

# LAB 5

## Kruskal's Algorithm:

Kruskal's algorithm is a greedy approach for finding the Minimum Spanning Tree (MST) by selecting edges in ascending order of weight, ensuring no cycles form. It efficiently uses the Disjoint Set (Union-Find) data structure to manage connected components.

```
1. #include <iostream>
2. #include <vector>
3. #include <algorithm>
4.
5. using namespace std;
6.
7. struct Edge {
8.     int start, end, weight;
9. };
10.
11. bool compareEdges(Edge a, Edge b) {
12.     return a.weight < b.weight;
13. }
14.
15. class DisjointSet {
16.     vector<int> parent, rank;
17. public:
18.     DisjointSet(int n) {
19.         parent.resize(n);
20.         rank.resize(n, 0);
21.         for (int i = 0; i < n; i++) parent[i] = i;
22.     }
23.
24.     int findParent(int node) {
25.         if (parent[node] != node)
26.             parent[node] = findParent(parent[node]);
27.         return parent[node];
28.     }
29.
30.     void unionSets(int node1, int node2) {
31.         int root1 = findParent(node1);
32.         int root2 = findParent(node2);
33.         if (root1 != root2) {
34.             if (rank[root1] > rank[root2])
35.                 parent[root2] = root1;
36.             else if (rank[root1] < rank[root2])
37.                 parent[root1] = root2;
38.             else {
39.                 parent[root2] = root1;
40.                 rank[root1]++;
41.             }
42.         }
43.     }
44. };
45.
46. int kruskalAlgorithm(int totalNodes, vector<Edge> &edges) {
47.     sort(edges.begin(), edges.end(), compareEdges);
48.     DisjointSet ds(totalNodes);
49.     int totalWeight = 0, selectedEdges = 0;
50.
51.     for (Edge edge : edges) {
52.         if (ds.findParent(edge.start) != ds.findParent(edge.end)) {
53.             ds.unionSets(edge.start, edge.end);
54.             totalWeight += edge.weight;
55.             selectedEdges++;
56.             if (selectedEdges == totalNodes - 1) break;
57.         }
58.     }
59.     return totalWeight;
60. }
61.
62. int main() {
63.     int totalNodes = 4;
64.     vector<Edge> edges = {
65.         {0, 1, 10}, {0, 2, 6}, {0, 3, 5}, {1, 3, 15}, {2, 3, 4}
66.     };
67. }
```

```

67.
68.     cout << "Minimum Spanning Tree Cost: " << kruskalAlgorithm(totalNodes, edges) << endl;
69.     return 0;

```

## Prim's Algorithm:

Prim's algorithm starts from any node and **grows the MST step by step** by adding the smallest available edge connecting a new vertex. It uses a **priority queue (min-heap)** for efficient edge selection, making it preferable for **dense graphs**.

```

1. #include <iostream>
2. #include <vector>
3.
4. using namespace std;
5.
6. #define V 5
7. #define INF 99999
8.
9. int findMin(vector<int>& key, vector<bool>& visited) {
10.     int min = INF, index = -1;
11.     for (int i = 0; i < V; i++) {
12.         if (!visited[i] && key[i] < min) {
13.             min = key[i];
14.             index = i;
15.         }
16.     }
17.     return index;
18. }
19.
20. void primMST(vector<vector<int>>& graph) {
21.     vector<int> parent(V, -1);
22.     vector<int> key(V, INF);
23.     vector<bool> visited(V, false);
24.
25.     key[0] = 0;
26.
27.     for (int count = 0; count < V - 1; count++) {
28.         int u = findMin(key, visited);
29.         visited[u] = true;
30.
31.         for (int v = 0; v < V; v++) {
32.             if (graph[u][v] && !visited[v] && graph[u][v] < key[v]) {
33.                 parent[v] = u;
34.                 key[v] = graph[u][v];
35.             }
36.         }
37.     }
38.
39.     for (int i = 1; i < V; i++)
40.         cout << parent[i] << " - " << i << " : " << graph[i][parent[i]] << "\n";
41. }
42.
43. int main() {
44.     vector<vector<int>> graph = {
45.         {2, 2, 0, 6, 8},
46.         {2, 5, 3, 8, 5},
47.         {0, 3, 8, 0, 7},
48.         {6, 8, 9, 9, 9},
49.         {0, 5, 7, 9, 0}
50.     };
51.
52.     primMST(graph);
53.
54.     return 0;
55. }
56.
57.
58.

```

```

} ; if ($?) { .\tempCodeRunnerFile }
0 - 1 : 2
1 - 2 : 3
0 - 3 : 6
1 - 4 : 5
PS C:\Users\mohit\Desktop\STUDY\DAA LAB\27>

```

## LEETCODE 1

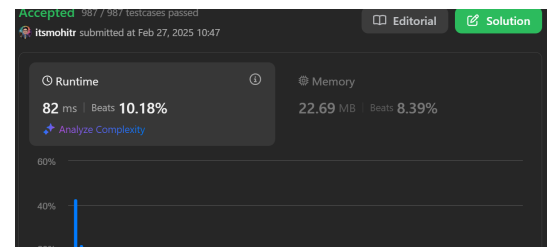
The problem "**Longest Substring Without Repeating Characters**" requires finding the longest contiguous substring in a given string *s* where no character appears more than once.

For example:

- **Input:** "abcabcbb"
- **Output:** 3 (Longest substring: "abc")

A common approach to solve this is using the **Sliding Window** technique with a **HashSet** or **HashMap** to track seen characters efficiently. The optimal solution runs in  **$O(n)$  time complexity**.

```
1. class Solution {
2. public:
3.     int lengthOfLongestSubstring(string s) {
4.         int maxLength = 0;
5.         int n = s.length();
6.
7.         for (int i = 0; i < n; i++) {
8.             string str = "";
9.             for (int j = i; j < n; j++) {
10.                if (str.find(s[j]) != string::npos) {
11.                    break;
12.                }
13.                str += s[j];
14.                maxLength = max(maxLength, (int)str.length());
15.            }
16.        }
17.        return maxLength;
18.    }
19.
20.
21. }
```



## LEETCODE 2

The problem "**Same Tree**" requires checking whether two binary trees *p* and *q* are identical.

Conditions for Two Trees to be the Same:

1. Both trees must have the same structure.
2. Corresponding nodes must have the same values.

```
1. class Solution {
2. public:
3.     bool isSameTree(TreeNode* p, TreeNode* q) {
4.         if (p == q) return true;
5.         if (!p || !q || p->val != q->val) return false;
6.         return isSameTree(p->left, q->left) && isSameTree(p->right, q->right);
7.     }
8. };
9. 
```

