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RED BLACK TREE

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Balanced Binary Search Tree Revisit AVL Tree



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Red Black Tree



- A Red Black Tree is a category of the self-balancing binary search tree.
- Created in 1972 by Rudolf Bayer who termed them "symmetric binary B-trees."
- A red-black tree is a Binary tree where a particular node has color as an extra attribute, either red or black.
- These colours are used to ensure that the tree remains balanced during insertions and deletions.
- Although the balance of the tree is not perfect, it is good enough to reduce the searching time and maintain it around O(log n) time, where n is the total number of elements in the tree.

Red Black Tree

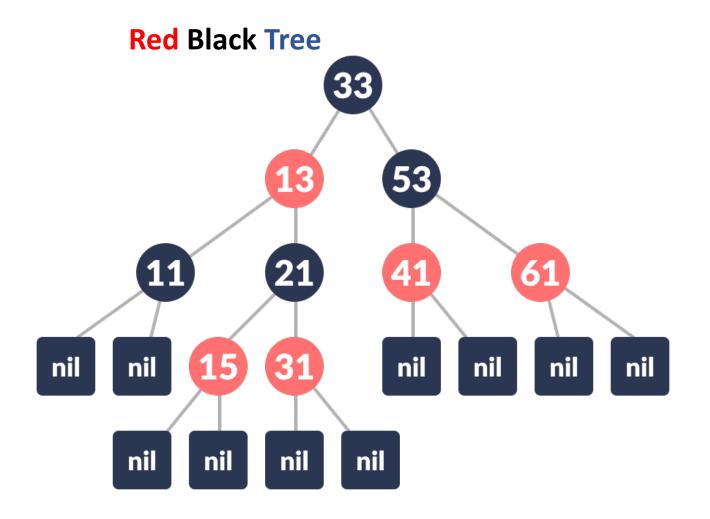


A red-black tree satisfies the following properties:

- Red/Black Property: Every node is colored, either red or black.
- **Root Property:** The root is black.
- Leaf Property: Every leaf (NIL) is black.
- Red Property: If a red node has children then, the children are always black.
- **Depth Property:** For each node, any simple path from this node to any of its descendant leaf has the same black-depth (the number of black nodes).

Red Black Tree





Each node has the following attributes:

- Color
- key
- leftChild
- rightChild
- parent (except root node)

Red Black Tree



Interesting points about Red-Black Tree:

- Black height of the red-black tree is the number of black nodes on a path from the root node to a leaf node. Leaf nodes are also counted as black nodes. So, a red-black tree of height h has black height >= h/2. Number of nodes from a node to its farthest descendant leaf is no more than twice as the number of nodes to the nearest descendant leaf.
- Height of a red-black tree with n nodes is $h \le 2 \log_2(n + 1)$.
- All leaves (NIL) are black.
- The black depth of a node is defined as the number of black nodes from the root to that node i.e the number of black ancestors.
- Every red-black tree is a special case of a binary tree.

Red Black Tree



Applications:

- Most of the self-balancing BST library functions like map and set in C++ (OR TreeSet and TreeMap in Java) use Red-Black Tree.
- It is used to implement CPU Scheduling Linux. Completely Fair Scheduler uses it.
- Besides they are used in the K-mean clustering algorithm for reducing time complexity.
- Moreover, MySQL also uses the Red-Black tree for indexes on tables.

Red Black Tree

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Operations on a Red-Black Tree

- insert a key value (insert)
- determine whether a key value is in the tree (lookup/search)
- remove key value from the tree (delete)
- print all of the key values in sorted order (print)

Red Black Tree



Search in Red-black Tree:

As every red-black tree is a special case of a binary tree so the searching algorithm of a red-black tree is similar to that of a binary tree.

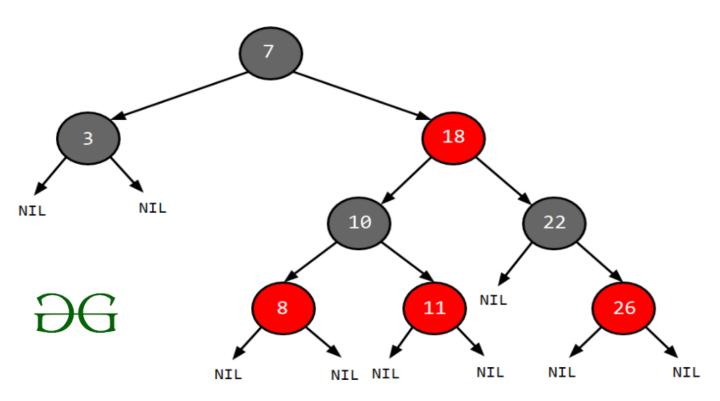
```
searchElement (tree, val)
Step 1: If tree -> data = val OR tree = NULL
Return tree
    Else If val data
        Return searchElement (tree -> left, val)
        Else Return searchElement (tree -> right, val)
        [ End of if ]
[ End of if ]
```

Step 2: END

Red Black Tree



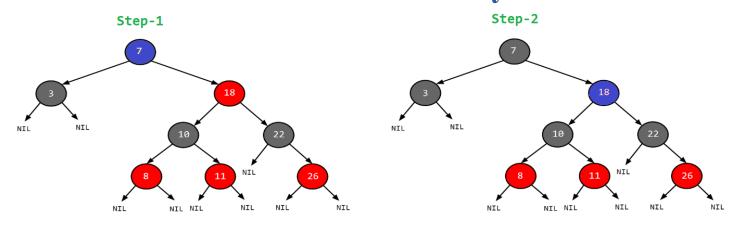
Search in Red-black Tree: search for the key 11

