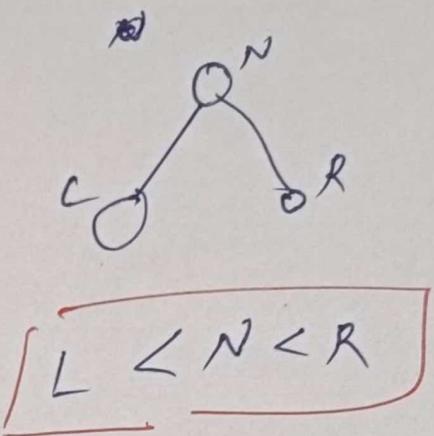
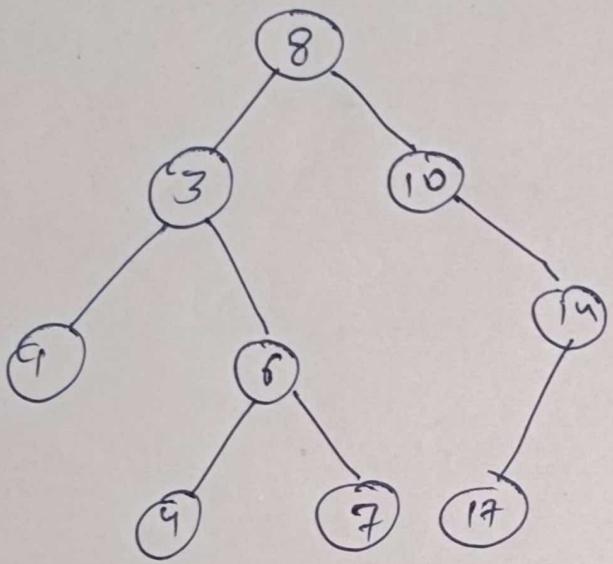


# Binary Search Tree



Ideally duplicates are not allowed in BST

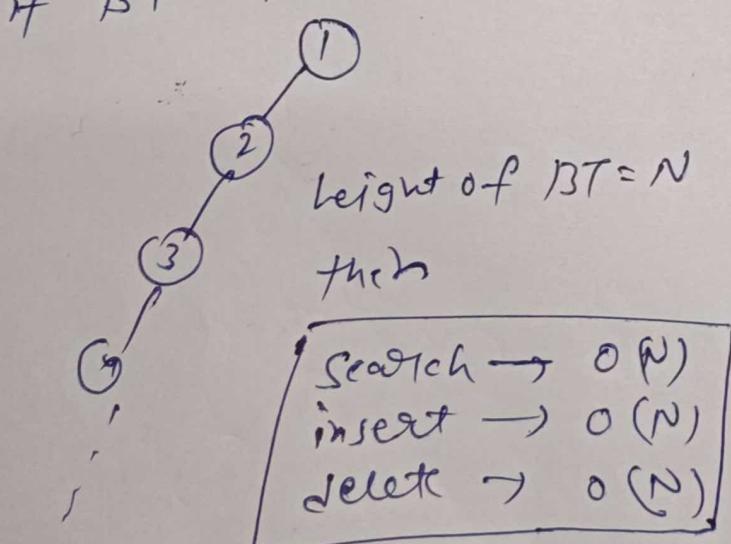
if it presents then

$L \leq N \leq R$  or  $L < N \leq R$

choose any one

## Why BST over The BT

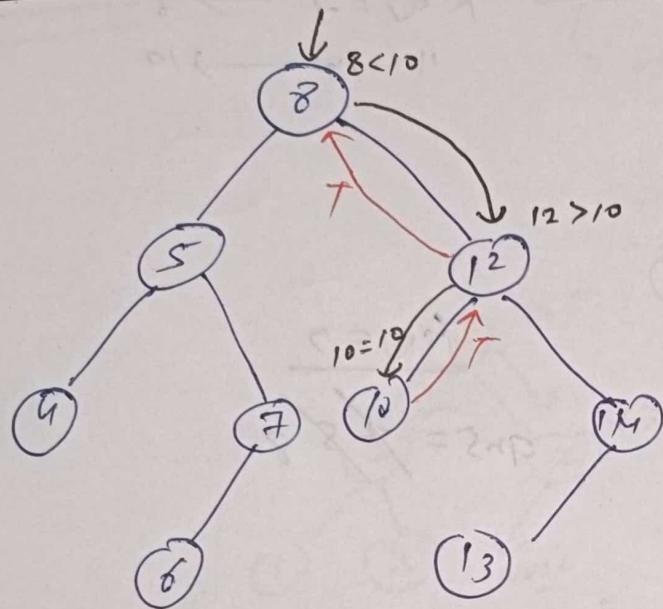
if BT like



But in BST generally  
not always the  
height is  $\log(n)$   
thus

$\boxed{\begin{array}{l} \text{Search} \rightarrow O(\log n) \\ \text{insert} \rightarrow " \\ \text{delete} \rightarrow " \end{array}}$

## Search in BST

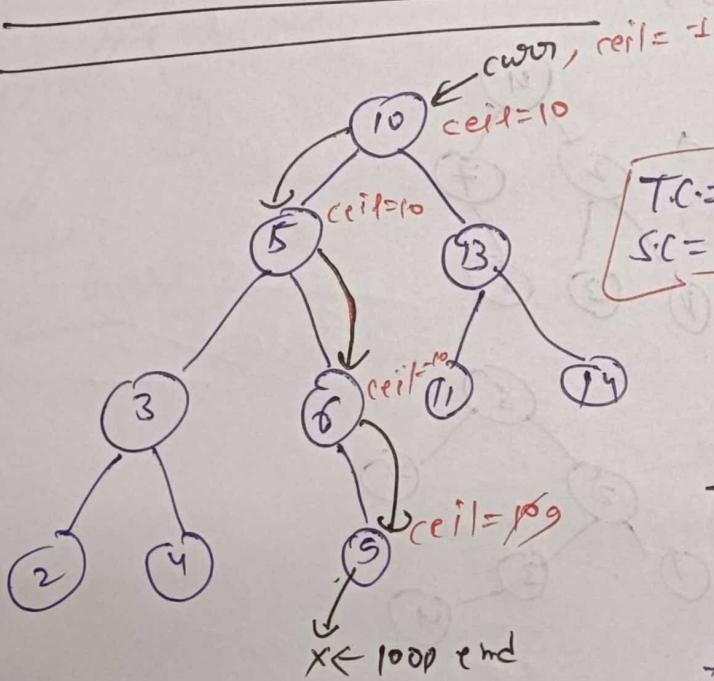


Search = 10

$$\boxed{T.C. = O(\log N)}$$

$$S.C. = O(\log N)$$

## Ceil in BST



$$\begin{aligned} \text{key} &= 8, \text{ans} = 9 \\ \text{key} &= 11, \text{ans} = 11 \\ \text{key} &= 12, \text{ans} = 12 \end{aligned}$$

## Approach

$$\text{key} = 8 \quad \text{ceil} = -1$$

$$\text{1st iteration} \quad \text{curr} = 10 \quad 10 > 8$$

$$\text{ceil} = 10$$

$$\& \quad \text{curr} = 5 \quad (\text{curr} \rightarrow \text{left})$$

$$\text{curr} = 5 \quad 8 > 5 \quad \text{no change in ceil.}$$

$$\text{curr} = 6 \quad (\text{curr} \rightarrow \text{right})$$

$$6 < 8 \quad \text{no change in ceil.}$$

$$\text{curr} = \text{curr} + \text{right} = 9$$

1<sup>st</sup> iteration

$$\text{curr} = 9 \quad 9 > 8$$

$$\text{ceil} = 9$$

$$\text{curr} = \text{curr} \rightarrow \text{left} = \text{NULL}$$

end 1000

2<sup>nd</sup> iteration

$$\text{curr} = 6$$

$$6 < 8 \quad \text{no change in ceil.}$$

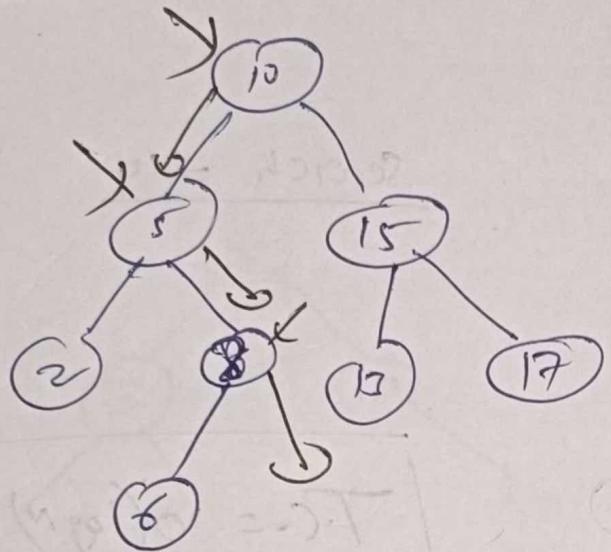
3<sup>rd</sup> iteration

$$\text{curr} = 6$$

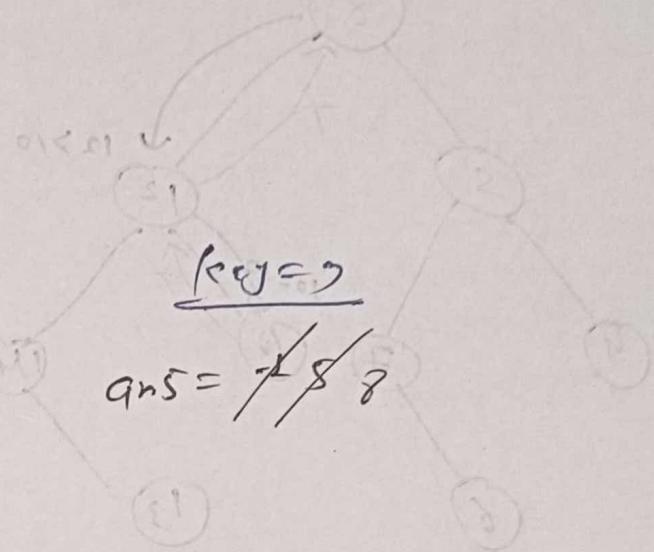
$$6 < 8 \quad \text{no change in ceil.}$$

