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Quick Sort

Major Slides Content: Anany Levitin

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Quick Sort

- Select a pivot (partitioning element) here, the first element
- Rearrange the list so that all the elements in the first s
 positions are smaller than or equal to the pivot and all the
 elements in the remaining n-s positions are larger than or
 equal to the pivot



- Exchange the pivot with the last element in the first (i.e., ≤)
 subarray the pivot is now in its final position
- Sort the two subarrays recursively



Quick Sort - Algorithm

```
ALGORITHM Quicksort(A[l..r])
// Sorts a subarray by quicksort
// Input: A subarray A[l ... r] of A[0 .. n -1], defined by its left and
// right indices I and r
// Output: Subarray A[l .. r] sorted in non decreasing order
ifl < r
  s \leftarrow Partition(A[I..r]) //s is a split position
  Quicksort(A[l .. s - 1])
  Quicksort(A[s + 1 .. r])
```



Quick Sort - Algorithm

```
ALGORITHM Partition(A[l..r])
// Partitions a subarray by using its first element as a pivot
// Input: A subarray A[I..r] of A[0 .. n - 1], defined by its left and right indices I and r (I < r)
// Output: A partition of A[l .. r ], with the split position returned as this function's value
p \leftarrow A[I]
i \leftarrow l; j \leftarrow r + 1
repeat
  repeat i \leftarrow i + 1 until A[i] \geq p
  repeat j \leftarrow j - 1 until A[j] \leq p
  swap(A[i], A[j])
until i ≥ j
                          //undo last swap when i ≥ j
swap(A[i], A[j])
swap(A[I], A[i])
return j
```

Quick Sort - Example

5 3 1 9 8 2 4 7



1 2 3 4 5 7 8 9

1 2 3 4 5 7 8 9

1 2 3 4 5 7 8 9

1 2 3 4 5 7 8 9



Quick Sort - Analysis: Best Case

- The number of comparisons in the best case satisfies the recurrence:
- $C_{best}(n) = 2C_{best}(n/2) + n$ for n > 1, $C_{best}(1) = 0$
- According to Master Theorem

$$C_{best}(n) \in \Theta(n \log_2 n)$$



Quick Sort - Analysis: Worst Case

The number of comparisons in the worst case satisfies the recurrence

$$C_{worst}(n) = (n+1) + n + \dots + 3 = \frac{(n+1)(n+2)}{2} - 3 \in \theta(n^2)$$



Quick Sort - Analysis: Average Case

Let $C_{avg}(n)$ be the number of key comparisons made by Quick Sort on a randomly ordered array of size n

$$C_{avg}(n) = \frac{1}{n} \sum_{s=0}^{n-1} [(n+1) + C_{avg}(s) + C_{avg}(n-1-s)]$$
 for n>1

The solution for the above recurrence is:

$$C_{avg}(n) \approx 2n \ln n \approx 1.38n \log_2 n$$





THANK YOU

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