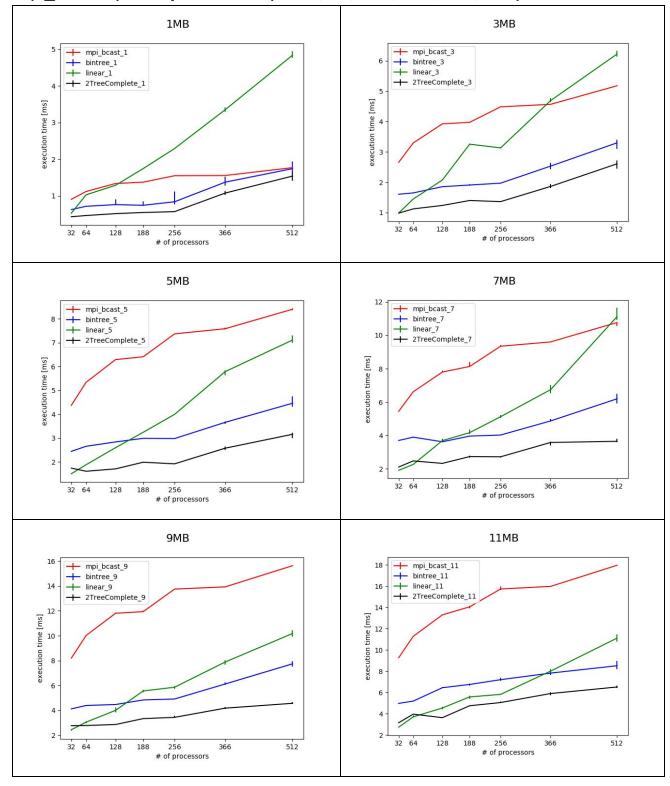
Comparisons on different message sizes(optimal values) (x_values(no of processors) = 32, 64, 128, 188, 256, 512)



Formulas used for calculating chunk values :

1. Linear Pipeline

$$T_{LP} = (L + o + (N \times (o + G \times (s \div N)))) + (L + o + (o + G \times (s \div N))) \times (P - 2)$$

The first part of the equation corresponds to the time taken by root processor to send all chunks. Then the second part is time taken by (P - 2) number of processors excluding the root and the leaf to send the last chunk, since the other chunks has already been sent in parallel and is considered in the first part.

2. Pipeline Binary Tree

$$\mathsf{T}_{\mathsf{PBT} =} \left(\left(L + o + \left(2 \times N \times \left(o + G \times \left(\frac{s}{N} \right) \right) \right) \right) + \left(L + o + 2 \times \left(o + G \times \left(\frac{s}{N} \right) \right) \right) \times \left(\mathsf{floor}(\mathsf{log}_2(\mathsf{P} - 1)) - 1 \right) \right)$$

3. Two Tree Pipeline

$$\mathsf{T}_{\mathsf{BTT}} = (L + 3 \times o + s \times G) + \mathsf{T}_{\mathsf{PBT}}(\frac{s}{2})$$

Parameters Values Used:

L = 1.589921

G = 0.000103

Value of o varies depending upon the value of chunk size.

Chunks Value Calculated Using formula:

(NP /MS/BinaryTree/TwoTree/linearPipeline)

32 1048576 9 15 37

64 1048576 9 17 53

128 1048576 12 17 78

188 1048576 12 21 78

256 1048576 14 21 102

```
366
     1048576
               14
                    23
                        102
512
                    23
                        102
     1048576
               14
32
    3145728
              17
                   29
                       66
    3145728
64
              29
                   29
                       87
128
                    29
     3145728
               29
                        133
188
     3145728
               29
                    29
                        161
256
     3145728
               29
                    29
                        204
366
     3145728
               29
                    39
                        236
               29
512
     3145728
                    39
                        236
32
    5242880
              25
                   37
                       78
    5242880
                   49
                       124
64
              25
     5242880
128
               28
                    49
                        182
188
     5242880
               28
                    49
                        196
256
     5242880
               36
                    49
                        232
366
     5242880
               36
                    49
                        320
512
     5242880
               37
                    49
                        341
32
    7340032
              29
                   41
                       106
                       155
                   51
64
    7340032
              29
128
    7340032
               34
                   69
                        193
                        265
188
     7340032
               34
                    69
256
     7340032
               40
                    69
                        275
366
     7340032
               40
                    69
                        325
512
     7340032
               40
                    69
                        448
32
    9437184
              33
                   45
                       89
    9437184
                       158
64
              37
                   53
128
     9437184
               40
                    65
                        224
188
     9437184
               40
                    65
                        297
256
     9437184
               44
                    65
                        341
                        400
366
     9437184
                    89
               44
512
     9437184
               44
                    89
                        418
32
      11534336
                 34
                     47
                          109
64
      11534336
                 38
                     55
                          178
128
      11534336
                 45
                     65
                          244
188
      11534336
                          312
                 45
                     79
256
      11534336
                 45
                     79
                          363
366
      11534336
                 45
                     79
                          433
512
      11534336
                 54
                     79
                          489
```

