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Batesian Mimicry  
Mullerian Mimicry  
Mimicry Ring

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# Modeling the Evolution of Mimicry

Mohiul Islam<sup>1</sup>   Peter Grogono<sup>1</sup>

<sup>1</sup>Faculty of Engineering & Computer Science  
Concordia University  
Montreal, Canada

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# The Inspiration: Mimicry

# The Inspiration: Mimicry

## History

- ▶ Henry W. Bates first published in 1862.
  - ▶ **Content:** Similarity and dissimilarity between Heliconiinae and Ithomiinae butterflies.
- ▶ Bates collected 94 species of butterfly.
- ▶ Grouped according to similar appearance.
- ▶ **Discovery:** Appearance: similar, Morphological feature: different species.
- ▶ 67 of 94: Ithomiinae.
- ▶ 27 of 94: Heliconiinae.

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# The Inspiration: Mimicry

## Batesian Mimicry

- ▶ Heliconiids are,
  - ▶ conspicuously colored
  - ▶ extremely abundant
  - ▶ slow in mobility.
- ▶ Predators, insectivorous birds do not prey on Heliconiids.
  - ▶ **Reason:** Inedibility and unpalatability.
- ▶ Heliconiids are easily recalled by predators.
  - ▶ Reason: Conspicuous coloration.
  - ▶ Color acts as warning.
- ▶ Ithomiinae and Pieridae are,
  - ▶ edible
  - ▶ palatable
  - ▶ pretend like Heliconiids, enjoy protection.

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# The Inspiration: Mimicry

## Batesian Mimicry

- ▶ According to Wilcker:
  - ▶ Actor is a mime.
  - ▶ False representation of warning pattern: Mimicry.
  - ▶ Bates: First to point out, so Batesian Mimicry.
- ▶ **Model:** Animal avoided by predator for unpalatable behavior.
- ▶ **Mimic:** Imitating animal.

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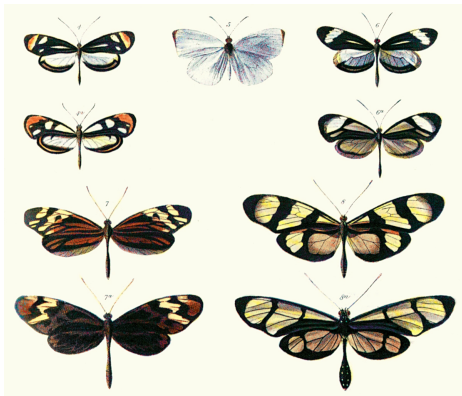
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# Batesian Mimicry

Plate from Bates (1862)



**Figure:** Plate from Bates (1862) illustrating Batesian mimicry between *Dismorphia* species (top row, third row) and various *Ithomiini* (*Nymphalidae*) (second row, bottom row).

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# Mullerian Mimicry

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- ▶ Two inedible unrelated butterfly species have similar appearance.
- ▶ Bates: Unable to explain.
- ▶ Explanation: from Fitz Muller in 1878.
- ▶ Muller's research was also in Brazil.

## Explanation:

- ▶ Predator's limited memory.
- ▶ Inedible species loose number.
- ▶ Save loss and survival of species:
  - ▶ inedible, different family
  - ▶ evolve to have similar appearance.
- ▶ Phenomenon: Mullerian mimicry, named after Fritz Muller.



# Mullerian Mimicry

Viceroy and Monarch



**Figure:** A very well-known example of mimicry. Viceroy (top). Unpalatable Monarch (bottom). Image source: Wikipedia

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# Evolutionary Dynamics

## Punctuated Equilibrium vs. Phyletic Gradualism

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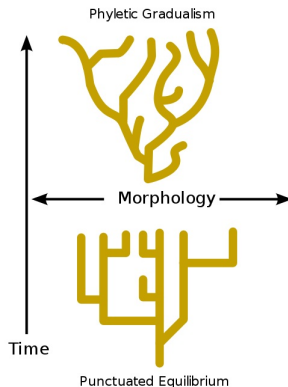
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**Figure:** Punctuated equilibrium (bottom), phyletic gradualism (top). Image source: Wikipedia

# Evolutionary Dynamics

## Turner's Two Stage Model

- ▶ Turner: Synthetic theory.
- ▶ Originated from Poulton and Nicholson.
- ▶ Mimicry arises in two steps:
  1. A comparatively large mutation achieves a good approximate resemblance.
  2. A gradual evolutionary change refines the resemblance to a higher degree of perfection.
- ▶ Theory also applied to Mullerian Mimicry.

