, v) \cong [u, v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

- Describe a point in terms of eigenvalues of M :
measure of corner response

$$R = \lambda_1 \lambda_2 - k (\lambda_1 + \lambda_2)^2$$

- A good (corner) point should have a *large intensity change in all directions*, i.e. R should be large positive



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Histograms of Oriented Gradients (HoG)

- **Histogram of Oriented Gradients (HOG)** are feature descriptors used in computer vision and image processing for the purpose of object detection.
- The technique counts occurrences of gradient orientation in localized portions of an image.
- Local object appearance and shape within an image can be described by the distribution of intensity gradients or edge directions



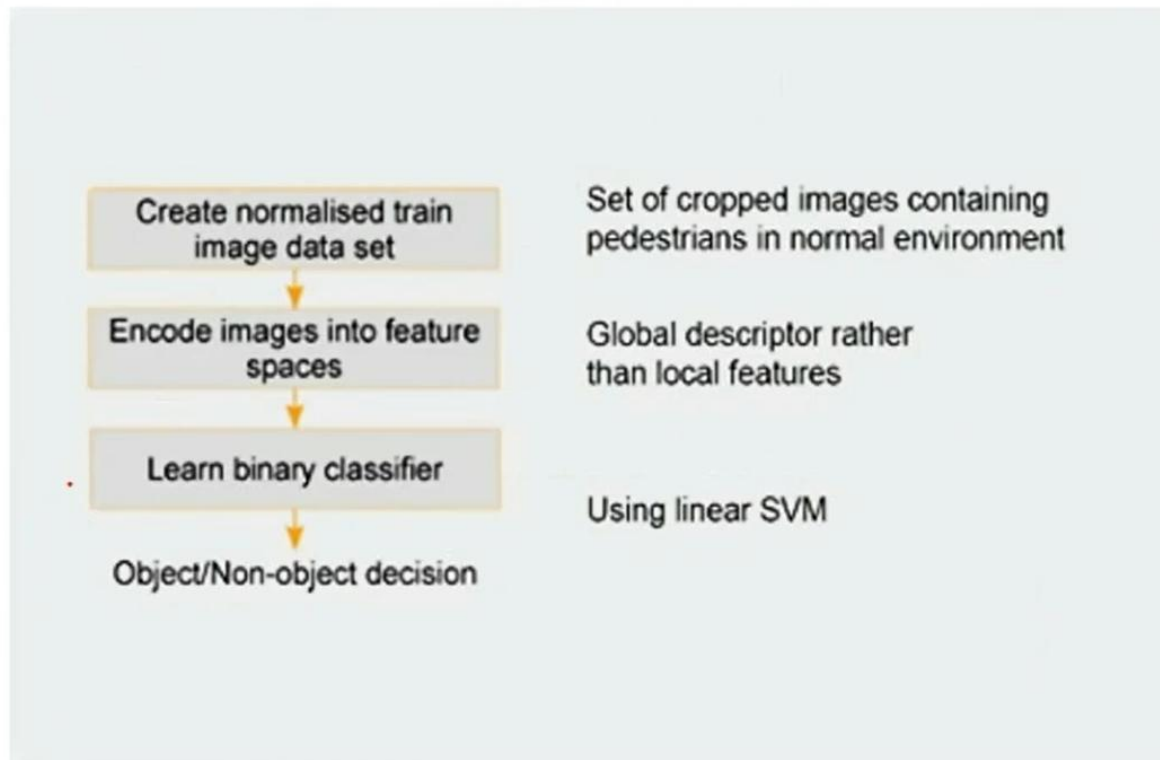
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- Gradient-based feature descriptor developed for people detection
 - Authors: Dalal&Triggs
 - Global descriptor for the complete body
- Very high-dimensional
 - Typically ~4000 dimensions

Very promising results on challenging data sets



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Gradient computation:

- Use Sobel / any other edge detection masks.
- Gradient:

