

'Cross-over' moves in the simulation
of 2-way tape TM:

New state: q_r^* (means next state
is r)

On M_2 : $\delta(q, \langle b, 0, \text{bottom} \rangle) = (q_r^*, \langle b, x, \text{top} \rangle, R)$

$\delta(q_r^*, \langle a, b, \text{top} \rangle) = (r, \langle a, b, \text{top} \rangle, L)$

- Simulating multitape Turing machine using a single tape machine:

$\# w_1 w_2 \dots w_n \# \dot{} \# \dot{} \# \dots \#$

k tapes, $k+1$ $\#$ (separator)

$\dot{}$ means the tape head points to this a .

- In each move, we may have to 'push' symbols right if we write on a blank.

• Non-deterministic Turing Machines:

Just like Non-deterministic
finite automata (NFA).

- There could be multiple choices
for a move. $\delta(q, 0)$ can be either
 (r, x, R) or $(q, 0, L)$.

We write

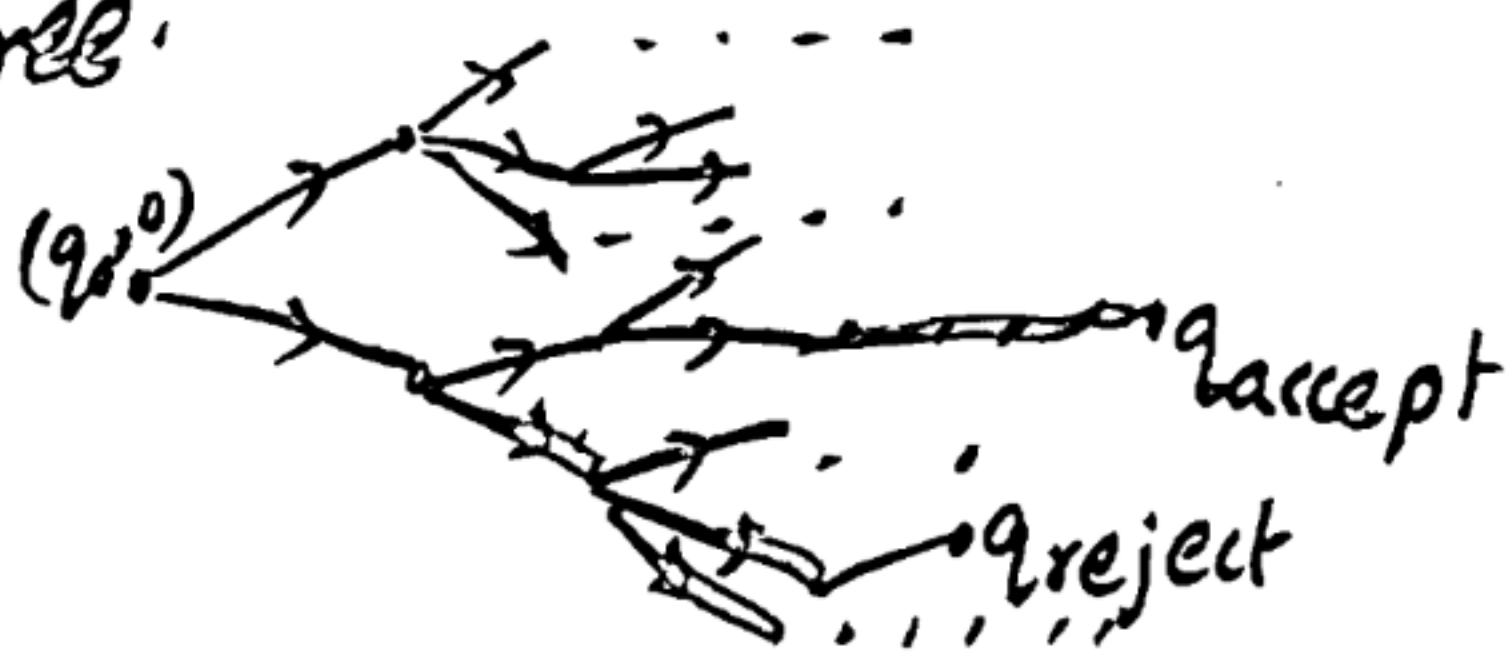
$$\delta(q, 0) = \{(r, x, R), (q, 0, L)\}$$

This is a set now.

Formally, $\delta: Q \times \Gamma \rightarrow \underbrace{2^{(Q \times \Gamma \times \{L, R\})}}_{\text{power set.}}$

Set of all subsets of $Q \times \Gamma \times \{L, R\}$.

- When do we say a non-deterministic TM "accepts" a string?
- Computation can be thought of as a tree.



- A non-deterministic TM, N , "accepts" a string if it goes to q_{accept} on any one of these branches!
- What about Reject?