# Problem Set 3 Solutions

### **BUAN 6356**

Due: Tuesday, 2017-10-24-11:59pm

### Deliverable:

an R source-code file named ps3.r

# Question 1

#### Data

hprice1.csv contains data on 88 U.S. houses, their characteristics, and their prices at the time of sale.

# Analysis

- Read the data hprice1.csv into a new variable: context1
- Run the following linear model using the 'lm' function. Store the result in: model1

$$price_i = \beta_0 + \beta_1 bdrms_i + \beta_2 lotsize_i + \beta_3 sqrft_i + e_i$$
 (1)

- Compute the OLS significance test results and the White-corrected significance test (vcovHC) results for model1.
- Run the following linear model using the 'lm' function. Store the result in: model2

$$\ln\left[\text{price}_i\right] = \beta_0 + \beta_1 \text{bdrms}_i + \beta_2 \ln\left[\text{lotsize}_i\right] + \beta_3 \ln\left[\text{sqrft}_i\right] + e_i \tag{2}$$

• Compute the OLS significance test results and the White-corrected significance test results for model2.

#### Interpretations

a. Identify which variables are significant using the OLS test for model1.

lotsize 
$$(p = 0.001823)$$
 & sqrft  $(p = 1.658e - 14)$ 

b. Which variables are still significant after using the White-corrected significance test for model 1?

only sqrft 
$$(p = 0.003406)$$

c. Identify which variables are significant using the OLS test for model2.

lotsize 
$$(p = 3.307e - 05)$$
 & sqrft  $(p = 5.006e - 11)$ 

d. Which variables are still significant after using the White-corrected significance test for model??

lotsize 
$$(p = 0.002243)$$
 & sqrft  $(p = 1.298e - 07)$ 

e. Keeping these results in mind, what is the effect of taking logs on heteroskedasticity in the data?

They mitigate the heteroskedasticity.

# Question 2

#### Data

beveridge.csv includes monthly observations on vacancy rates and unemployment rates for the U.S. from December 2000 through February 2012.

### **Analysis**

- Read the data beveridge.csv into a new variable: context2
- Run the following linear model using the 'lm' function. Store the result in: model3

$$urate_t = \beta_0 + \beta_1 vrate_t + e_t \tag{3}$$

- Compute the OLS significance test results and the Newey-West-corrected significance test (5 lags; NeweyWest) results for model3.
- Perform the level and trend KPSS tests on  $urate_t$  and  $vrate_t$  (4 tests total).
- Perform the level and trend KPSS tests on  $\Delta \text{urate}_t$  and  $\Delta \text{vrate}_t$  (4 tests total).
- Perform the level and trend KPSS tests on  $\Delta(\Delta urate_t)$  and  $\Delta(\Delta vrate_t)$  (4 tests total).
- Run the following first-difference model using the 'lm' function. Store the result in: model4

$$\Delta \text{urate}_t = \beta_0 + \beta_1 \Delta \text{vrate}_t + e_t \tag{4}$$

• Compute the OLS significance test results and the Newey-West-corrected significance test (5 lags; Newey-West) results for model4.

## Interpretations

f. Do the OLS and NeweyWest significance tests show that the coefficient on the vanancy rate is significant or not (before we correct for nonstationarity)?

Yes 
$$(p < 2.2e - 16)$$
 and Yes  $(p < 2.2e - 16)$ 

g. Based on the KPSS findings, which transformation/transformations should we apply to the unemployment rate before modeling?

After first-differencing,  $urate_t$  is level stationary.

h. Based on the KPSS findings, which transformation/transformations should we apply to the vacancy rate before modeling?

After first-differencing, vrate, is level stationary.

i. How have the significance tests changed from model3 to model4?

It is insignificant 
$$(p_{ols} = 0.79745, p_{nw} = 0.7342)$$

j. Which model better describes the data?

We can only use linear models when the series is stationary.

So model4 is the better model.

# Question 3

### Data

JTRAIN.csv has data on the scrap rates of various firms whether they were given a grant to increase their productivity. The scrap rate for a manufacturing firm is the number of defective items—products that must be discarded—out of every 100 produced. Thus, for a given number of items produced, a decrease in the scrap rate reflects higher worker productivity.

## Analysis

- Read the data JTRAIN.csv into a new variable: context3
- Generate a new variable: d88

$$\mathrm{d}88_t = \left\{ \begin{array}{ll} 1 & \quad \text{if } \mathrm{year}_t = 1988 \\ 0 & \quad \text{otherwise} \end{array} \right.$$

• Generate a new variable: d89

$$\mathrm{d}89_t = \left\{ \begin{array}{ll} 1 & \quad \text{if } \mathrm{year}_t = 1989 \\ 0 & \quad \text{otherwise} \end{array} \right.$$

- Generate a new variable indicating whether or not the firm had a grant last year: grant<sub>i,t-1</sub> [Hint: grant<sub>i,t-1</sub> is equal to zero when the year is 1987!]
- Run the following pooled linear model using the 'plm' function. Store the result in: model5

$$\ln\left[\operatorname{scrap}_{it}\right] = \alpha + \beta_1 d88_t + \beta_2 d89_t + \beta_3 \operatorname{grant}_{it} + \beta_4 \operatorname{grant}_{i,t-1} + e_t \tag{5}$$

• Run the following fixed-effects model using the 'plm' function. Store the result in: model6

$$\ln\left[\operatorname{scrap}_{it}\right] = \alpha_i + \beta_1 d88_t + \beta_2 d89_t + \beta_3 \operatorname{grant}_{it} + \beta_4 \operatorname{grant}_{i,t-1} + e_t \tag{6}$$

• Compute the OLS significance test results and the HAC-corrected significance test (Arellano) results for model6.

### Interpretations

k. Interpret the estimated coefficient on  $grant_{it}$  in model5.

Getting a grant this period is associated with a 0.20% increase in the scrap rate.

l. Interpret the estimated coefficient on  $grant_{i,t-1}$  in model5.

Getting a last period is associated with a 0.05% increase in the scrap rate.

m. How do you interpret the signs of  $\beta_3$  and  $\beta_4$ ?

The funding agency chose bad (high scrap rate) firms to get the grants.

Hence grants are positively correlated with the scrap rate.

n. Interpret the estimated coefficient on grant $_{it}$  in model6.

Getting a grant this period is associated with a 0.25% decrease in the scrap rate.

o. Interpret the estimated coefficient on  $grant_{i,t-1}$  in model6.

Getting a last period is associated with a 0.42% decrease in the scrap rate.

p. How do you interpret the signs of  $\beta_3$  and  $\beta_4$  now?

For a given firm, getting a grant is going to decrease the overall scrap rate.

q. How do the significance results change from using the HAC (Arellano) significance results compared to OLS?

 $Grant_{i,t-1}$  is significant in the OLS results at 5% but insignificant in the HAC model.