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# Mimicry Ring

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- ▶ Examine the local butterfly fauna in any area of the world
  - ▶ all the aposomatic species
  - ▶ limited number of different patterns
  - ▶ normally far smaller than the number of species.
- ▶ Mullerian mimicry ring:
  - ▶ Each cluster of species
  - ▶ all sharing a common pattern
- ▶ All the rain forest in South and Central America,
  - ▶ most of the long winged butterflies (ithomiids, danaids and heliconids)
  - ▶ belong to one of only five different rings.

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# The Model: Evolution of Mimicry

# The Model

## Evolution of Mimicry

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- ▶ **Objective:** Build an *agent based* Artificial Life model for simulating the evolution of mimicry.
- ▶ Two species of agents:
  1. Prey
    - ▶ Model
    - ▶ Mimic
  2. Predator
- ▶ Prey pattern representation: Cellular Automata.
- ▶ Predator pattern recognition: Hopfield Network.
- ▶ Environment: Visual representation, 3D, toroidal.

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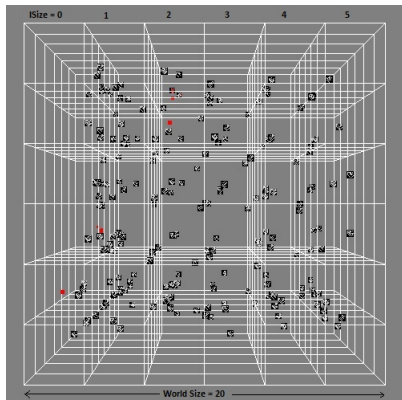
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- ▶ Ideas from Peter Grogono's Formal Artificial Life (FormAL) project.
- ▶ **Goal:**
  - ▶ Study the emergence of complexity.
  - ▶ No variable unless genetically controlled or influenced.  
*Principal not followed for Hopfield Network.*
- ▶ **Agents:**
  - ▶ Simulated organism.
  - ▶ Reproduce itself using genetic information.
  - ▶ Capable of modifying structures of genome between generations.
  - ▶ Interaction with other agents.
  - ▶ Survive and reproduce in a challenging environment.

# FormAL Framework

## Environment - Visual representation - Front



**Figure:** Three dimensional representation of the environment divided in cells. Presence of different species of agents inside.

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# The Prey

## Mimics and Models

- ▶ Agent in the FormAL environment.
- ▶ Genetic representation of pattern with Cellular Automata.
- ▶ Creates diversity of species.
- ▶ Pattern evolution is in the process of punctuated equilibrium.
- ▶ Mobility and reproduction capability controlled genetically.

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# The Prey: Mimics and Models

## Pattern Representation

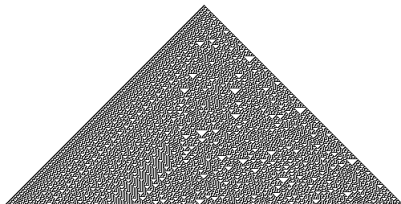


Figure: Cellular Automata Rule 30. Image source: Wikipedia

| Current Pattern          | 111 | 110 | 101 | 100 | 011 | 010 | 001 | 000 |
|--------------------------|-----|-----|-----|-----|-----|-----|-----|-----|
| New state of center cell | 0   | 0   | 0   | 1   | 1   | 1   | 1   | 0   |

Table: Cellular Automata rule

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# The Prey: Mimics and Models

## Species Diversity

- ▶ Pattern genome is 8 bit binary. Decimal range 0 to 255.
- ▶ 256 unique CA pattern.
- ▶ Linear representation of pattern stored in Hopfield Network.
- ▶ Pattern similarity: Hamming distance between linear representation.
- ▶ Single species: group of prey with a specific pattern.
- ▶ Inter species reproduction: restricted to control diversity of patterns.
- ▶ “Pattern Mutation Rate”: control diversity of new species.

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# Prey Pattern

## Genotype vs. Phenotype

- ▶ Genetic bit difference of one.
- ▶ Vastly different phenotype.

| CA Rule | 60 $\equiv$ 00111100  | 61 $\equiv$ 00111101  | 62 $\equiv$ 00111110  |
|---------|---|---|---|
| Pattern |  |  |  |

**Table:** Difference in prey pattern genotype and phenotype

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# The Prey: Mimics and Models

## Genome

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### ► 17 bit prey Genome

| Pattern(8) | Palatability(2) | Mobility(6) | Reproduction(1) |
|------------|-----------------|-------------|-----------------|
| 10101101   | 01              | 110001      | 1               |

**Table:** Distribution and purpose of each gene of the 17 bit prey genome.

# The Prey: Mimics and Models

## Punctuated Equilibrium

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- ▶ Punctuated Equilibrium:
  - ▶ inclined to cladogenesis instead of gradualism.
  - ▶ Turner's emphasis on punctuated equilibrium to explain evolution of mimicry.
  - ▶ CA pattern evolution: single mutation in the pattern genome.
  - ▶ Change of pattern:
    - ▶ not gradual
    - ▶ arbitrary discontinuous

# The Predator

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- ▶ Agent in the FormAL environment.
- ▶ Provide selection pressure for the evolution of mimicry.
- ▶ Equipped with Hopfield Network Memory.
- ▶ Mobility and reproduction capability controlled genetically.
- ▶ Unable to represent pattern recognition capability with genome.
- ▶ New predators are born with zero memory, as memory is not inherited.