$$\text{curr} = \text{curr} + \text{right} = 9$$

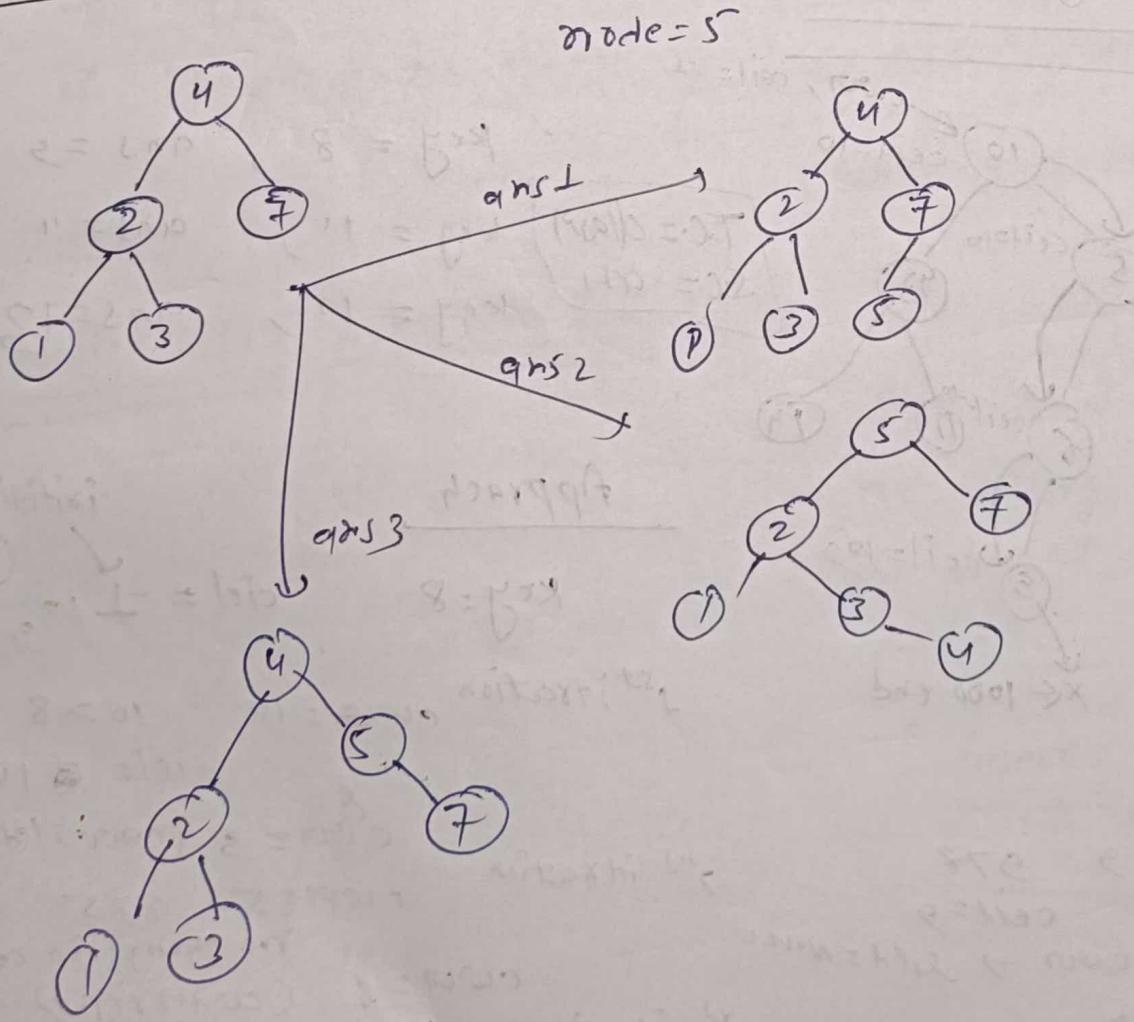
## Floor in BST



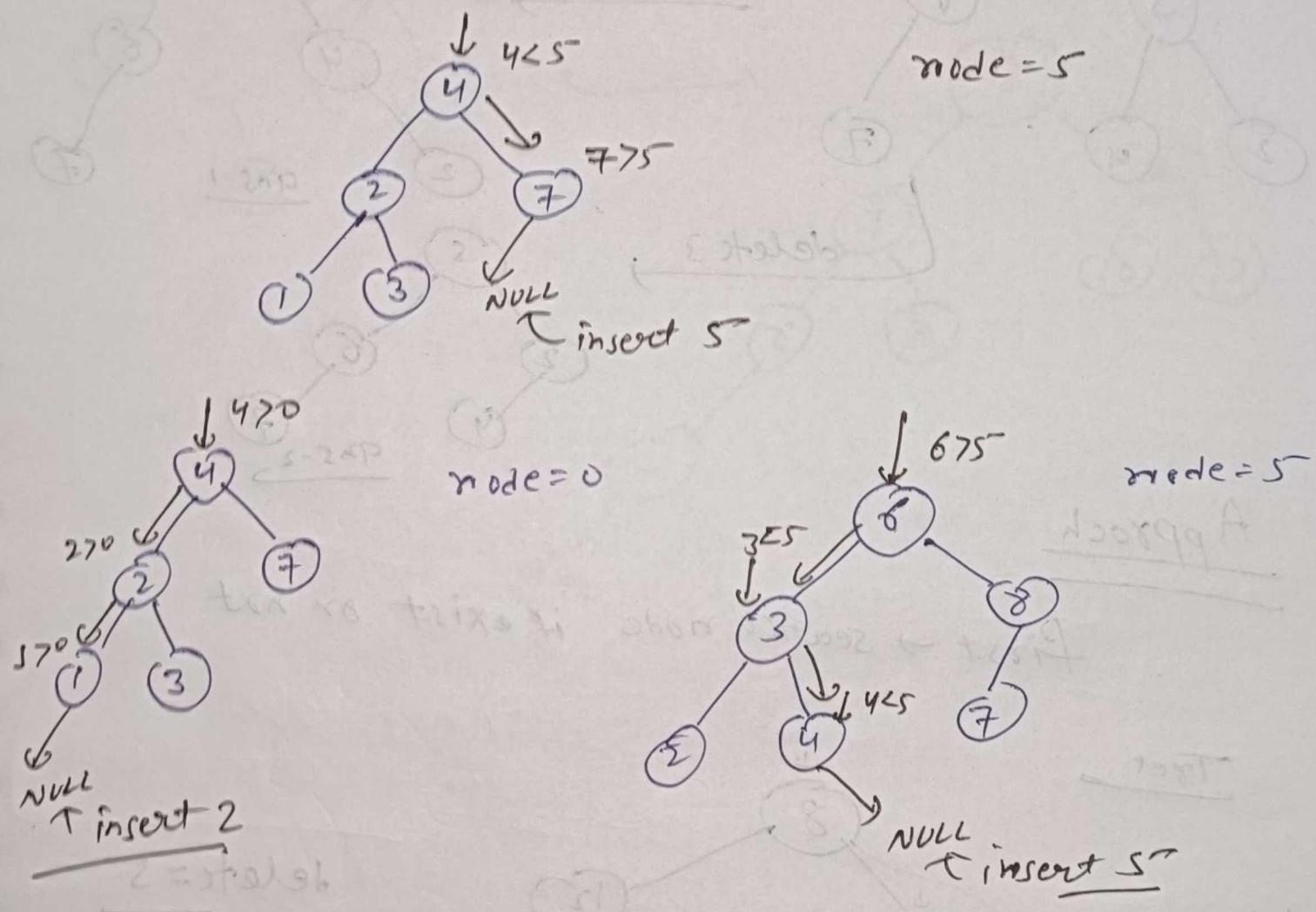
Key = 7 → 6  
10 14 → 10



## Insert a node in BST



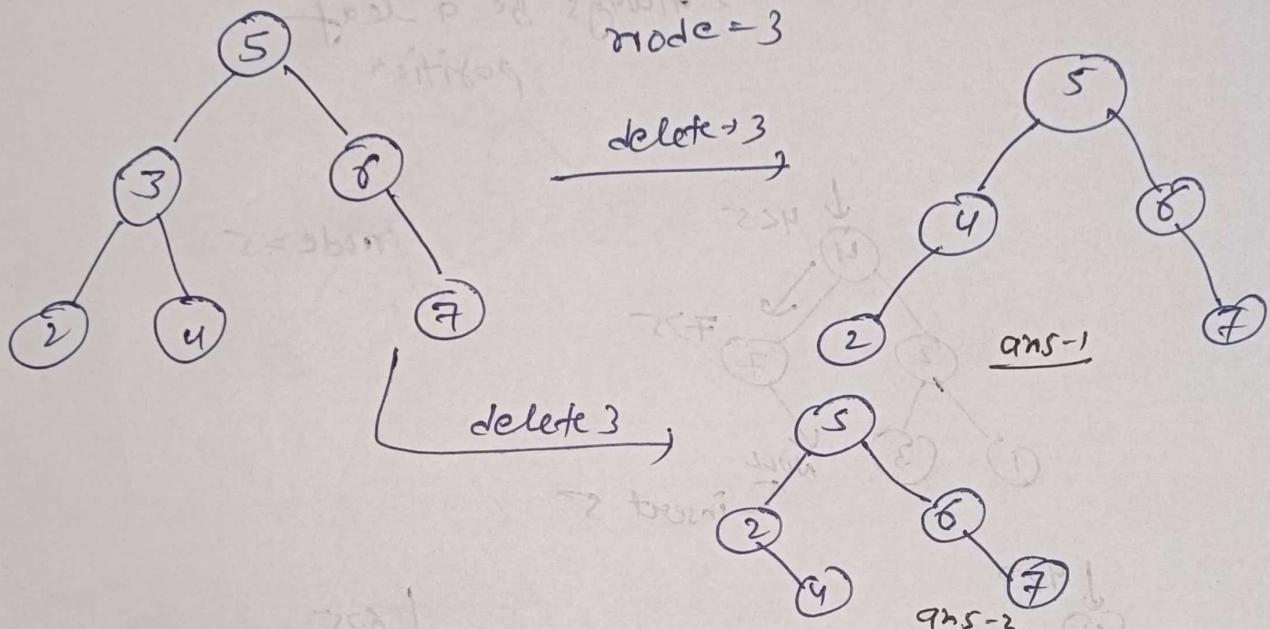
Approach → Find where it (node) can be & insert it  
 ↴ always be a leaf position



