

-: TIME COMPLEXITY :-

Sort	Time		
	Average	Best	Worst
Bubble Sort	$O(n^2)$	$O(n^2)$	$O(n^2)$
Modified Bubble Sort	$O(n^2)$	$O(n)$	$O(n^2)$
Selection Sort	$O(n^2)$	$O(n^2)$	$O(n^2)$
Insertion Sort	$O(n^2)$	$O(n)$	$O(n^2)$
Heap Sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
Merge Sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
Quick Sort	$O(n \log n)$	$O(n \log n)$	$O(n^2)$

Operation	1D Array complexity	Singly linked list complexity
Insert at beginning	$O(N)$	$O(1)$
Insert at End	$O(1)$	$O(N)$
Insert at middle	$O(N)$	$O(N)$
Delete at Beginning	$O(N)$	$O(1)$
Delete at End	$O(1)$	$O(N)$
Delete at middle	$O(N)$	$O(N)$
Search	$O(N)$ Linear Search $O(\log n)$ Binary Search	$O(N)$
Indexing	$O(1)$	$O(N)$

- (i) Reverse the singly linked list - $O(n)$
- (ii) Reverse the doubly linked list - $O(n)$
- (iii) Reverse the circular linked list - $O(n)$
- (iv) Reverse a doubly circular linked list - $O(n)$
- (v) Reverse an array - $O(n)$.

Data Structure	Access	Search	Insertion	Delete
Array	$O(1)$	$O(n)$	$O(n)$	$O(n)$
Stack	$O(n)$	$O(n)$	$O(1)$	$O(1)$
Queue	$O(n)$	$O(n)$	$O(1)$	$O(1)$
SLL	$O(n)$	$O(n)$	Begin: $O(1)$ End: $O(n)$	Begin: $O(1)$ End: $O(n)$
DLL	$O(n)$	$O(n)$	Begin: $O(1)$ End: $O(n)$	Begin: $O(1)$ End: $O(n)$
BST	$O(n)$	$O(n)$	$O(n)$	$O(n)$
B-TREE	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$
AVL-TREE	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$

Algorithm	Average	Best	Worst
Linear Search	$O(n)$	$O(1)$	$O(n)$
Binary Search	$O(\log n)$	$O(1)$	$O(\log n)$
Bucket Sort	$O(n+k)$	$O(n+k)$	$O(n^2)$
Radix Sort	$O(nk)$	$O(nk)$	$O(n+k)$
Tim Sort	$O(n \log n)$	$O(n)$	$O(n \log n)$
Shell Sort	$O((n \log n)^2)$	$O(n)$	$O((n \log n)^2)$
Counting Sort	$O(n+k)$	$O(n+k)$	$O(n+k)$
Randomized Quick Sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$

	$O(V^2)$ matrix Representation
Dijkstra	$O(E \log V) = O(V \log V)$ adjacency list representation (Fibonacci Heap)
Bellman Ford	$O(VE)$
Floyd Warshall	$O(V^3)$ There are three nested loops that run through the vertices of the graph
Kruskal's	$O(E \log E) = O(E \log V) \rightarrow$ Sparse Graphs.
Prim's	$O(E \log V) \rightarrow$ Dense Graphs prim's algorithm can be improved using Fibonacci Heaps to $O(E + \log V)$.
Job Sequencing	1. Sort job according to decreasing order of deadline = $O(n \log n)$ 2. for each job find slot in array of size $n = O(n^2)$ total time = $O(n \log n) + O(n^2) = O(n^2)$.
ASP	$O(n \log n), O(n)$ (I/p Always Sorted) SRP (COMPLEXITIES)
Huffman	$O(n \log n)$
mcm	Time complexity: $O(n^3)$, Auxiliary space: $O(n^2)$.
LCS	$O(mn)$.

Algorithm	Time complexity
Breadth First Traversal for a Graph	$O(V+E)$ for adjacency list representation. $O(V^2)$ for adjacency matrix representation.
Depth First Traversal for a Graph	$O(V+E)$ for adjacency list representation. $O(V^2)$ for adjacency matrix representation.
Dijkstra's Shortest path Algorithm	Adjacency matrix - $O(V^2)$ Adjacency list - $O(E \log V)$
Topological sorting:- Shortest path in Directed Acyclic Graph	$O(V+E)$.

Note:- $O(\log \log \log n) < O(\log \log n) < O(\log n) < O(n \log n) < O(n^p) < O(n^{\log n}) < O(2^n) < O(n!)$

Commonly used complexity:-

for ($i=0; i < n; i++$) $\longrightarrow O(n)$

for ($i=0; i < n; i=i+2$) $\longrightarrow O(n)$

for ($i=n; i > 1; i--$) $\longrightarrow O(n)$

for ($i=1; i < n; i=i*2$) $\longrightarrow O(\log_2^n)$

for ($i=1; i < n; i=i*3$) $\longrightarrow O(\log_3^n)$

for ($i=n; i > 1; i=i/2$) $\longrightarrow O(\log_2^n)$

for ($i=n; i > 1; i=i/3$) $\longrightarrow O(\log_3^n)$.

In-place sorting:-

Ex:- Bubble sort, Insertion & Selection

Not-in-place sorting:-

Ex:- merge sort

Stable sorting:-

Ex:- Insertion, Bubble & merge sort

Adaptive sorting algorithms:-

1. Bubble sort

2. Insertion sort

3. Quick sort

Non-adaptive sorting algorithms:-

1. Selection sort

2. merge sort

3. Heap sort

Master's Theorem:-

$$T(n) = aT(n/b) + O(n^k \log^p n).$$

We compare 'a' with 'b^k' and then following cases-

Case-1:-

If $a > b^k$, then $T(n) = O(n^{\log_b a})$

Case-2:-

If $a = b^k$ then,

If $p < -1$, then $T(n) = O(n^{\log_b a})$

If $p = -1$, then $T(n) = O(n^{\log_b a} \cdot \log^2 n)$

If $p > -1$, then $T(n) = O(n^{\log_b a} \cdot \log^{p+1} n)$.

Case-3:-

If $a < b^k$ then,

If $p < 0$, then $T(n) = O(n^k)$

If $p \geq 0$, then $T(n) = O(n^k \log^p n)$.