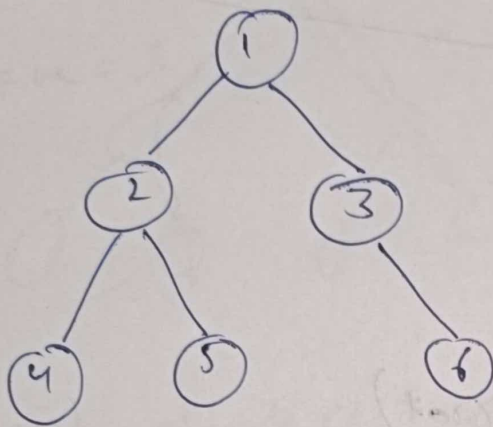


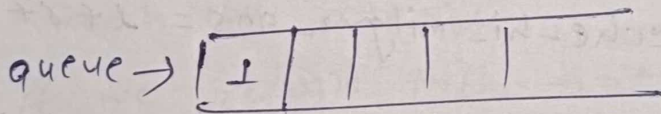
Zig-Zag Traversal



1
3 2
4 5 6

Approach :- Same approach as level order traversal.

(i) initially we take a queue & insert root in it



(ii) further we take a flag which is either 0 or 1 of the base basis of 0 or 1 we insert values into vector

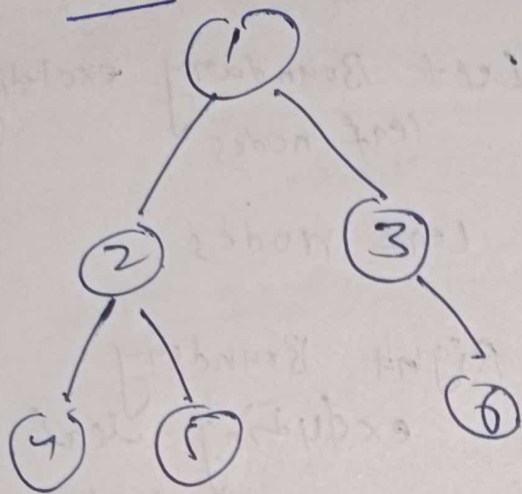
if flag == 0 that means push into vector from left to right

