

1463. Cherry Pickup II

→ Fixed starting point.

2	3	1	2
8	4	2	2
5	8	3	5

$$12 + 9 = 21$$

→ Will Greedy work:-

Greedy will not work here bcz of uniformity nature bcz in the grid cherries are not uniformly distributed & greedy works on uniform distribution.

→ Recursion:-

(All path by robot 1 + All path by robot 2) & take maximum of them.

Imp:- In order to write recurrence we have to make sure that robot 1 &

robot 2 move together bcz it might happen

there is common cell in robot 1's path & robot 2's path & that consider only once.

You don't be like that let's do for 'robot1' first & get the maximum sum & then for 'robot2' in that case you have to traverse all the path for both & if there are something common then you have to subtract that cell from actual answer & this will be much longer.

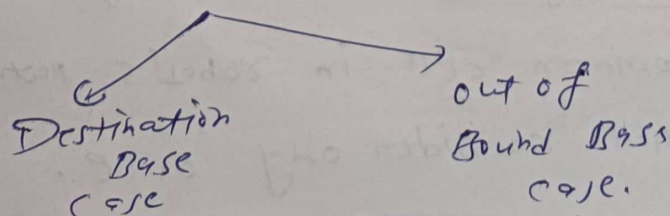
Rules for Recursion

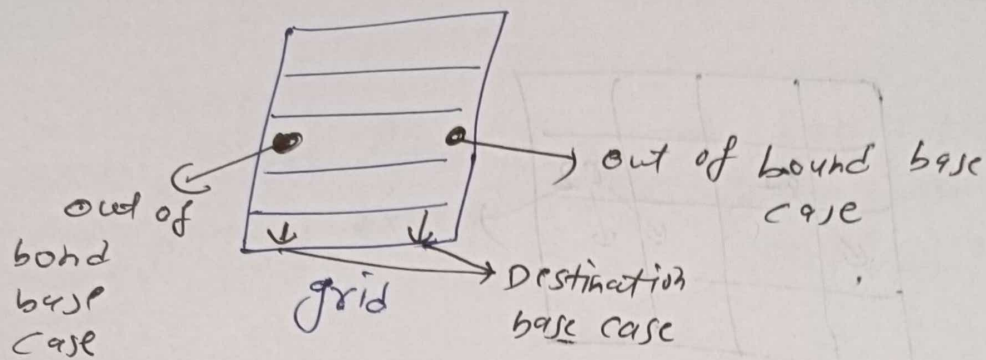
- ① express every thing in terms of $(i1, j1)$ & $(i2, j2)$ and write down all the base cases
- ② explore all the paths
- ③ return the maximum sum

Whenever you have fixed starting points & variable ending points then start recursion from fixed starting point.

Rule-1 write down the Base cases

There are two types of Base case





If any robo go out of bound then that path should not be considered.

$f(i, j_1, j_2)$ Here we are only taking i not j_1 & j_2 bec for both robo j_1 & j_2 will be same.

```

{
    // out of Bound Base case
    if ( $j_1 < 0$  ||  $j_1 > m$  ||  $j_2 < 0$  ||  $j_2 > m$ )
        return -1e8;
    // Destination Base case.
    if ( $i == n-1$ )
    {
        if ( $j_1 == j_2$ ) return  $a[i][j_1]$ ;
        return  $a[i][j_1] + a[i][j_2]$ ;
    }
}

```

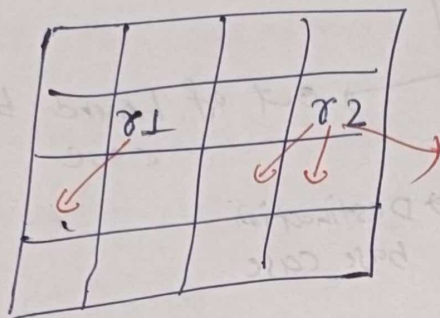
// Explore all possibilities.

```

for (maxi = 0;
    for ( $dj_1 \rightarrow -1$  to  $+1$ )
    {
        for ( $dj_2 \rightarrow -1$  to  $+1$ )
        {
            if ( $j_1 == j_2$ )
            {
                maxi = max(maxi,  $f(i+1, j_1+dj_1, j_2+dj_2)$ 
                    +  $a[i][j_1]$ );
            }
            else
            {
                maxi = max(maxi,  $a[i][j_1] + a[i][j_2] +$ 
                     $f(i+1, j_1+dj_1, j_2+dj_2)$ );
            }
        }
    }
    return maxi;
}

```


② explore all possibilities:



i.e. if robot 1 \rightarrow r1 move left then robot 2 \rightarrow r2
can move in three different cell

so total movements are = 9

so there are 9 possibilities of path.

$$T.C. = O(3^n * 3^n)$$

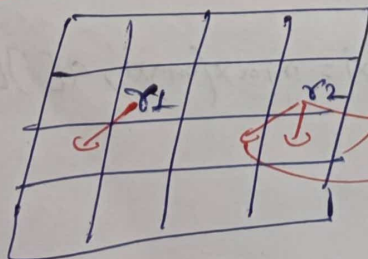
$$S.C. = O(n) \leftarrow \text{stack space}$$

\rightarrow DP Memoization

$$T.C. = O(N * M * M) * 9$$

$$S.C. = O(N * M * M) + O(N)$$

why DP



here r2 is already
explored this &
might possible r1
(come here)

Tabulation

↓
Rules

- (i) first write the base cases.
- (ii) express every state in for loop
↳ states $\rightarrow i, j_1, j_2$.

(i) Base case

$dp[n][m][m]$

// first Base case \rightarrow Destination Base case.

if ($i == n-1$) \rightarrow for $i = n-1$ the $j_1 \rightarrow 0$ to $m-1$
 $j_2 \rightarrow 0$ to $m-1$

for ($j_1 \rightarrow 0$ to $m-1$)

 for ($j_2 \rightarrow 0$ to $m-1$)

 if ($j_1 == j_2$) $dp[n-1][j_1][j_2] = grid[n-1][j_1]$

 else $dp[n-1][j_1][j_2] = grid[n-1][j_1] + grid[n-1][j_2]$

// for loop

for ($i = n-2$ to 0)

 for ($j_1 = 0$ to $m-1$)

 for ($j_2 = 0$ to $m-1$)

\leftarrow copy the recurrence