# The Predator

## Learning

- ▶ Predator's interaction objective with prey is consumption.
- ▶ Consumption is based on palatability.
- ▶ If unable to consume prey is thrown back into environment.
- ▶ Store prey pattern into memory with the associated palatability.
- ▶ New pattern learned with Hebbian Learning.

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# The Predator

## Design of Memory

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- ▶ Input to Memory:
  - ▶ Each prey has an evolving CA represented by a binary Genome.
  - ▶ 2D pattern is serialized to a 1D binary array.
  - ▶ Binary representation converted to bipolar representation.
- ▶ Pattern Recognition with Hopfield Network:
  - ▶ Learning: Apply Hebbian learning to calculate weights.
  - ▶ Initialization: Input to network initialized with input vector.
  - ▶ Iterate Until Convergence: Asynchronous update of each neuron. Input: previous state.
  - ▶ Output: Finally a pattern is set as output when the network reaches convergence.

# The Predator

## Attack Algorithm

- ▶ Agent reaches 'Minimum Attack Age' it starts hunting.
- ▶ Select a random prey within vicinity (same cell).
- ▶ Involves recognition of prey pattern.
- ▶ Pattern memorization and recognition process: computationally expensive.
- ▶ Two parameters to limit
  - ▶ Hopfield Minimum Memory Size (value 2 to 6)
  - ▶ Hopfield Maximum Memory Size (value 10)
- ▶ New predator attacks without caution.
- ▶ Attacks everyone and in the process store pattern and palatability.
- ▶ When memory reaches 'Hopfield Minimum Memory Size': intelligent selection.

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# The Results

- ▶ **Objective:** Evaluate evolution of mimicry.
- ▶ **Evaluation process:**
  - ▶ Calculate number of mimicry rings.
  - ▶ Calculate size of mimicry rings:
    - ▶ Population of *palatable* species.
    - ▶ Population of *unpalatable* species.
- ▶ **Report parameters:**

| Parameter                     | Value                    |
|-------------------------------|--------------------------|
| Mimicry Ring hamming distance | 10 % of the Pattern Size |
| Number of Rings to report     | 8                        |

**Table:** Parameters to mimicry ring report.

# Two Prey Species

## Initial Configuration

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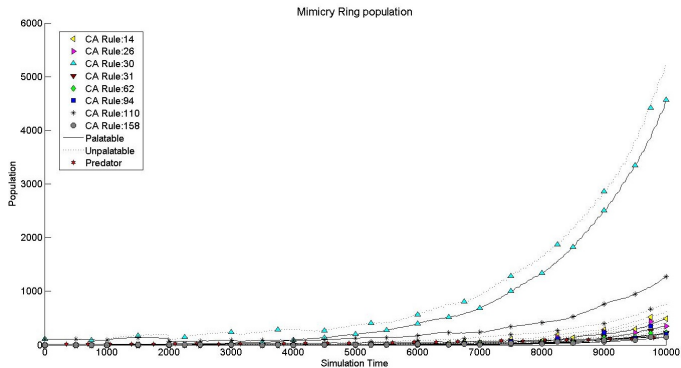
|                      | Prey configuration   |   |     | Predator configuration |    |
|----------------------|----------------------|---|-----|------------------------|----|
| Population           | Rule110 (Palatable)  |  | 108 | 10                     |    |
|                      | Rule30 (Unpalatable) |  | 108 |                        |    |
| Reproduction         | Age Limit            | 100   |     | 500                    |    |
|                      | Interval             | 1000  |     | 1200                   |    |
| Mutation Rate        | Pattern              | 0.05  |     | 0.3                    |    |
|                      | Genome               | 0.5   |     |                        |    |
| Demise Age           | 2000                 |   |     | 2500                   |    |
| Minimum Attack Age   |                      |   |     | 500                    |    |
| Memory Configuration |                      |   |     | Minimum                | 2  |
|                      |                      |   |     | Maximum                | 10 |

Table: Agent configuration of 2 prey species

# Two Prey Species

Population vs. Time (10k)