flag == 0 $\xrightarrow{\text{push}}$

if flag == 1 push into vector from right to left

flag == 1 $\xleftarrow{\text{push}}$

ex



$$flag = \phi \neq 0$$

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
|---|---|---|---|---|---|

result =

| | | |
|---|---|---|
| | 1 | |
| 3 | | 2 |
| 4 | 5 | 6 |

~~temp = 1~~

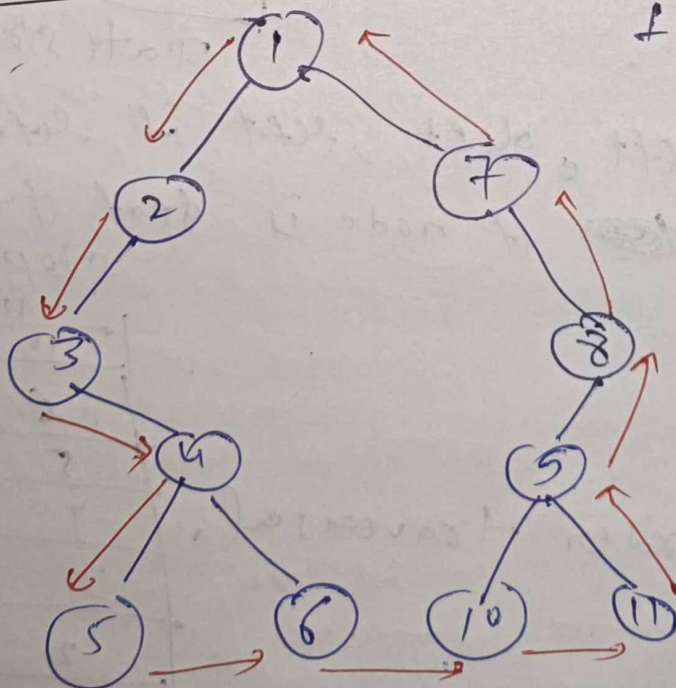
1st iteration

queue.size() = 1

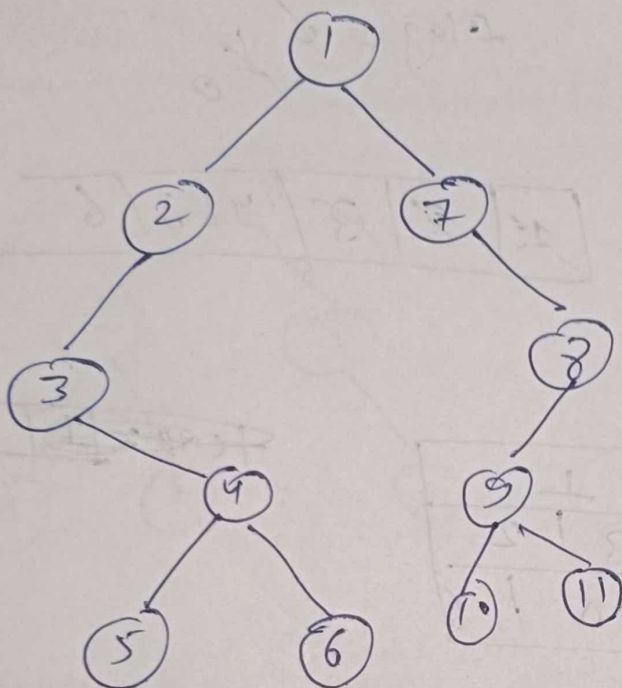
for (i = 0 to 1)

1

Boundary Traversal



1 2 3 4 5 6 10 11
5 8 7



Approach -

- (i) Left Boundary excluding leaf nodes
- (ii) Leaf nodes
- (iii) Right Boundary excluding leaf nodes

(i) Left Boundary excluding leaf

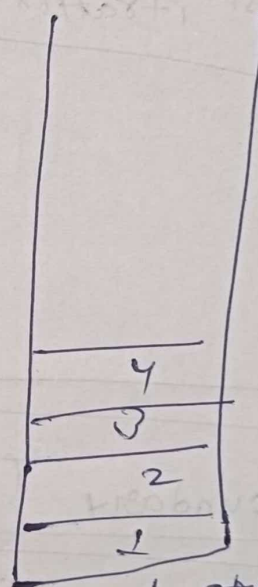
first insert root into DS

now go left of the root = 2 so insert it into DS.

Now same go left of 2 = 3

3's left == NULL go for right = 4

4's left == 5 but it is leaf then stop

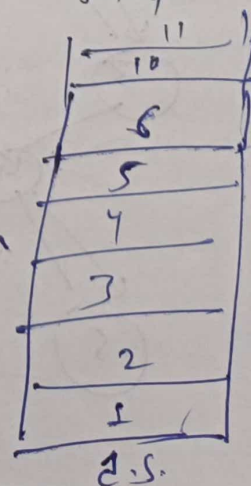


Data structure

That means go left, left, left if left not exist go right ~~then~~ if node is leaf then stop

(ii) leaf nodes

follow pre order traversal.



(iii) right boundary traversal excluding leaf & root.

temp \leftarrow vector.

