

Q92. Subarrays with K Different Integers

e.g. $\text{nums} = [1, 2, 1, 2, 3]$ $K=2$

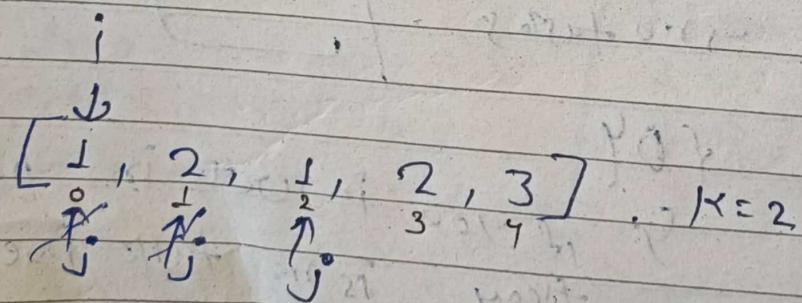
$$\text{res} = 7$$

good subarrays = $[1, 2]$, $[1, 2, 1]$, $(1, 2, 1, 2)$,
 $[2, 1]$, $[2, 1, 2]$, $[1, 2]$, $[2, 3]$

Note:- It seems like you can apply Sliding window approach but can it work with Khanda's Sliding window approach -

let's see.

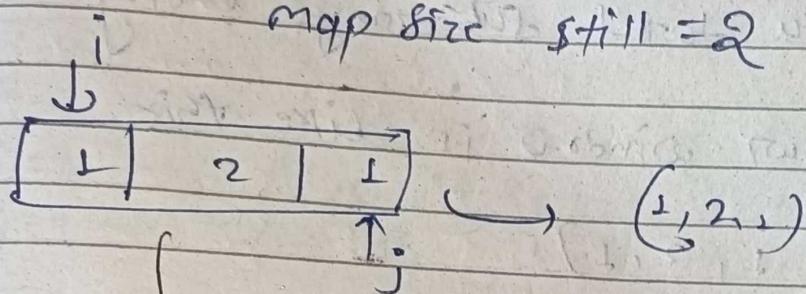
Applying Standard template of
Sliding window



res +=
at idx $j=1$
 $(1, 2)$

map	
$1 \rightarrow X$	2
$2 \rightarrow 1$	

at $idx = 2 \rightarrow$ i.e. $j = idx - 2$ &



→ यहाँ कैसे valid window है?

only $(1, 2, 1)$ good subarray है यह
or ~~1, 2~~ → यहाँ subarray exist नहीं.

Yes $\rightarrow (2, 1)$ also exist in this
valid window.

How can you find that $(2, 1)$ is
also a good subarray in the given
window?

$\Rightarrow (j-i+1) \rightarrow$ इस से हम पहचान सकते हैं कि यह window में i to j में
 j के end होने तक total
subarray कितने हैं।

If we apply this then we get

$[1, 2, 1]$

$$(j-i+1) = 2 - 0 + 1 = 3$$

this subarray
is not valid

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So by the formula $(j-i+1)$ we can compute the total subarrays ending at j .

So if your window is like this

$$\{1, 2, 1\}$$

$$\text{then } (j-i+1) = 3$$

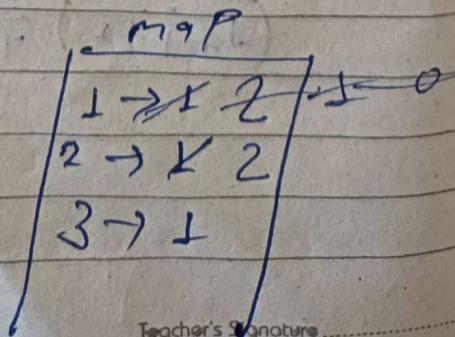
It means there is one distinct element in the subarray. As there are three unique elements and all $K \leq 3$ equal to it (less than $K+1$).