Note:

The chunk values calculated using the formulas are an approximation. Hence, during our experiment we used for different values of chunks.

- 1. Calculated Value.
- 2. Calculated minus 10%.
- 3. Calculated minus 20%.
- 4. Calculated minus 30%.

The final graphs are drawn using the minimum chunks value out of these for each and every value of processors and message size for each algorithm.

Chunks Used for different values:

1. 2TreeComplete

_	Message Sizes								
Process ors	1MB	3МВ	5MB	7MB	9МВ	11MB			
32	10%	0%	0%	20%	30%	0%			
64	0%	0%	0%	0%	0%	10%			
128	10%	0%	0%	0%	0%	10%			
188	20%	10%	0%	0%	0%	0%			
256	20%	0%	0%	10%	0%	10%			
366	20%	0%	0%	0%	0%	0%			
512	10%	30%	0%	0%	0%	0%			

2. Linear Pipeline

	Message Sizes								
Process ors	1MB	3МВ	5MB	7MB	9MB	11MB			
32	0%	0%	10%	0%	0%	20%			
64	20%	20%	10%	0%	10%	30%			
128	10%	30%	0%	0%	10%	0%			
188	10%	30%	0%	10%	20%	20%			
256	30%	30%	20%	0%	0%	10%			
366	30%	10%	10%	20%	20%	10%			
512	30%	20%	20%	10%	0%	20%			

3. BinTree

_	Message Sizes								
Process ors	1MB	3МВ	5MB	7MB	9MB	11MB			
32	30%	0%	10%	0%	0%	10%			
64	0%	0%	10%	0%	0%	0%			
128	0%	0%	30%	10%	10%	0%			
188	0%	20%	20%	10%	0%	20%			
256	0%	10%	20%	10%	10%	0%			
366	30%	30%	20%	20%	20%	20%			
512	0%	10%	0%	0%	0%	0%			

Gain using optimal value over calculated value.(in %)

1. 2TreeComplete

695	32mb	64mb	128mb	188mb	256mb	366mb	512mb
1	0.889454	0.00000	6.716189	10.118819	3.919596	11.803925	0.007777
3	0.000000	0.00000	0.000000	1.625021	0.000000	0.000000	6.734288
5	0.000000	0.00000	0.000000	0.000000	0.000000	0.000000	0.000000
7	10.761468	0.00000	0.322523	0.000000	3.061445	0.000000	0.000000
9	8.122992	0.00000	0.000000	0.000000	0.000000	0.228332	0.000000
11	0.000000	7.33981	19.308749	0.000000	0.832203	0.000000	0.000000

2. LinearPipeline

	32mb	64mb	128mb	188mb	256mb	366mb	512mb
1	0.000000	6.151524	0.874254	0.143586	37.298763	32.870761	33.241264
3	0.000000	4.674128	21.666643	17.159337	7.320765	5.746045	24.114116
5	0.457618	7.342395	0.000000	0.000000	35.113571	10.072209	49.680757
7	0.000000	0.000000	0.000000	26.029365	0.000000	34.761706	9.043133
9	0.000000	3.940497	11.024169	10.642547	0.000000	37.743306	0.000000
11	0.000000	0.765373	0.000000	16.977416	31.004490	39.065871	43.773709

3. Bintree

	32mb	64mb	128mb	188mb	256mb	366mb	512mb
1	1.644890	1.056312	0.331140	0.000000	0.000000	5.687317	0.000000
3	0.000000	0.000000	0.000000	0.595725	1.600985	4.167629	1.083074
5	8.595395	6.181565	5.410343	2.480945	3.969101	9.693637	0.000000
7	0.000000	0.000000	11.532071	11.520448	14.800718	6.971294	0.000000
9	0.000000	0.000000	2.730418	0.000000	19.723635	19.069917	0.023100
11	13.290014	0.000000	0.000000	1.249070	0.000000	0.984796	0.000000