$$\boxed{T.C. = O(\log n)}$$

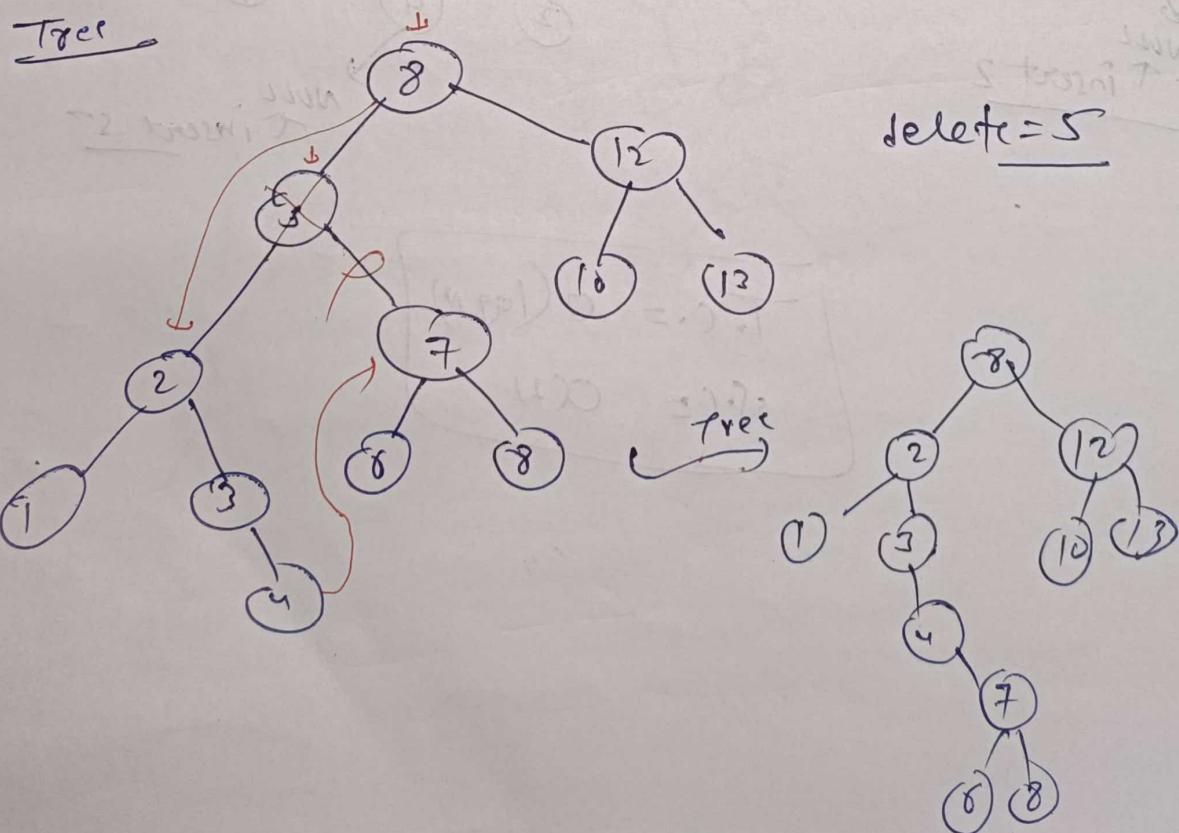
$$S.C. = O(1)$$

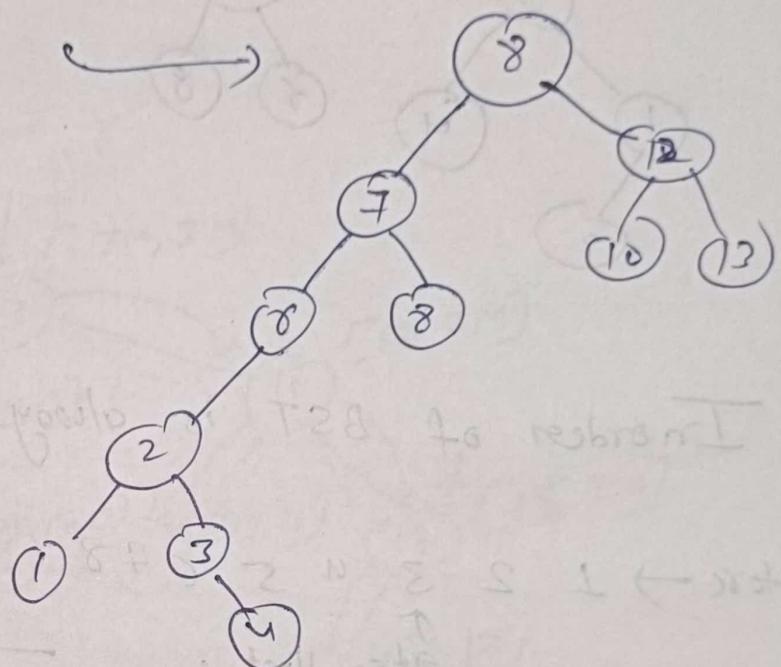
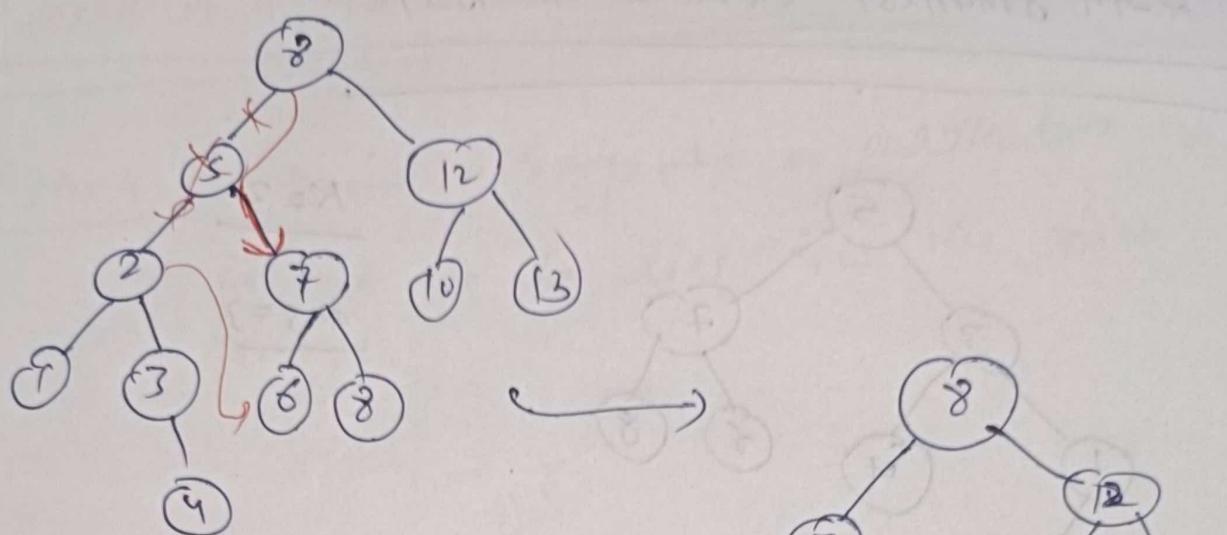
## Delete a Node in BST



### Approach

first  $\rightarrow$  search node if exist or not





$$\begin{cases} (u)_0 = 0.7 \\ (u)_0 = -0.2 \end{cases}$$

or rebalance or not

if already this map ends

then return

$(u)_0 = 0.7$

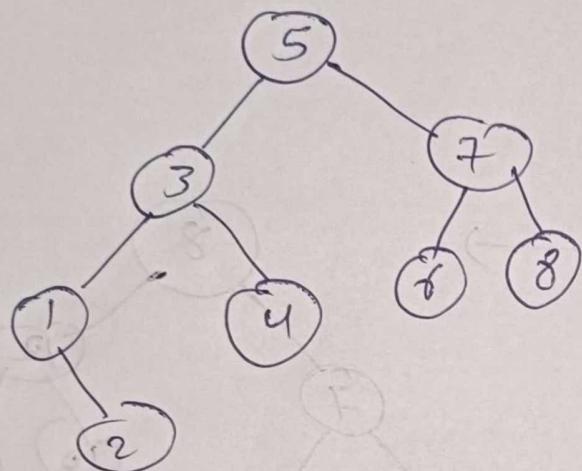
return  $\rightarrow$  rebalance

$$\begin{cases} (u)_0 = 0.7 \\ (u)_0 = -0.2 \end{cases}$$

rebalance  $\rightarrow$

$$\begin{cases} (u)_0 = 0.7 \\ (u)_0 = -0.2 \end{cases}$$

## K-th Smallest element in BST



$$K=3$$

$$\text{ans} = 3$$

Inorder of BST is always sorted order.