**Figure:** Population distribution of mimicry rings, initialized with 2 prey species, 10k iterations

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# Only Unpalatable Species

## Initial Configuration

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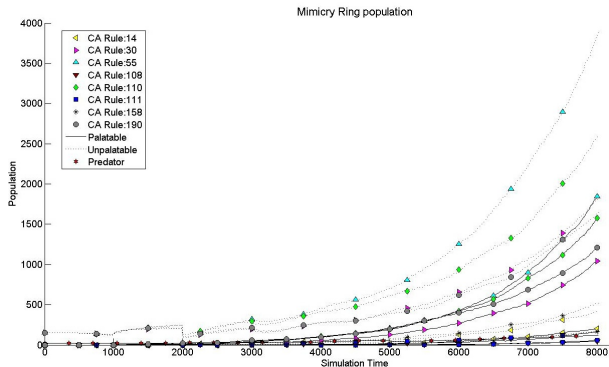
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|                      | Prey configuration    |   |     | Predator configuration |     |
|----------------------|-----------------------|---|-----|------------------------|-----|
| Population           | Rule110 (Unpalatable) |  | 150 | 20 ↓                   |     |
|                      | Rule30 (Unpalatable)  |  | 150 |                        |     |
|                      | Rule55 (Unpalatable)  |  | 150 |                        |     |
|                      | Rule190 (Unpalatable) |  | 150 |                        |     |
| Reproduction         | Age Limit             | 100   |     | 500                    |     |
|                      | Interval              | 1000  |     | 2000                   |     |
| Mutation Rate        | Pattern               | 0.05  |     | 0.3                    |     |
|                      | Genome                | 0.5   |     |                        |     |
| Demise Age           | 2000                  |   |     | 5000 ↓                 |     |
| Minimum Attack Age   |                       |   |     | 500                    |     |
| Memory Configuration |                       |   |     | Minimum                | 4 ↓ |
|                      |                       |   |     | Maximum                | 10  |

**Table:** Agent configuration of 4 prey species all unpalatable.

# Only Unpalatable Species

Population vs. Time (10k)



**Figure:** Population distribution of mimicry rings(4 prey species all unpalatable)

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# Only Unpalatable Species

Reduced Predator Memory

Population vs. Time (10k)

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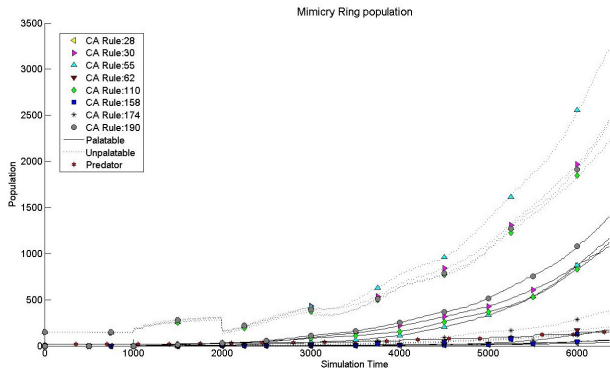
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**Figure:** Population distribution of mimicry rings. 4 prey, all unpalatable but reduced predator memory

# Analysis

## Batesian Mimicry

- ▶ Batesian Mimicry has taken effect, for all possible initial conditions.
  - ▶ Every ring of unpalatable species there is a palatable ring.
- ▶ Start with palatable population, prey reaches extinction.  
**Reason:** No models to mimic for palatable species.
- ▶ **Conclusion:** This model can simulate evolution of Batesian Mimicry.

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## Mullerian Mimicry

*“Mullerian mimics converge into one large ring.”*

- ▶ Initialize simulation with 4 unpalatable species. No palatable ones.
- ▶ After 10k iteration all unpalatable species survive with dominance.
- ▶ **Reason:** Predator minimum memory configuration set to 4.

### New experiment:

- ▶ Reduce predator memory to 1.
- ▶ **Observation:** Single large ring do not occur.
- ▶ **Conclusion:** Similar to Franks and Noble.  
Multiple Mullerian mimics do not converge into one large ring.

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- ▶ Successful simulation of evolution of mimicry.
- ▶ Accurate simulation of mimicry ring.  
Diverse new rings and shift in their population.
- ▶ Proof of the theory of Turner: evolution of mimicry with punctuated equilibrium.

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# Conclusion

## Artificial Life:

- ▶ Tool for biological inquiry
  - ▶ Success: Proof of Turner's punctuated equilibrium
  - ▶ Proof of Franks and Noble's converge of one large ring.
- ▶ Nature inspired computer science
  - ▶ Success: Appropriate emulation of Batesian and Mullerian mimicry.
- ▶ Solve problem in computer science
  - ▶ Not successful: unable to find the appropriate problem solving scenario.