Note 1 - Here we can do like this first we can count all the subarrays in which different integers at most K i.e. $\leq K$

then we count for $\leq (K-1)$ & if we subtract these two we have only subarray in which cat is equal to K .

e.g. $\begin{matrix} i & j & j & j \\ \downarrow & \downarrow & \downarrow & \downarrow \\ [1, 2, 1, 2, 3] \end{matrix}$, $K=2$

$$\text{cat} + = (j-i+1)$$



res =

- $j=0 \rightarrow \{1\}$
 $j=1 \rightarrow \{1, 2\}, \{2\}$
 $j=2 \rightarrow \{1, 2, 2\}, \{2, 2\}, \{1\}$
 $j=3 \rightarrow \{1, 2, 1, 2\}, \{2, 1, 2\}, \{1, 2\}, \{2\}$
 $j=4 \rightarrow \{1, 2, 1, 2, 1\}, \{2, 1, 2, 1\}, \{1, 2, 1\}, \{2, 1\}$

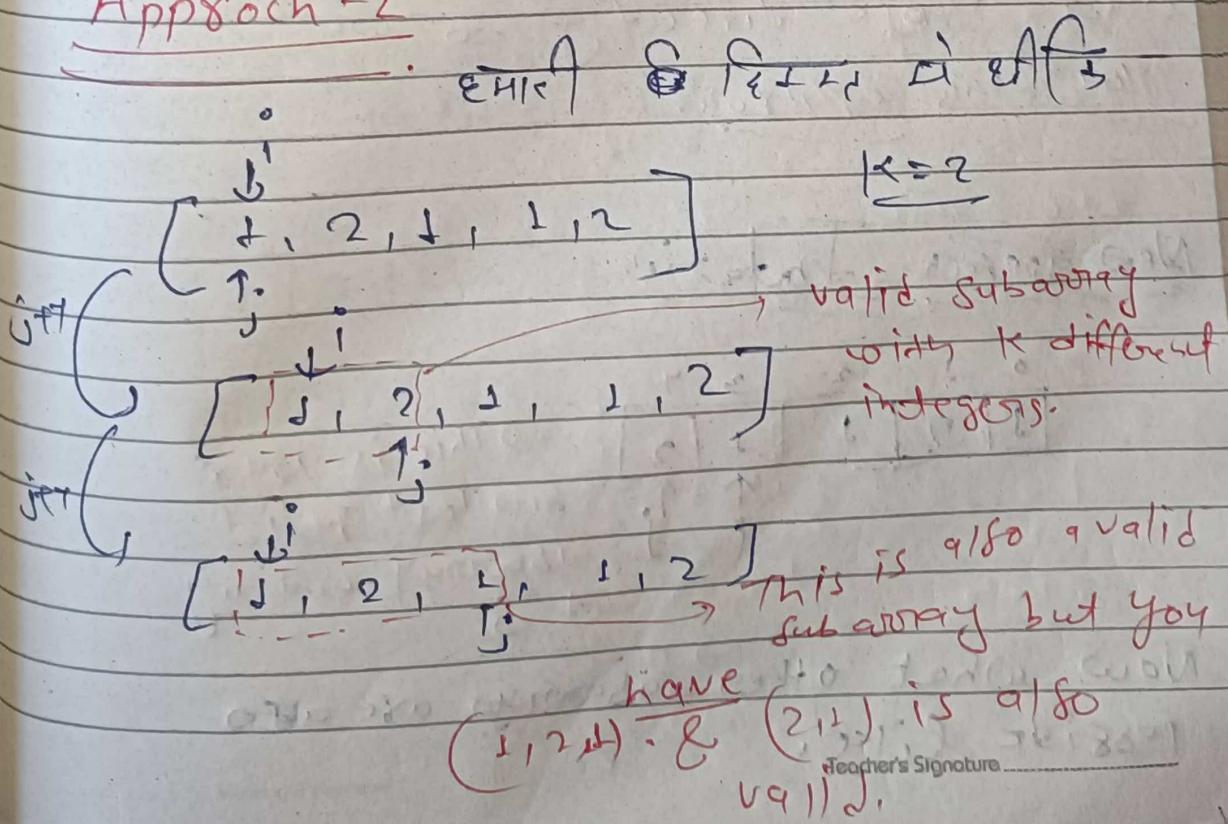
total count = 12

Now consider for $\leq (k-1) = 1 \Leftarrow 1$

total count = 5