store  $\rightarrow 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8$

$\uparrow$   
3rd smallest  
element

$$T.C. = O(N)$$

$$S.C. = O(N) + O(N)$$

Other

take a counter = 0

when you visit a node in  
inorder  $cnt++$

if ( $cnt == K$ )

$ans = node.val$ ,

$$T.C. = O(N)$$

$$S.C. = O(N)$$

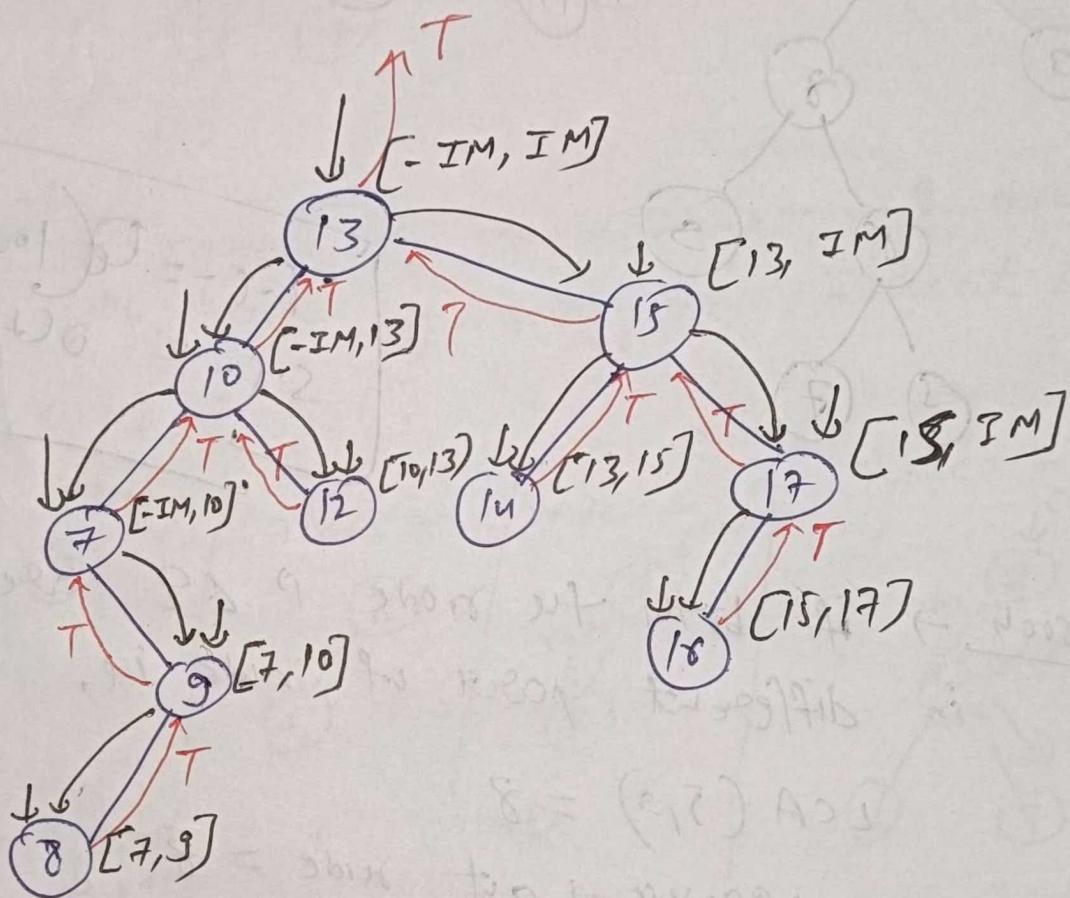
inorder  
recursion / iterative

$$\begin{cases} T.C. = O(N) \\ S.C. = O(1) \end{cases}$$

morris Traversal,

Check if a tree is a BST or BT.

Approach :- provide a range to a particular node  
i.e. it can be lies b/w the given range.

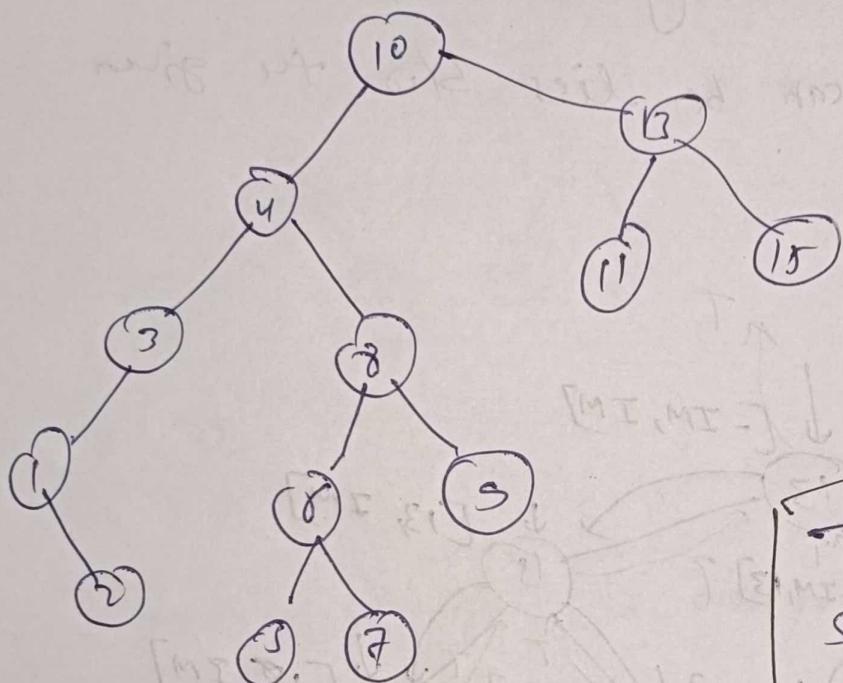


if gave go left  $\rightarrow$  update INT-MAX  
if  $\rightarrow$  visited  $\rightarrow$  INT-MIN

T.C. =  $O(N)$   
S.C. =  $O(1)$

Morris  
Traversal

## LCA in BST

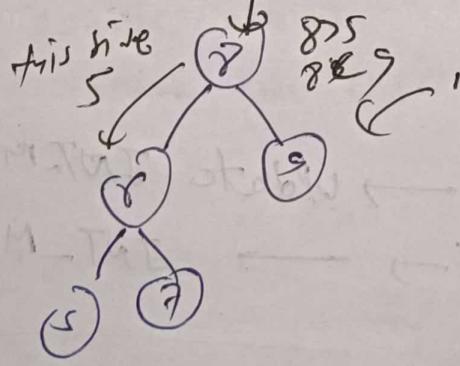


$$\begin{aligned} T.C. &= O(\log N) \\ S.C. &= O(1) \end{aligned}$$

Approach → If both the node  $P$  &  $Q$  are lies in different part of tree i.e.

$$LCA(5, 9) = 8$$

because root node = 8

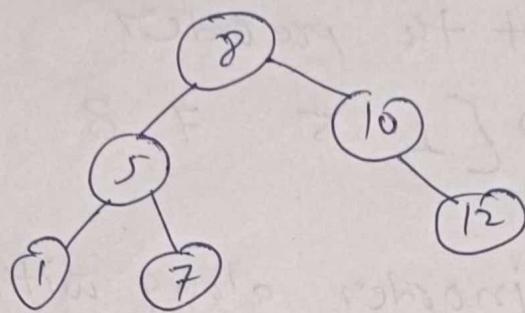


5 on left      → on visit subtree

9 on right      → the first point of partition

# Construct a BST from Preorder Traversal

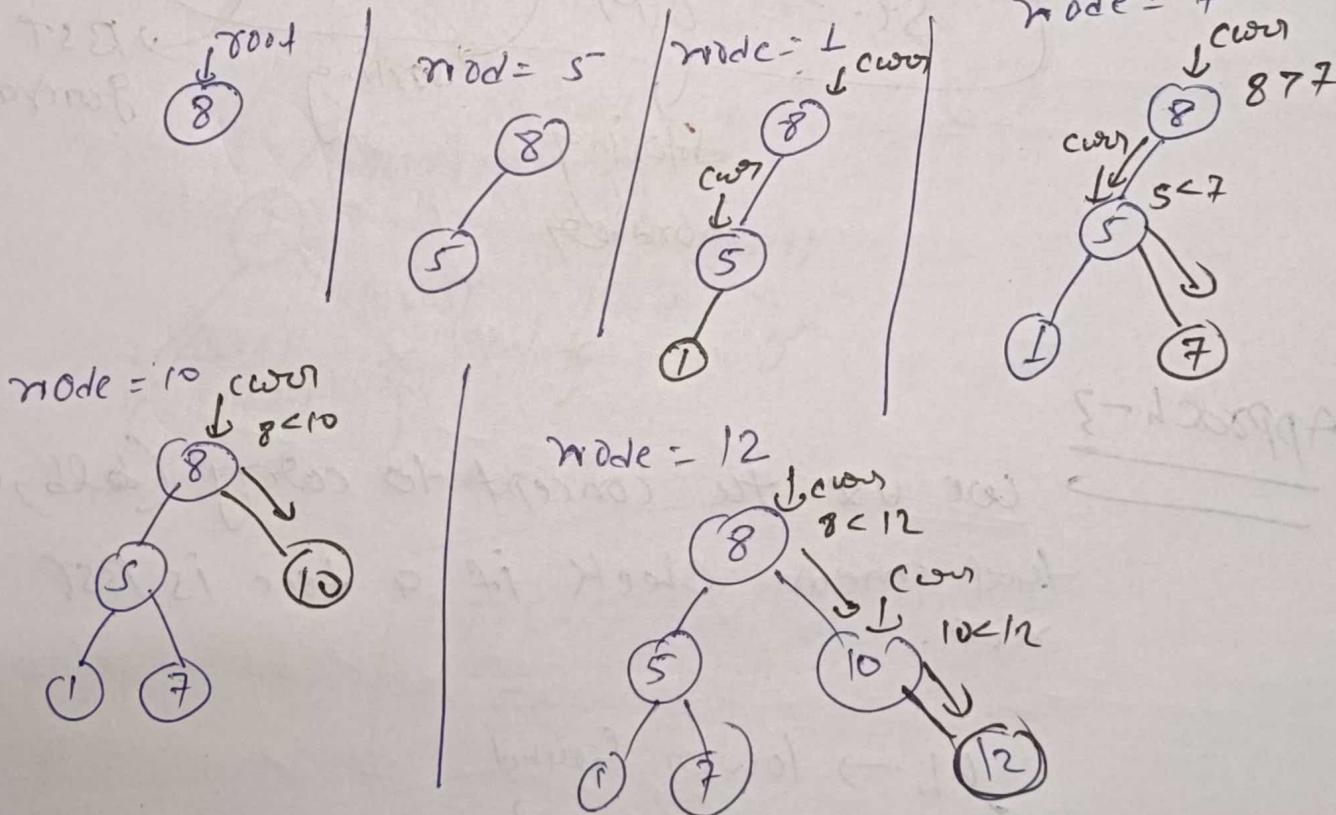
preorder  $\rightarrow [8, 5, 1, 7, 10, 12]$



## Approach - 1

Traverse the preorder array & insert the node by getting the correct position.