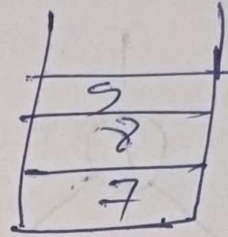
go root \rightarrow right = 7

7 \rightarrow right = 8

8 \rightarrow right = NULL So

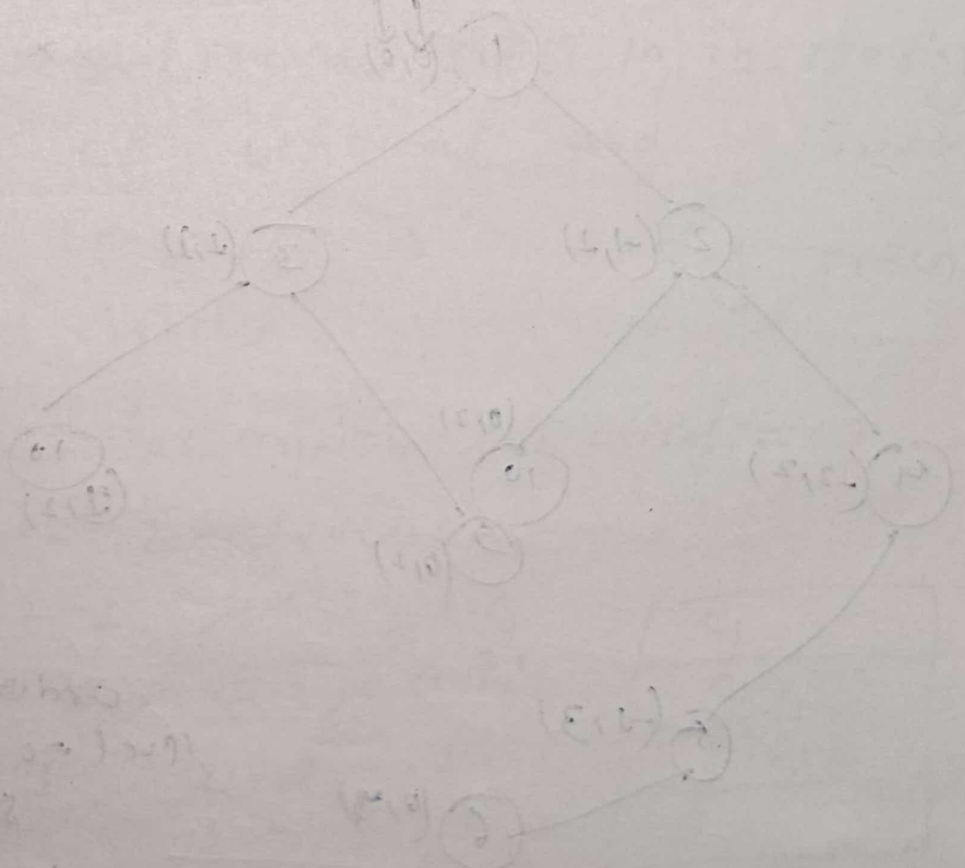
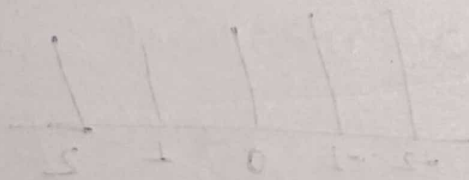
9 \rightarrow right = leaf then stop

that means right, right, right if null
left don't follow leaf.