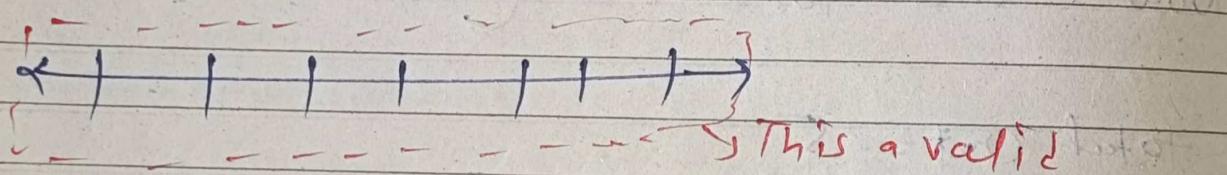
$$12 - 5 = 7$$

Approach - 2



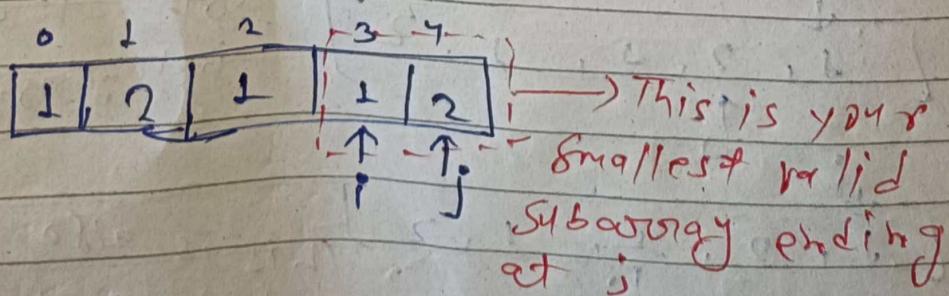
but you don't have any formula to finding that $(2,1)$ is also valid bcz if you apply $(j-i+1)$ you get all subarray ending at j .

Then our problem $(\sum_{i=1}^j)$ is like this.

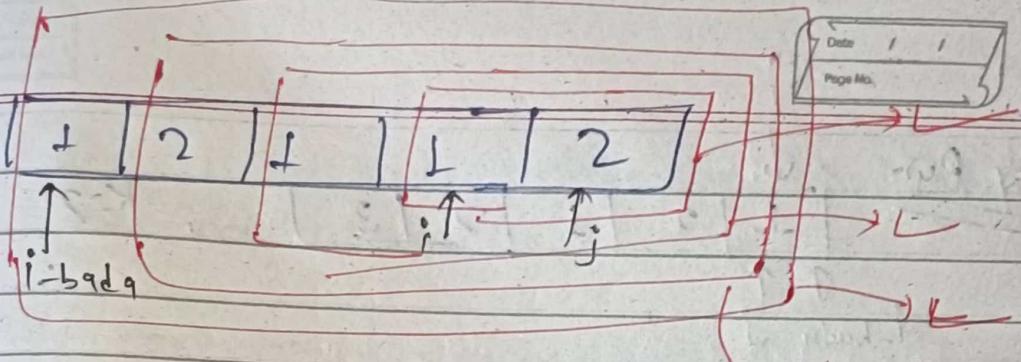


There are many subarray which also valid so we cannot figure out those directly so we use this approach.

New approach Intuition



Now what other subarrays are also possible like.



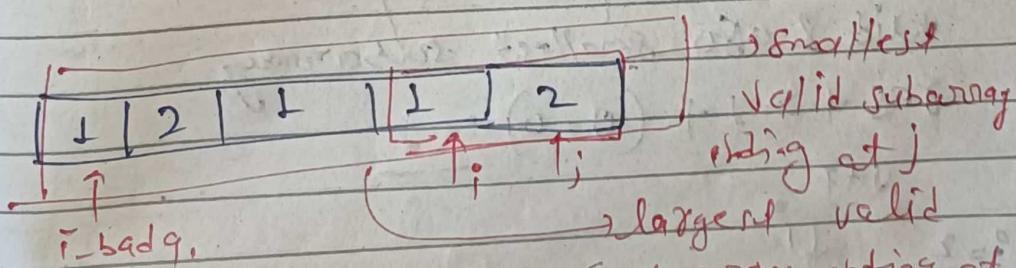
i-p.

$$\begin{aligned}
 & (1, 2) \downarrow \\
 & (1, 1, 2) \downarrow \\
 & (2, 1, 1, 2) \downarrow \\
 & (1, 2, 1, 1, 2) \downarrow
 \end{aligned}$$

or you can say that I am shifting i to left till I can get the largest valid subarray.