Magnitude : $|\Delta f| = \sqrt{G_x^2 + G_y^2}$

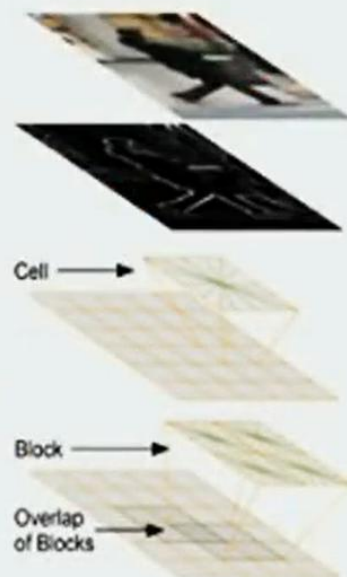
Orientation : $\theta = \arctan\left(\frac{G_y}{G_x}\right)$



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Orientation binning:

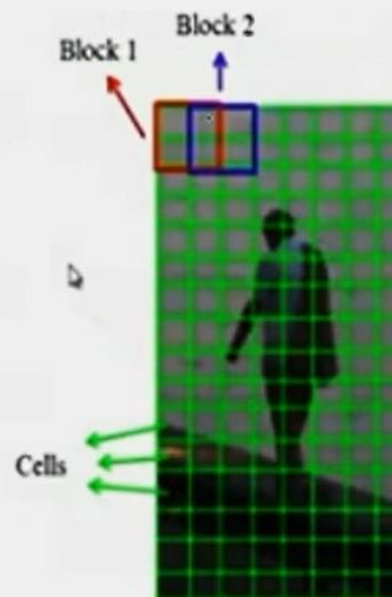
- For a 64x128 image,
- Divide the image into 16x16 blocks of 50% overlap.
- $7 \times 15 = 105$ blocks in total
- Each block should consist of 2x2 cells with size 8x8.
- Quantize the gradient orientation into 9 bins
- The vote is the gradient magnitude
- Interpolate votes bi-linearly between neighboring bin center



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Blocks, Cells

- 16x16 blocks of 50% overlap.
 - $7 \times 15 = 105$ blocks in total
- Each block should consist of 2x2 cells with size 8x8.



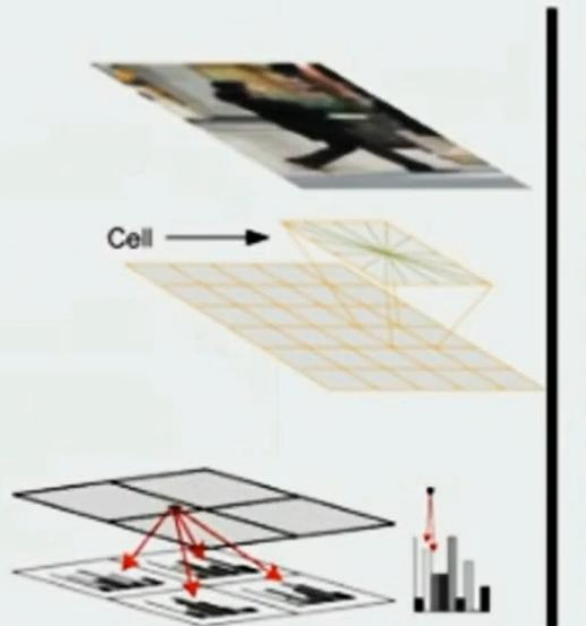
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Cell histograms

