

Shylaja S S

Department of Computer Science & Engineering



# **Assignment Problem**

Major Slides Content: Anany Levitin

Shylaja S S

Department of Computer Science & Engineering

#### **The Assignment Problem**

• There are n people who need to be assigned to n jobs, one person per job. The cost of assigning person i to job j is C[i, j]. Find an assignment that minimizes the total cost



## **The Assignment Problem**

## Example

|          | Job 1 | Job 2 | Job 3 | Job 4 |
|----------|-------|-------|-------|-------|
| Person 1 | 9     | 2     | 7     | 8     |
| Person 2 | 6     | 4     | 3     | 7     |
| Person 3 | 5     | 8     | 1     | 8     |
| Person 4 | 7     | 6     | 9     | 4     |



#### **The Assignment Problem**

### Algorithmic Plan

- 1. Generate all legitimate assignments
- 2. Compute their costs
- 3. Select the cheapest one



### **The Assignment Problem**

## The Assignment Problem by Exhaustive Search

| Assignment | Cost               |  |
|------------|--------------------|--|
| 1, 2, 3, 4 | 9 + 4 + 1 + 4 = 18 |  |
| 1, 3, 4, 2 | 9 + 8 + 9 + 7 = 33 |  |
| 1, 4, 3, 2 | 9 + 6 + 1 + 7 = 23 |  |
| 1, 4, 2, 3 | 9 + 6 + 3 + 8 = 26 |  |
| 1, 3, 2, 4 | 9 + 8 + 3 + 4 = 24 |  |
| 1, 2, 4, 3 | 9 + 4 + 9 + 8 = 30 |  |



#### **The Assignment Problem**

#### **Efficiency**

- The Assignment Problem is solved by generating all permutations of n
- The number of permutations for a given number n is n!
- Therefore, the exhaustive search is impractical for all but very small instances of the problem





# **THANK YOU**

Shylaja S S

Department of Computer Science & Engineering

shylaja.sharath@pes.edu