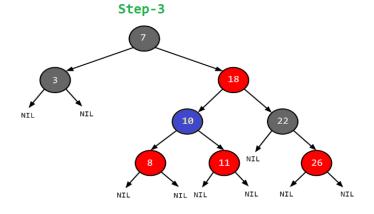


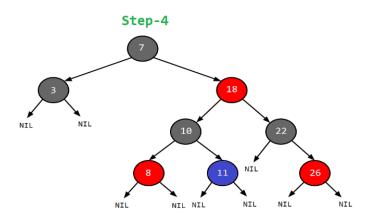
- 1.Start from the root.
- 2. Compare the inserting element with root, if less than root, then recurse for left, else recurse for right.
- 3.If the element to search is found anywhere, return true, else return false.

Red Black Tree

Search in Red-black Tree: search for the key 11









Red Black Tree - Insertion



Let x be the newly inserted node.

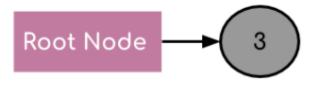
- 1.Perform standard BST insertion and make the colour of newly inserted nodes as RED.
- 2.If x is the root, change the colour of x as BLACK (Black height of complete tree increases by 1).
- 3.Do the following if the color of x's parent is not BLACK and x is not the root.
- a) If x's uncle is RED (Grandparent must have been black from property 4)
- (i) Change the colour of parent and uncle as BLACK.
- (ii) Colour of a grandparent as RED.
- (iii) Change x = x's grandparent, repeat steps 2 and 3 for new x.
- b) If x's uncle is BLACK, then there can be four configurations for x, x's parent (p) and x's grandparent (g) (This is similar to AVL Tree)
- (i) Left Left Case (p is left child of g and x is left child of p)
- (ii) Left Right Case (p is left child of g and x is the right child of p)
- (iii) Right Right Case (Mirror of case i)
- (iv) Right Left Case (Mirror of case ii)

Red Black Tree - Insertion

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Create a red-black tree with elements 3, 21, 32 and 15.

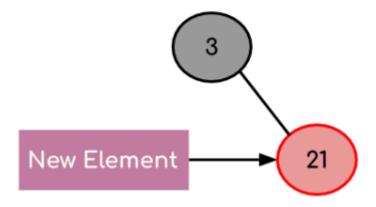
Step 1: Inserting element 3 inside the tree.



Red Black Tree - Insertion

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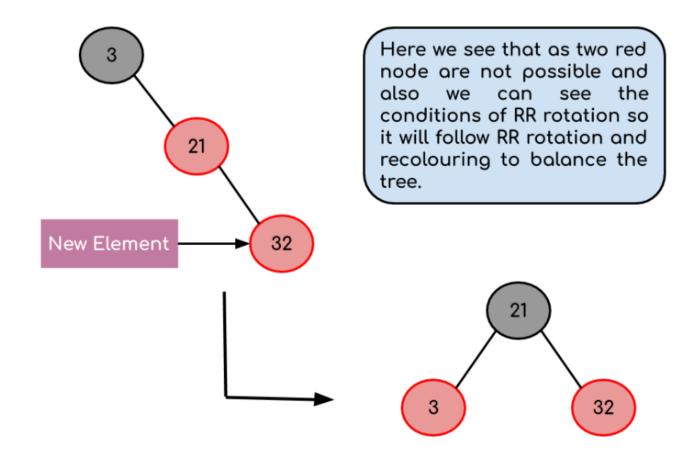
Step 2: Inserting element 21 inside the tree.



Red Black Tree - Insertion

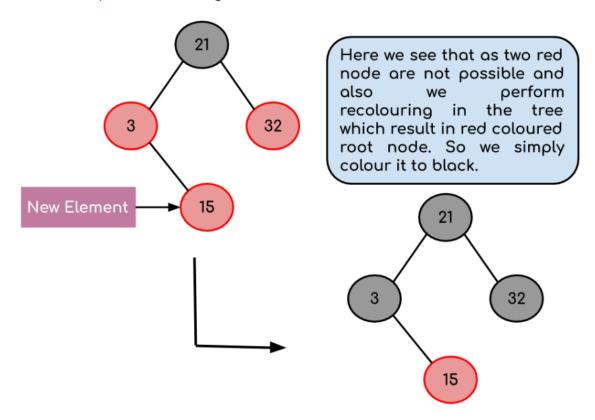
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Step 3: Inserting element 32 inside the tree.



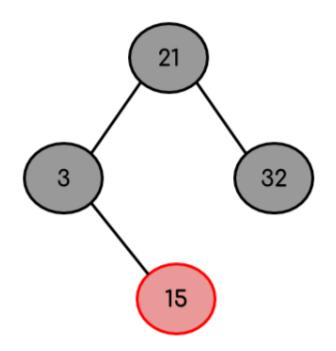
Red Black Tree - Insertion

Step 4: Inserting element 17 inside the tree.





Red Black Tree - Insertion





Red Black Tree - Insertion



Create a red-black tree with elements 1,2,3,4,5,6,7,8,9,10,11,12,13.



THANK YOU

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