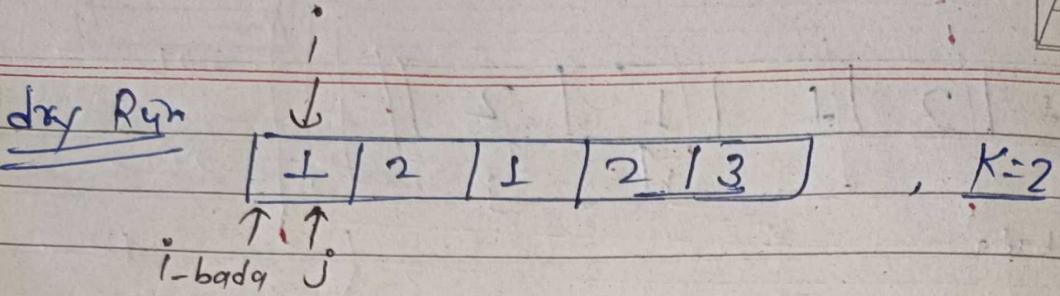
$$\text{Yes. } i = l + (i - i_{\text{badg}})$$

for smallest valid subarray for remaining valid subarray.



so from $i = l + (i - i_{\text{badg}})$ you can find the in $\log n$ valid subarrays

dry Run



$$\text{mp}[\text{nums}[i:j]] \leftarrow \begin{cases} \text{map} & \text{if } i=j \\ \text{map} & \text{if } i \neq j \end{cases}$$

while ($\text{mp.size()} > k$)

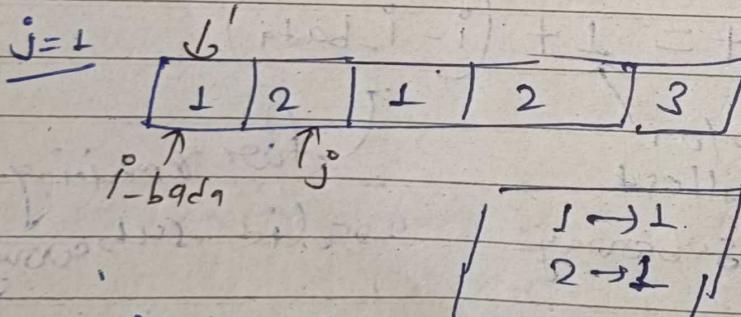
i shrink the window

i.e. $i++$ & also $i_bound = i$;