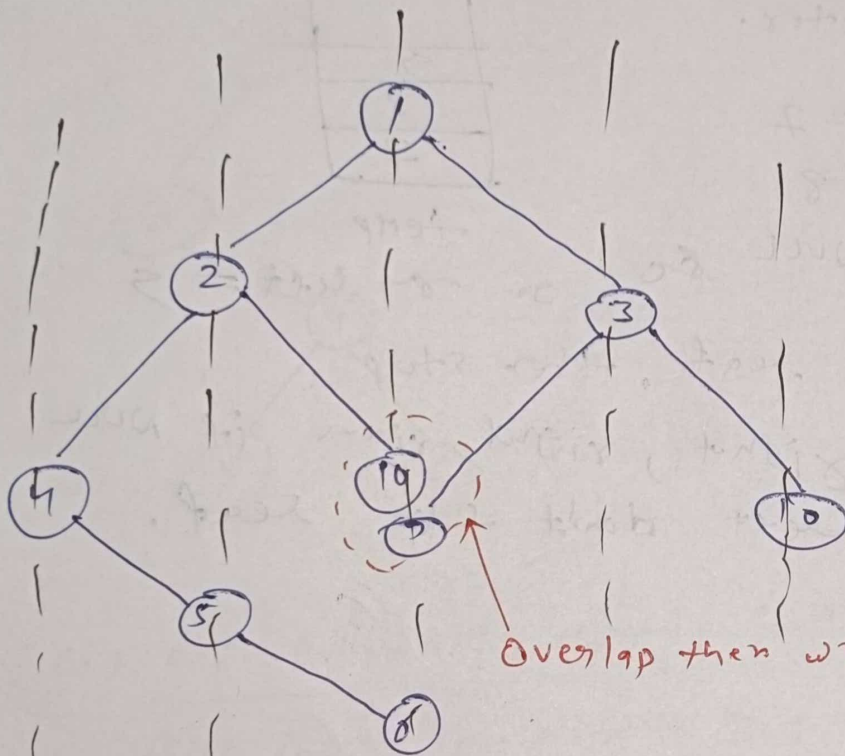


temp

or \rightarrow left = 5



Vertical Order Traversal of Binary Tree



ans

4

2 5

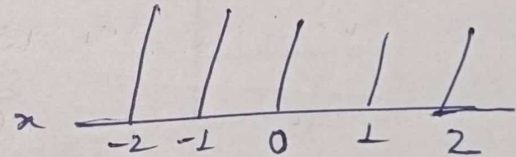
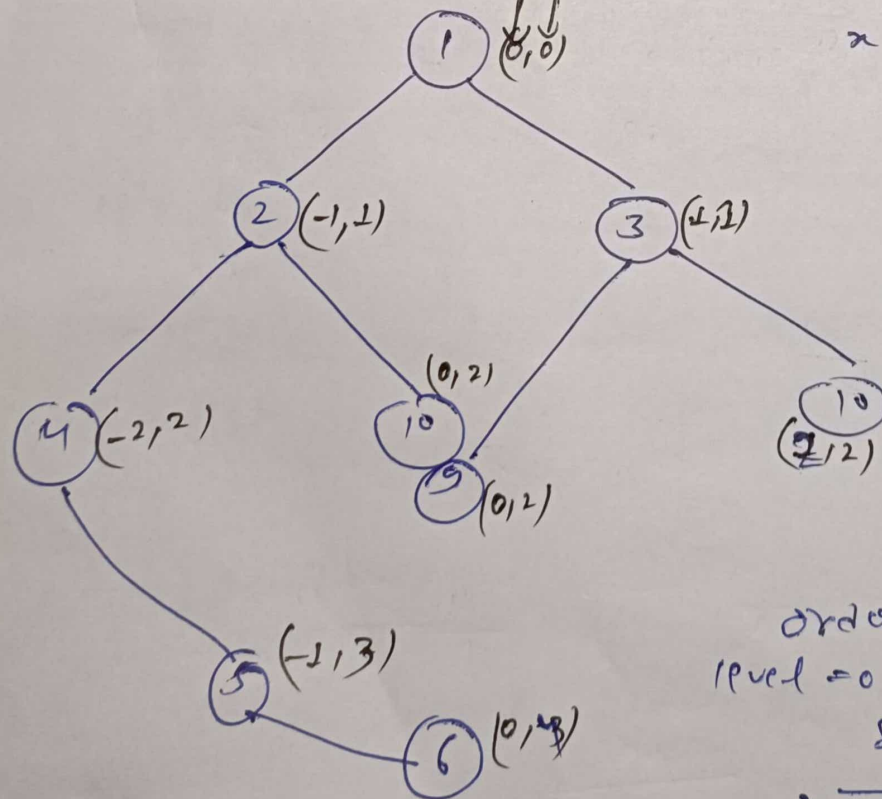
1 9 10 6

3

11

Overlap then write smaller value first.

Vertical no. $\rightarrow x$ levels



for x we can
iterate the ascending
order of x that
means first -2 , then
 -1 , 0 & so on

also same for level
iterate from ascending
order that means first
level $= 0$ then level $= 1$ 2 3
so on

level $x \rightarrow$

4

2 5

1 9 10 6

3

11

So we need to traverse every node and assign them (x, level)

where

$x = \text{vertical no.}$

$\text{level} = \text{level no. start from } 0, 1, 2, \dots$

Intuition:- we can give every vertical a number so that our traversing become easy And we assign every node to a coordinate

type of coordinate is like

$(\text{vertical no}, \text{level no})$

By this coordinating ~~our~~ our traversing become easy

How:- we ~~traverse from~~ traverse in increasing order of vertical and in vertical we traverse in increasing order of levels.

like first go for minimum vertical = -2

vertical = -2 level = 2

vertical = -1 level = 1, 3

vertical = 0 level = 0, 2, 4

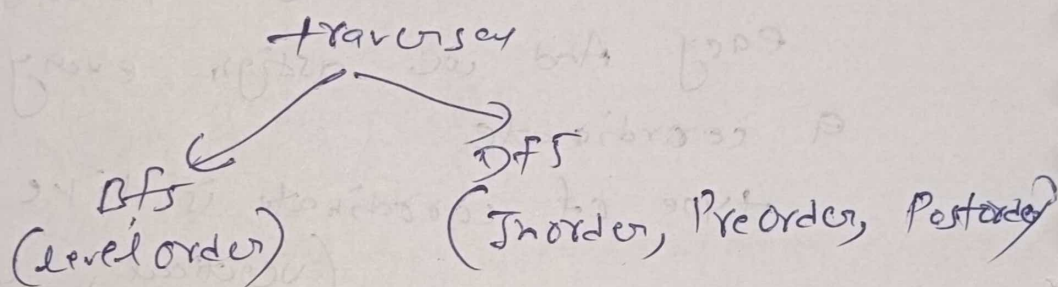
vertical = 1 level = 1

vertical = 2 level = 2

| |
|-------------|
| 4 |
| 2, 5 |
| 1, 3, 10, 6 |
| 7 |
| 1, 0 |

Now think about the Data Structure that means which kind of DS you use for solution.