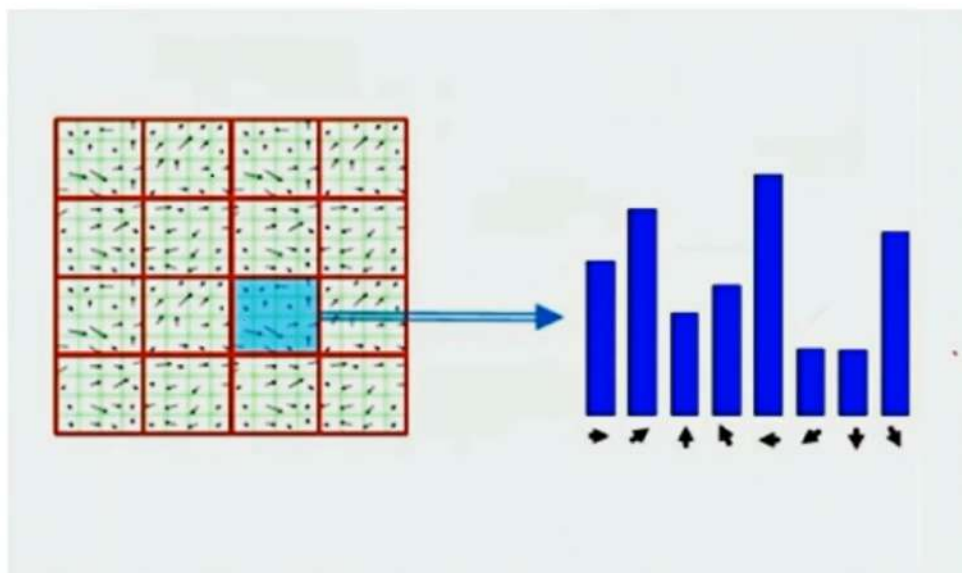
- 9 bins for gradient orientations

0-180 degrees
(Unsigned gradient Orientation)

- Each bin voted with gradient magnitudes



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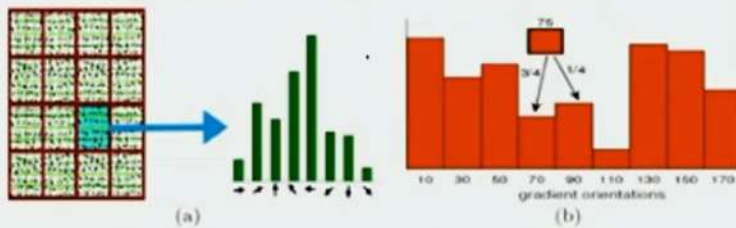
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Histogram interpolation example

$$\theta = 75^\circ$$

- Distance to bin centers
 - Bin 70 \rightarrow 5 degrees
 - Bin 90 \rightarrow 15 degrees

The ratios of belongingness • Ratios: $5/20=1/4$, $15/20=3/4$



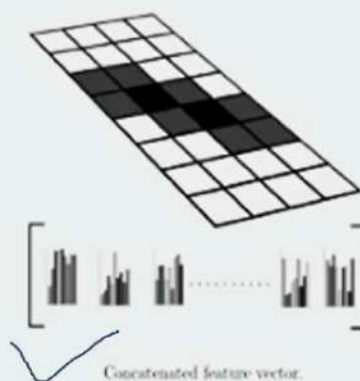
Histogram of oriented gradients: (a) cell histogram and (b) orientation binning.



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Concatenation of descriptor blocks:

- The cell histograms are then concatenated to form a feature vector.
- The histograms obtained from overlapping blocks of 2X2 cells are concatenated into a 1-D feature vector of dimension $105 \times 2 \times 2 \times 9 = 3780$.



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Block normalization:

Let v be the non-normalized vector containing all histograms in a given block

Dalal and Triggs explored different methods for block normalization

L_2 -norm:

$$f = \frac{v}{\|v\|_2}$$

L_1 -norm:

$$f = \frac{v}{\|v\|_1}$$

L_1 -square root

$$f = \sqrt{\frac{v}{\|v\|_1}}$$

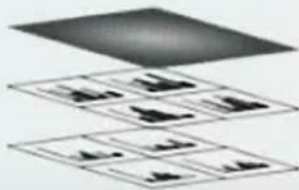
In addition, the scheme L_2 -Hysteresis can be computed by first taking the L_2 -norm, clipping the result, and then renormalizing.



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- Block normalization ensures invariance of descriptor to illumination and photometric variation. Improved performance.

- Gradient magnitudes are weighted according to a Gaussian spatial window



- Distant gradients contribute less to the histogram



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Final descriptor:

- Concatenation of Blocks



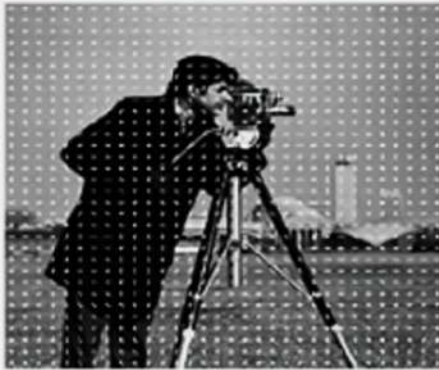
Visualization:



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(a)



(b)