$[8, 5, 1, 7, 10, 12]$



$$T.C. = O(N^2)$$

$$S.C. = O(1)$$

## Approach-2

preorder  $\rightarrow [8 \ 5 \ 1 \ 7 \ 10 \ 12]$   
 $\downarrow$   
 sort the preorder  
 Inorder  $\rightarrow [1 \ 5 \ 7 \ 8 \ 10 \ 12]$

Now we have inorder along with preorder & we can generate a unique Binary tree & that unique BT will be our BST

$$\boxed{T.C. = O(N \lg(N)) + O(N)}$$

$$S.C. = O(N)$$

↑                          ↓  
 sorting                    storing  
 inorder                    inorder

BST generation

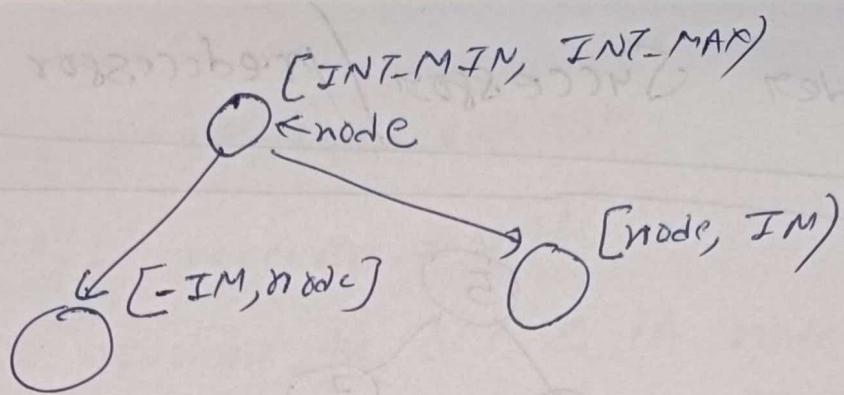
## Approach-3

we use the concept to carry  $(lb, ub)$  that mean check if a tree is BST or not.

$lb \rightarrow$  lower bound  
 $ub \rightarrow$  upper bound

→ Here we only required us.

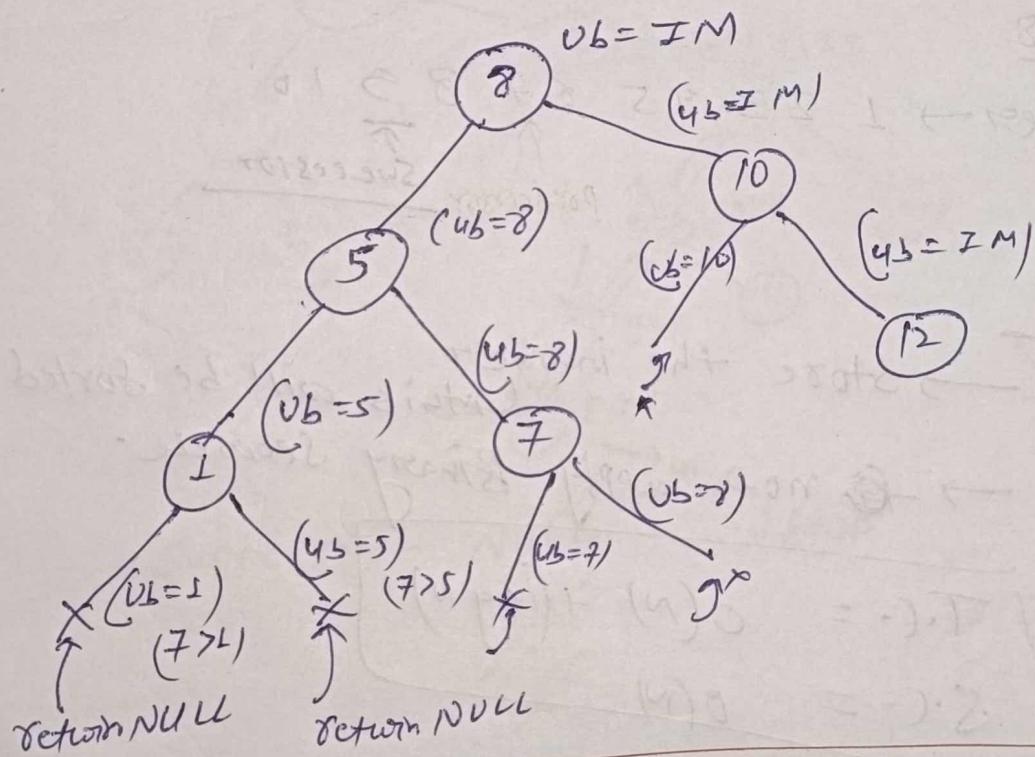
isTreeABST



80.5<sup>r</sup>

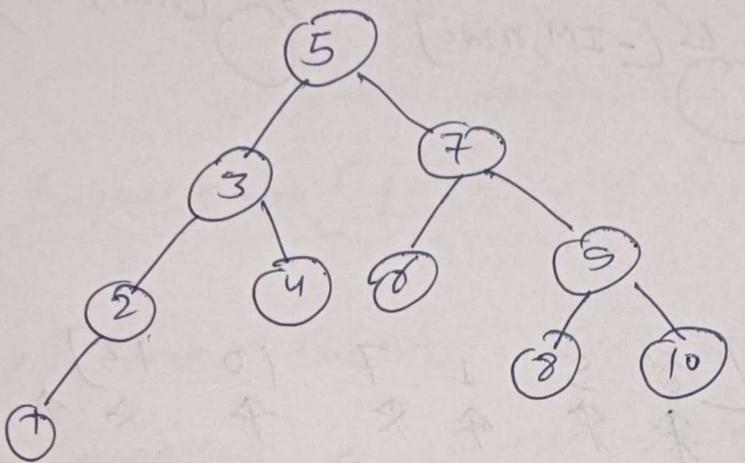
preorder

$[8 \ 5 \ 1 \ 7 \ 10 \ 12]$



T.C. =  $O(3N) \Rightarrow O(N)$   
 S.C. =  $O(N)$

# Inorder Successor / predecessor



Val = 8

inorder  $\rightarrow 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \ 9 \ 10$

predecessor successor

## Brute force

→ store the inorder  
this will be sorted

→ now apply Binary search

$$T.C. = O(N) + (\log N)$$

$$S.C. = O(N)$$

## Approach - 2

Traverse the BST in using inorder & the first value which is  $> 8$  store it & stop bcz this is your answer

$$\boxed{T.C. = O(N) \\ S.C. = O(1)}$$

→ morris  
Traversal

### Approach - 3

take a successor variable

initially  $\text{successor} = \text{NULL}$

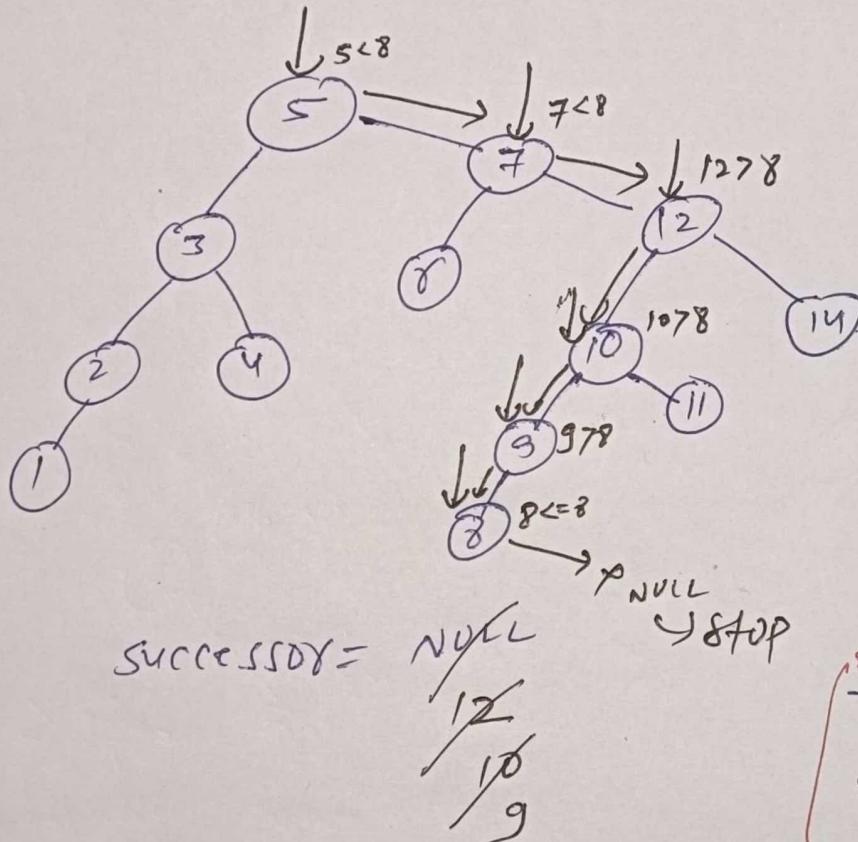
Now traverse the BST & if  $\text{node\_val} > \text{val}$   
 $\text{successor} = \text{node\_val}$