// find the smallest valid subarray

$$\text{res} += 1 + (i - i_bound)$$

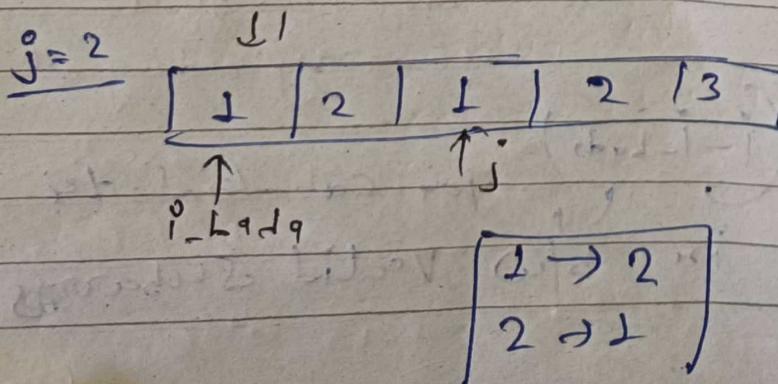
$i++$



valid & also smallest subarray

$$\text{res} += 1 + (0 - 0) = 1$$

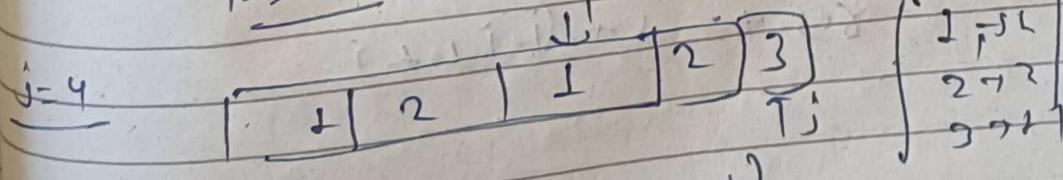
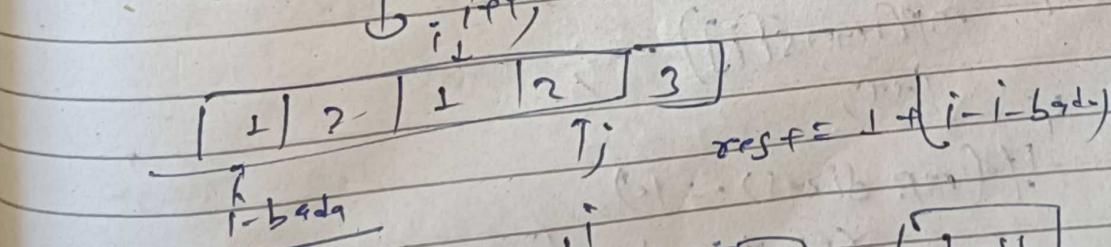
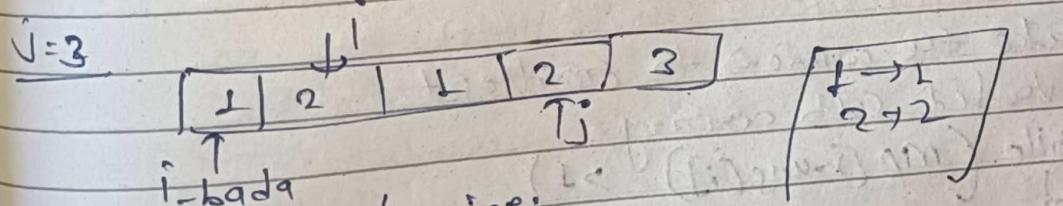
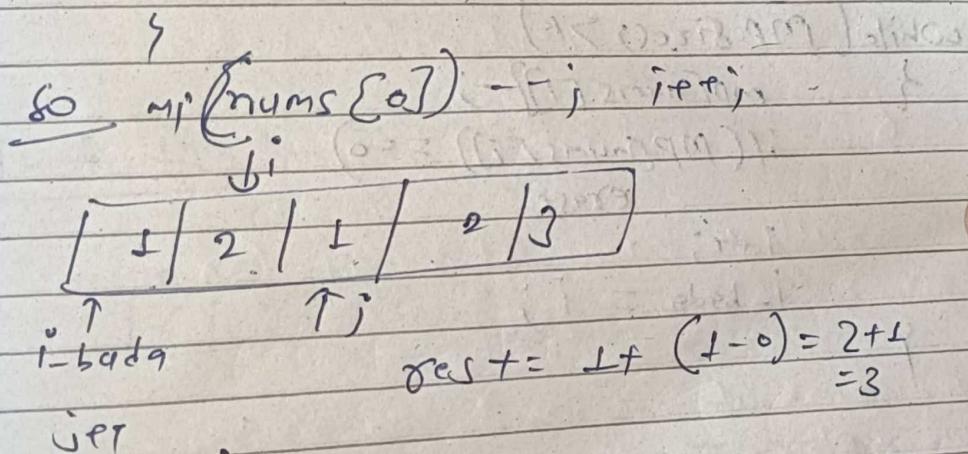
$i++$



This is a valid subarray but not the smallest valid subarray.

// how could you make the subarray the smallest valid subarray

```
while (mp[nums[i]] > 0)
{
    mp[nums[i]]--;
    i++;
}
```



while (mp.size() > 1)

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// Pseudocode

```
{ while (j < n)
    mp[nums[j]]++;
```

// Step-1: if mp.size() > k
Shrink window

```
while (mp.size() > k)
{
    mp[nums[i]]--;
    if (mp[nums[i]] == 0)
        erase;
    i++;
    i - bnd = ij;
```

// make the window to smallest

Valid subarray

```
while (mp[nums[i]] > 1)
{
    mp[nums[i]]--;
    i++;
```

If (mp.size() == 1)
 s += i + (i - ij)

i++;

}