(a) Cameraman image and (b) HOG



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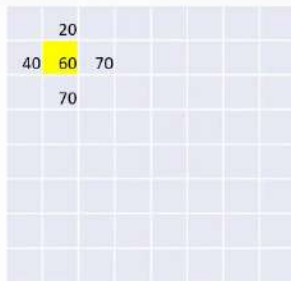
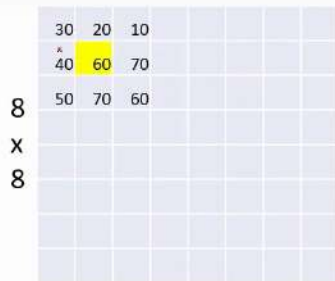
HOG Steps

HOG feature extraction

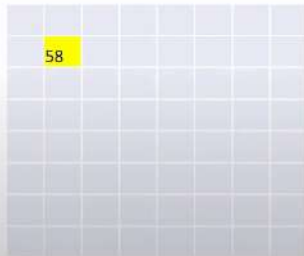
- Compute centered horizontal and vertical gradients with no smoothing
- Compute gradient orientation and magnitudes
 - For color image, pick the color channel with the highest gradient magnitude for each pixel.
- For a 64x128 image,
- Divide the image into 16x16 blocks of 50% overlap.
 - 7x5=105 blocks in total
- Each block should consist of 2x2 cells with size 8x8.
- Quantize the gradient orientation into 9 bins
 - The vote is the gradient magnitude
 - Interpolate votes bi-linearly between neighboring bin center.
 - The vote can also be weighted with Gaussian to downweight the pixels near the edges of the block.
- Concatenate histograms (Feature dimension: $105 \times 4 \times 9 = 3,780$)



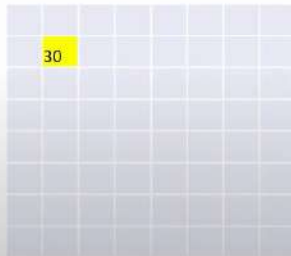
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X direction = $|40 - 70| = 30$
Y direction = $|20 - 70| = 50$



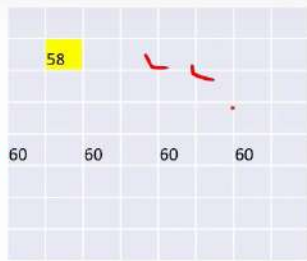
Grad Magnitude



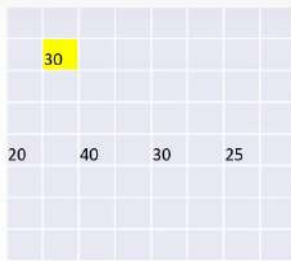
Grad Direction

Grad Mag = $\sqrt{30^2 + 50^2} = \sim 58$
Grad Direction = $\tan^{-1}(30/50) = \sim 30^\circ$

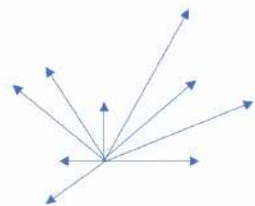
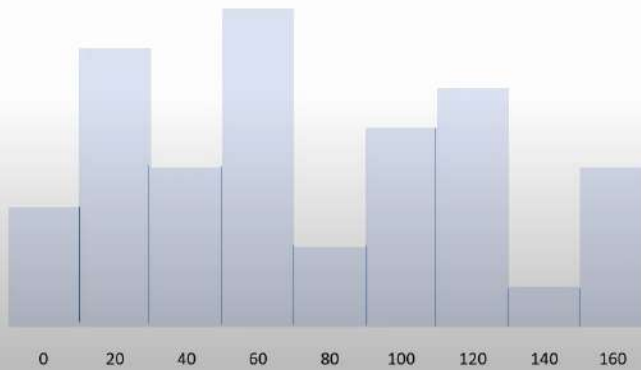
HOG