& go node  $\rightarrow$  left

else go  $\rightarrow$  right

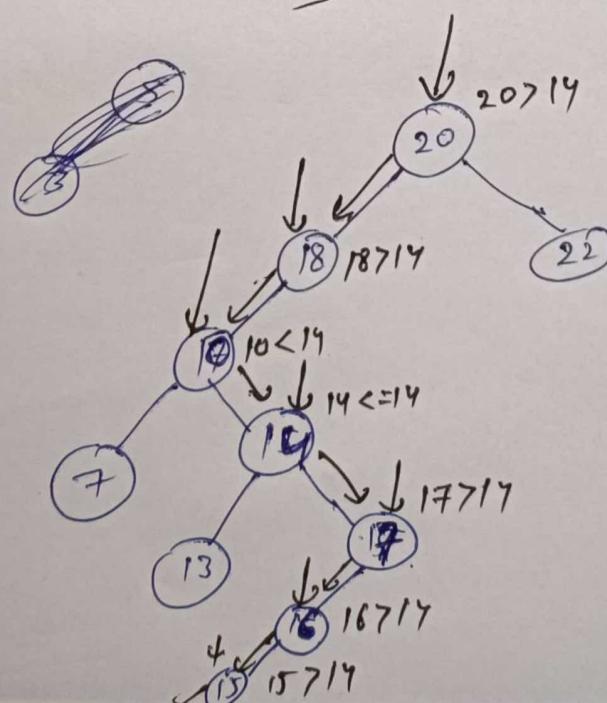
until  $\text{NULL}$

ex

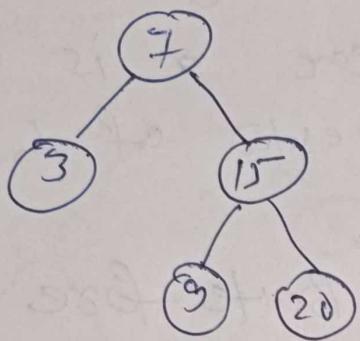


$T.C. = O(H)$   
 $S.C. = O(1)$

ex



# BST Iterator



BST Iterator(7)

next → 3

next → 7

hasNext → True

next → 9

hasNext → True

next → 15

hasNext → True

next → 20

hasNext → false

Approach-1

store the inorder

3	7	9	15	20
---	---	---	----	----

↑  
initially  
pointer

for next &  
hasNext

$T.C. = O(1)$
$S.C. = O(N)$

$T.C. = O(N)$  for inorder.

Follow up! → don't store the inorder.

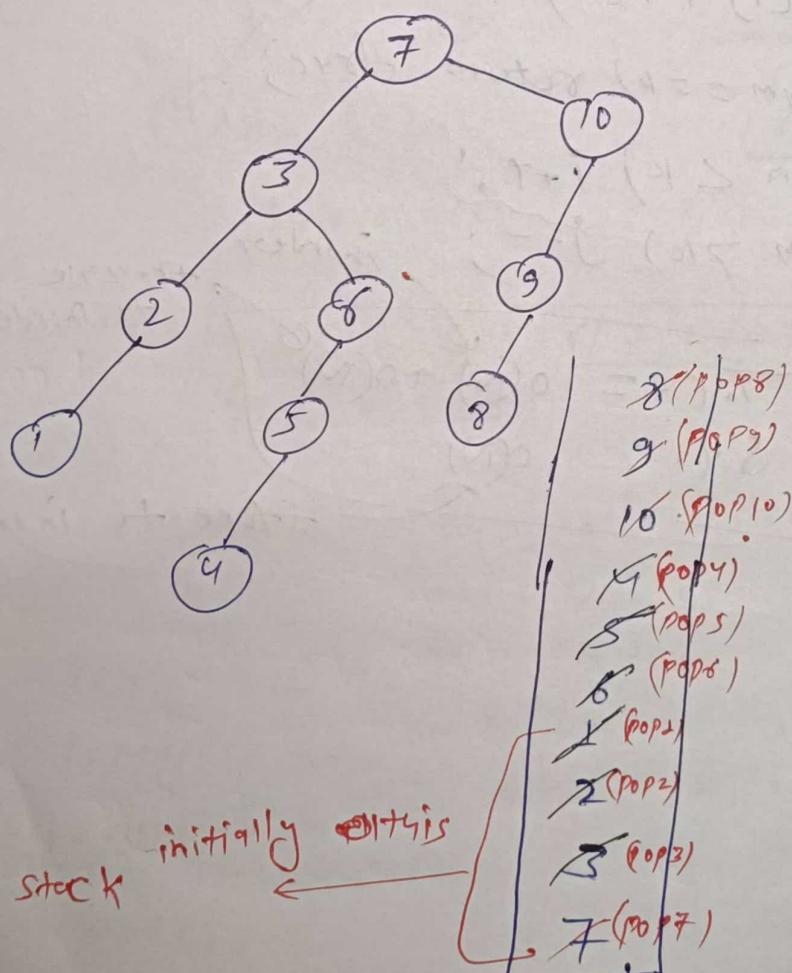
## Approach-2

Inorder  $\rightarrow$  left node right

To solve this problem we can borrow the logic of inorder.

i.e., first we store all extreme left into stack & check which next() is called the return st.top(); & st.pop()

i.e.      left    node    right  
 this is done      ↑      this means  
 next() called      ↓      now put nodes  
 right & all  
 left onto  
 stack.



BST iterator (7)

next  $\rightarrow$  1  
 $1 \rightarrow \text{right} = \text{NULL}$

next  $\rightarrow$  2  
 $2 \rightarrow \text{right} = \text{NULL}$

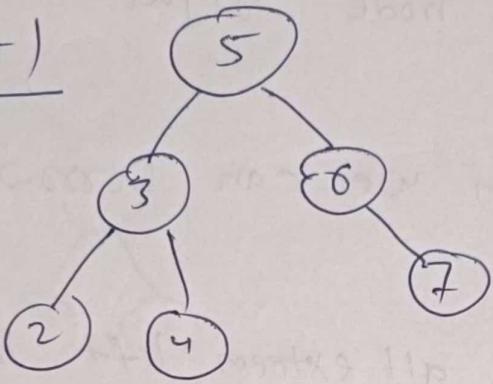
next  $\rightarrow$  3  
 $3 \rightarrow \text{right} = 6$   
 $6 \rightarrow \text{left} = 5$   
 insert all left  
 onto stack

next  $\rightarrow$  4  
 next  $\rightarrow$  5  
 next  $\rightarrow$  6  
 next  $\rightarrow$  7  
 insert  $7 \rightarrow \text{right} = 10$   
 & all 10's left

next  $\rightarrow$  8  
 next  $\rightarrow$  9  
 next  $\rightarrow$  10

## Two Sum In BST

Approach - 1



Store the inorder of BST & apply two pointer approach

inorder traversal:  
2 3 4 5 6 7  
↑  
7

$$\text{sum} = \text{in}[i] + \text{in}[j]$$

if ( $\text{sum} == k$ ) returns true;

if ( $\text{sum} < k$ ) i++;

if ( $\text{sum} > k$ ) j--;

inorder  
traverse  
the inorder

$$\text{T.C.} = O(N) + O(N)$$

$$\text{S.C.} = O(N)$$

store the inorder

## Approach-2

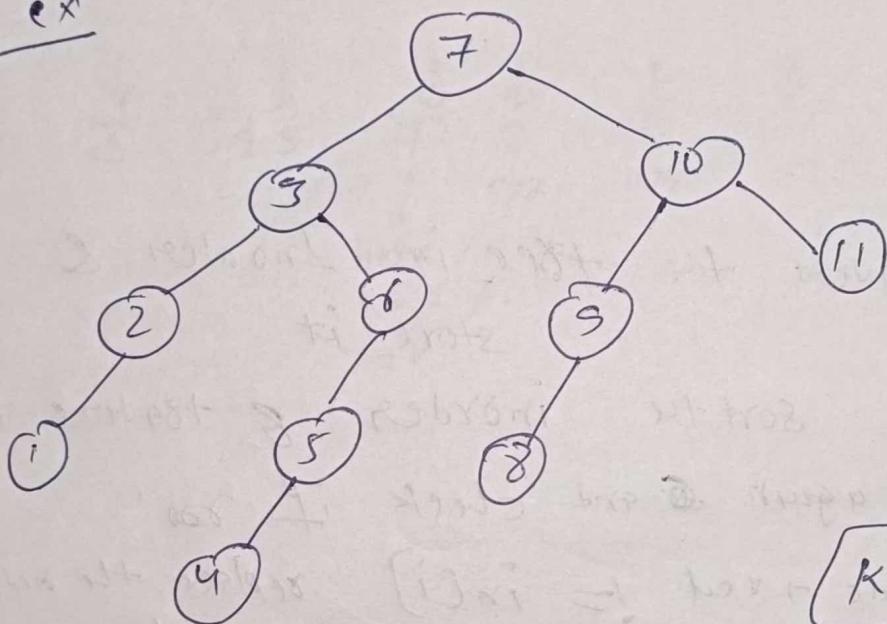
We use the concept of BST Iterators

i.e.