Before moving on DS think about the traversal of Binary tree because mainly you have two kind of traversal



for this question you can use any of the traversal but we use level order because in our intuition we are discussing about levels so.

→ Now DS.

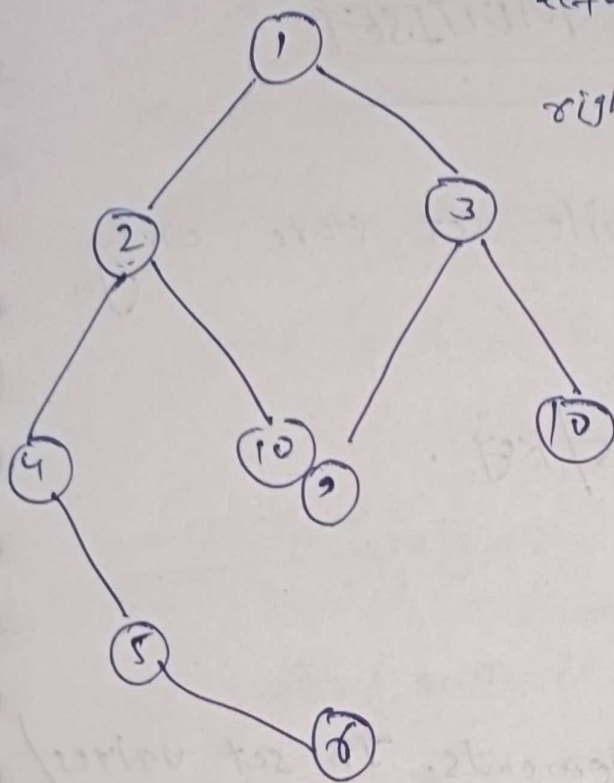
we use two data structures

(i) `queue<node, vertical, level>`

(ii) `map<int, map<int, multiset<int>>>`

\uparrow vertical \downarrow levels (levels, values)

levels store the values of and values can be same so multiset.



left \rightarrow vertical $--$ 0
level $++$
right \rightarrow vertical $++$
level $++$

node = $(1, 0, 0)$
node val vertical level

$1 \rightarrow \text{left} = (2, -1, 1)$
 $1 \rightarrow \text{right} = (3, 1, 1)$

~~$(2, -1, 1)$~~ ~~$(3, 1, 1)$~~

node = $(2, -1, 1)$
 $2 \rightarrow \text{left} = (4, -2, 2)$
 $2 \rightarrow \text{right} = (10, 0, 2)$

~~$(3, 1, 1)$~~ ~~$(4, -2, 2)$~~ ~~$(10, 0, 2)$~~

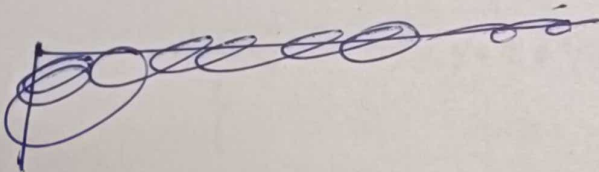
node = $(3, 1, 1)$

$3 \rightarrow \text{left} = (9, 0, 2)$

$3 \rightarrow \text{right} = (10, 2, 2)$

Data structure

| vertical | levels | values |
|----------|--------|--------|
| 0 | 0 | 1 |
| -1 | 1 | 2 |
| 1 | 1 | 3 |
| -2 | 2 | 4 |



~~$(4, -2, 2)$~~ ~~$(10, 0, 2)$~~ ~~$(9, 0, 2)$~~ ~~$(10, 2, 2)$~~

node = $(4, -2, 2)$

$4 \rightarrow \text{left} = \text{NULL}$

$4 \rightarrow \text{right} = (5, -1, 3)$

So . . .

T.C. = $O(n) \times O(\log n)$

S.C. = $O(n)$