Grad Magnitude

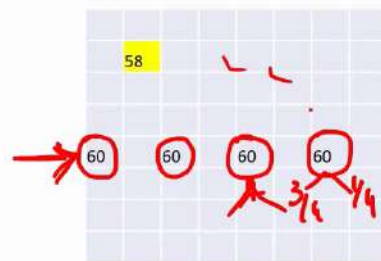


Grad Direction

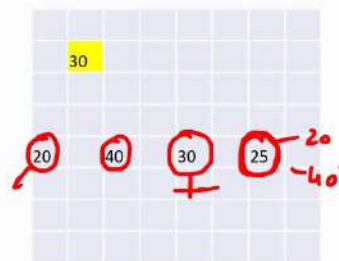


Feature Vector of size 9

HOG

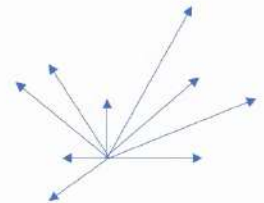


Grad Magnitude ✓

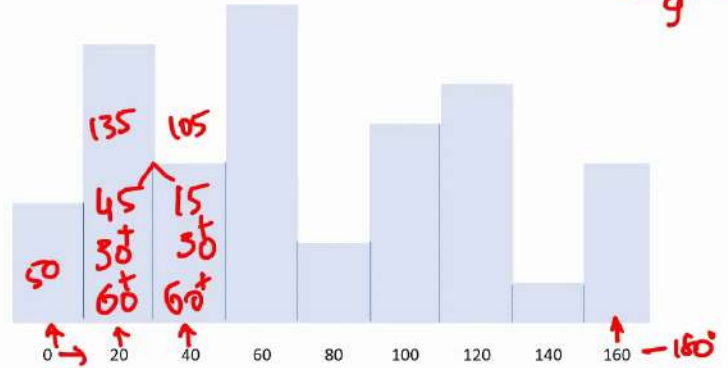


Grad Direction

$$\frac{0-180^\circ}{9}$$



Feature Vector of size 9

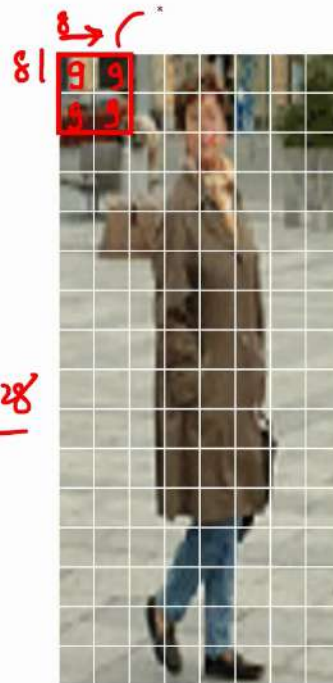


$$fV = [50, 135, 105, \dots] 9$$

HOG Feature Vector



64x128



8x16

$7 \times 15 \times 36 = 3780$

HOG Feature Vector



64x128



$$\begin{bmatrix} 2 \\ 4 \end{bmatrix} \quad \sqrt{2^2 + 4^2} = \underline{4.472}$$

$$\frac{2}{4.472}, \frac{4}{4.472} = \underline{0.4472}, \underline{0.8944}$$

$$\begin{bmatrix} 4 \\ 8 \end{bmatrix} \quad \sqrt{4^2 + 8^2} = 8.944$$

$$\frac{4}{8.944}, \frac{8}{8.944} = 0.4472, 0.8944$$

$$\frac{8 \times 16}{7 \times 15}$$

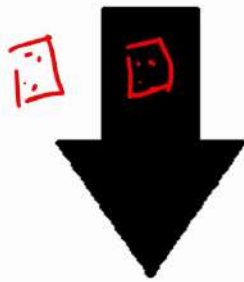
$$7 \times 15 \times 36 = \underline{3780}$$

$$150 \times 300 = \underline{\underline{45,000}}$$

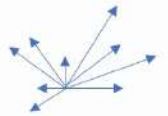
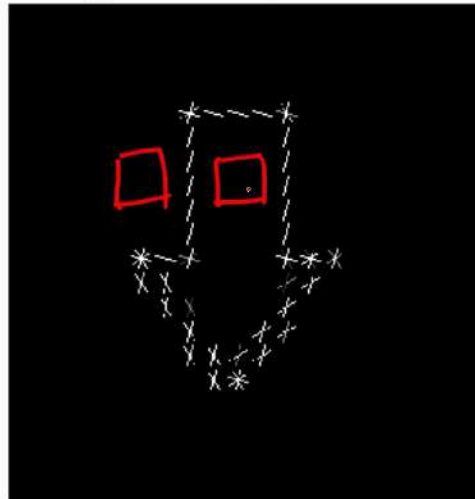
HOG - Example