`next()` ← this will give you the next value in inorder

`before()` ← this will give first value in inorder

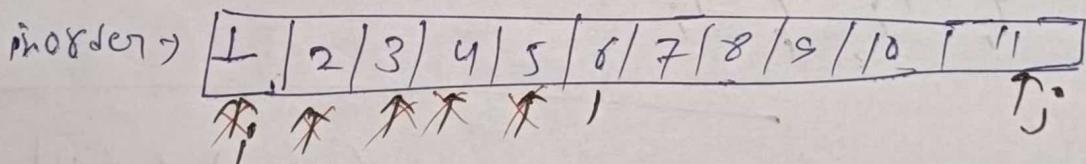
Ex



$T.C. = O(N)$   
 $S.C. = O(H) \times 2$   
 ↑  
 insert before

$$k = 16$$

$i \rightarrow \text{next}()$      $j \rightarrow \text{before}()$



$$i = \text{next}() = 1$$

$$j = \text{before}() = 11$$

$$1 + 11 = 12 < 16$$

so increase  $i$

$$2 + 11 = 13 < 16 \text{ iff}$$

$$i = \text{next}() = 2$$

$$3 + 11 = 14 < 16 \text{ iff}$$

$$i = \text{next}() = 3$$

$$4 + 11 = 15 < 16 \text{ iff}$$

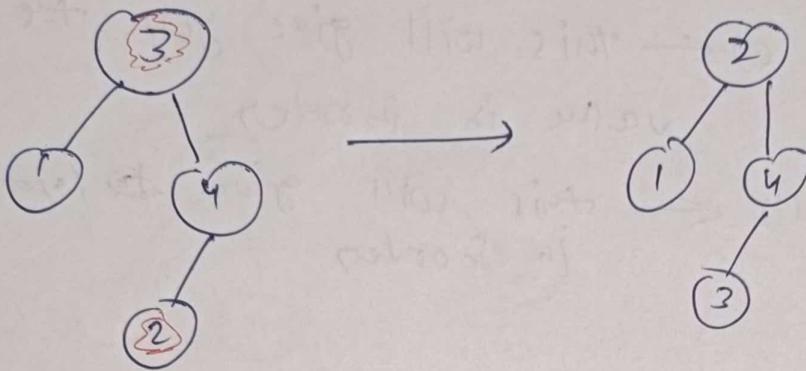
$$i = \text{next}() = 4$$

$$5 + 11 = 16 \text{ true!}$$

$$i = \text{next}() = 5$$

# Recover BST

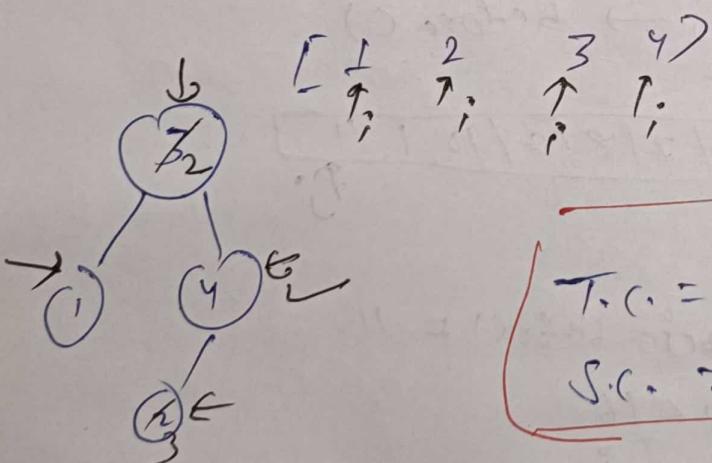
ex



Brute force :-

Traverse the tree in Inorder & store it

Now sort the inorder & traverse the tree again & check if  
node->val != in[i] replace the node  
val.



[ 1 2 3 4 ]

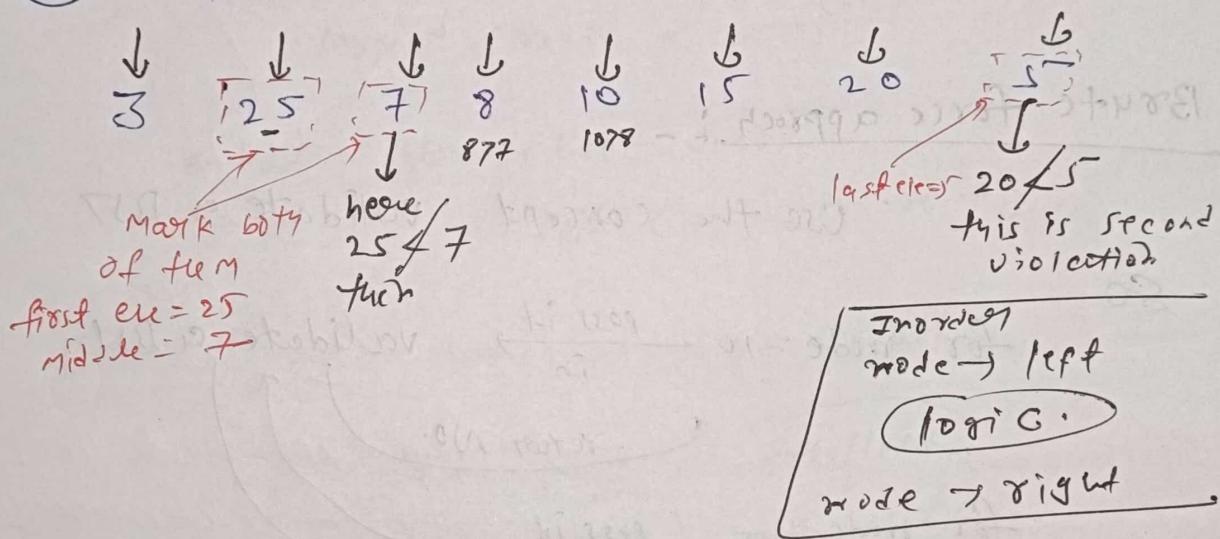
$$T.C. = O(N) + O(N \log N) + O(N)$$

$$S.C. = O(N)$$

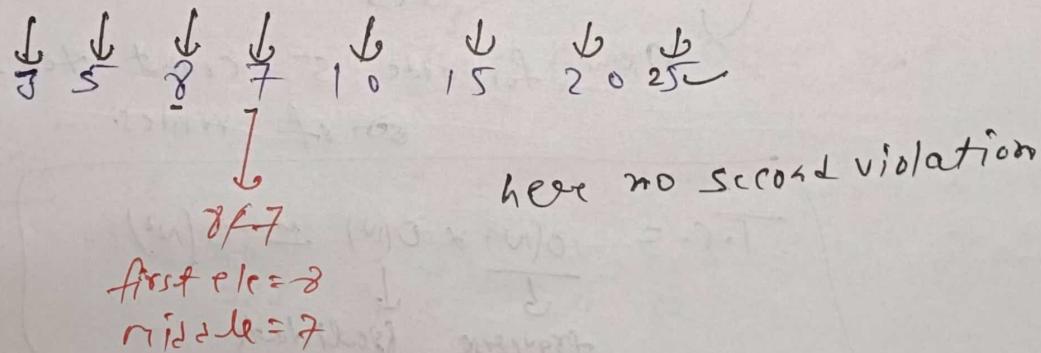
## Optimal Approach:-

If we think about a sorted array where only two elements are swapped then there are only two cases. & inorder of BST is sorted so we can figure out these two nodes in these two cases.

1. Swapped nodes are not adjacent



2. Swapped nodes are adjacent.

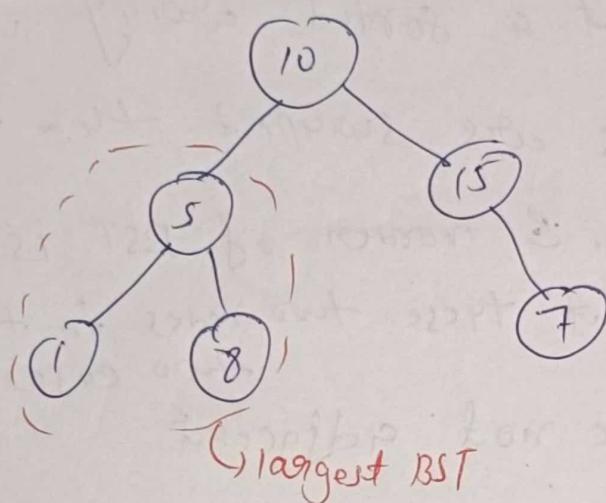


$$T.C. = O(N)$$

$$S.C. = O(1)$$

end

# Largest BST in BT



## Brute force approach :-

Use the concept validate a BST

80

for node = 10 → pass it, validate a BST

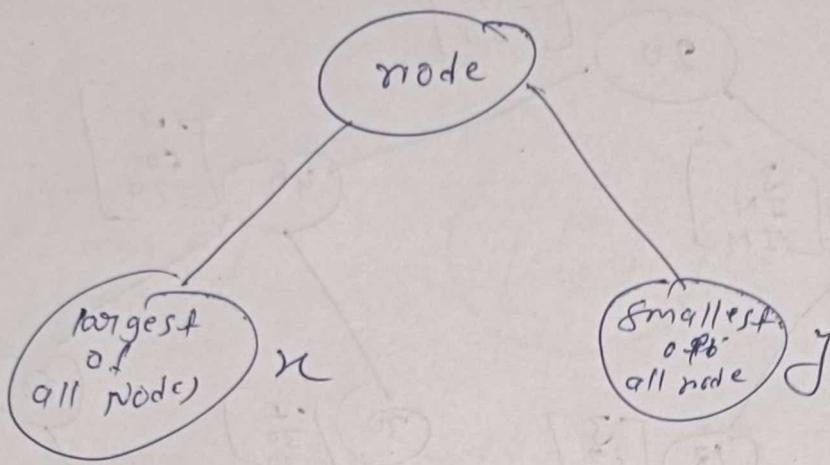
return NO.

for node = 5 → pass id  
is  
Yes

Now for node 5 count the number  
of nodes.

$$\begin{aligned} T.C. &= O(N) \times O(N) = O(N^2) \\ &\quad \downarrow \quad \downarrow \\ &\quad \text{traverse tree} \quad \text{Validate BST} \end{aligned}$$

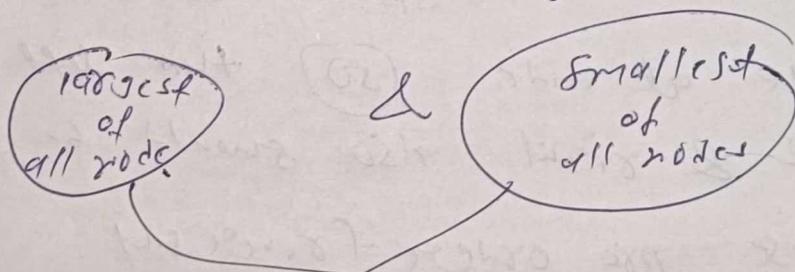
## Approach-2



• how you check size

$$\text{size} = l + n + r$$

Ques → how can we say that

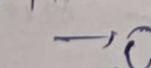


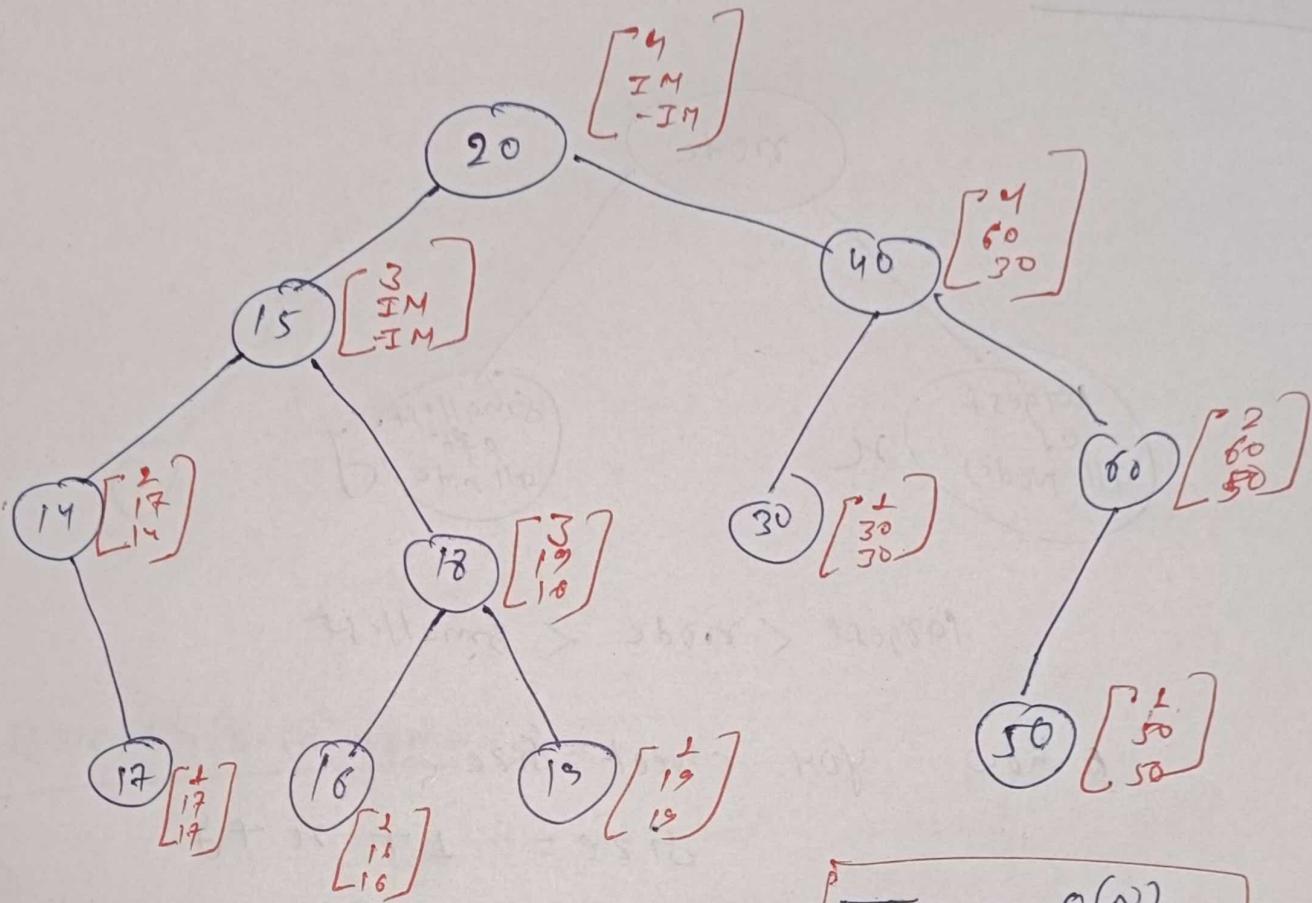
These guys are best

Soln → if we start from bottom node & if bottom guy is best then if we add some node to

if it satisfies the condition first id is also best

this  
is D.S.T.





not consider  
 recursive stack  
 space

T.C. =  $O(N)$   
 S.C. =  $O(1)$

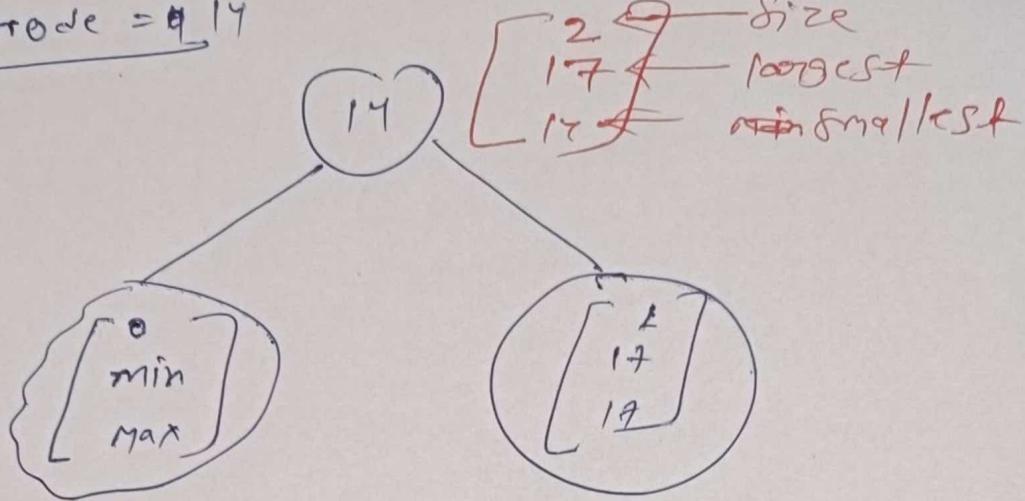
if we are at node 50 then left has to  
 be computed & right also should be computed  
 so we use pre order traversal

Preorder  $\longrightarrow$  left right root

for a leaf node  $\rightarrow$   $\begin{cases} 1 \leftarrow \text{size} \\ 17 \leftarrow \text{largest} \\ 17 \leftarrow \text{smallest} \end{cases}$

for a null node  $\rightarrow$   $\begin{cases} 0 \leftarrow \text{size} \\ \text{INT-MIN} \leftarrow \text{largest} \\ \text{INT-MAX} \leftarrow \text{smallest} \end{cases}$

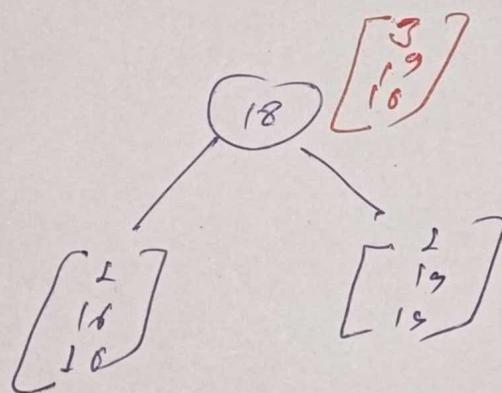
node = 14



$\text{min} < 14 < \text{max} \rightarrow \text{True}$

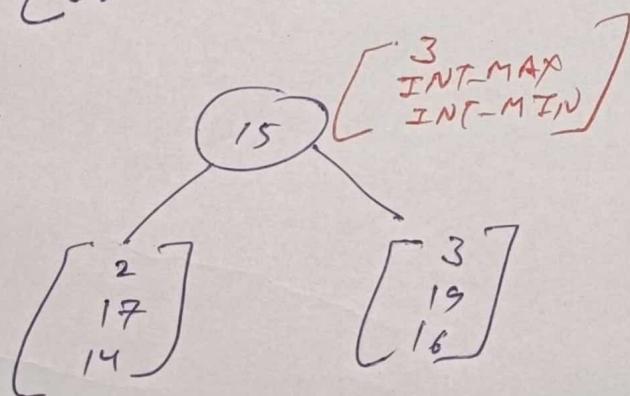
then the node 14 can make a BST

node = 18



$$\begin{aligned}16 &< 18 &< 19 \\ \text{size} &= 1 + (\text{L}) + (\text{R}) \\ &= 3\end{aligned}$$

node = 15



$17 < 15 < 16$   
violation

Imp when condition is violated then pass

largest = INT-MAX

smallest = INT-MIN

so that comparison

condition be true  
in future,

node = 20

$15 < 20 < 30$

violate

size = max (left, right)