Ev-00N

Input image



Histogram of Oriented Gradients



HOG generated using skimage: http://scikit-image.org/docs/dev/auto_examples/features_detection/plot_hog.html ✓

nt

HOG - Example

Ev-00N

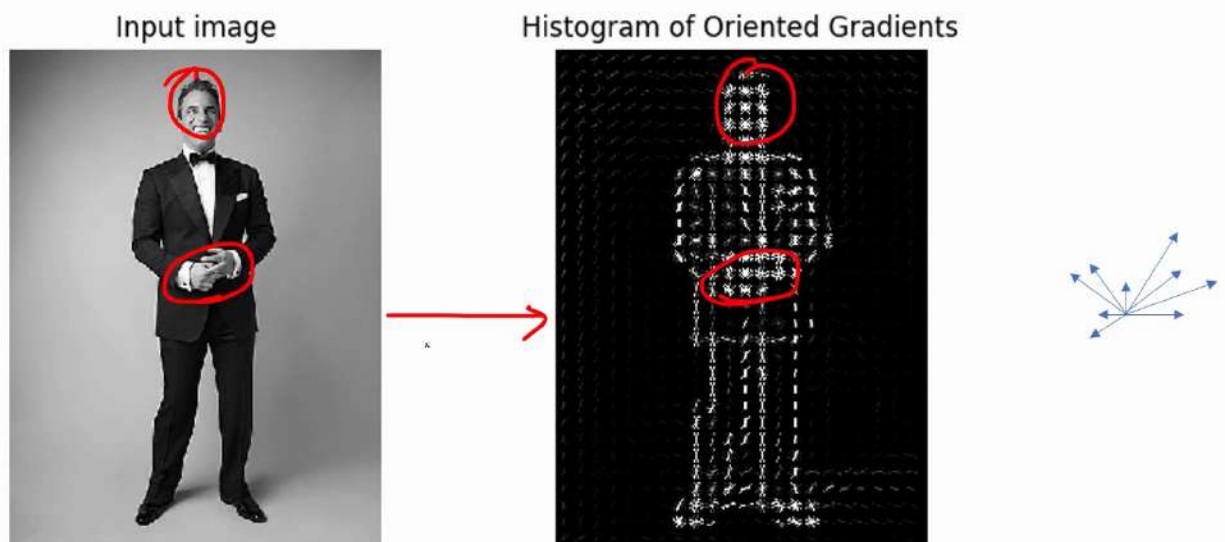
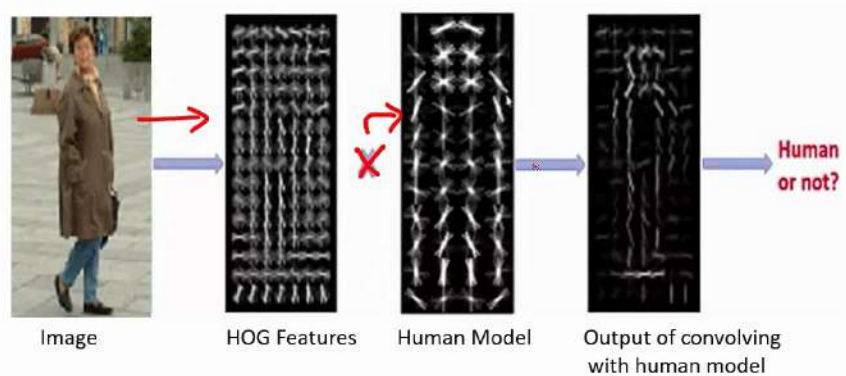


Image Credit - https://en.wikipedia.org/wiki/File:05_Sebastian_Maniscalco_1251f.jpg
HOG generated using skimage: http://scikit-image.org/docs/dev/auto_examples/features_detection/plot_hog.html

nt

Object Detection with HOG+SVM



Histograms of Oriented Gradients for Human Detection:
Navneet Dalal and Bill Triggs

Slide credit: <https://www.youtube.com/watch?v=2DihV1m8y38>

Dalal & Triggs Detector: <https://lear.inrialpes.fr/people/triggs/pubs/Dalal-cvpr05.pdf>