



Computer Sciences University of Technology



Date: 17/9/2017

Time. 3 hours

Lecturers, Akbas E., Ahmed E. & Amar F.

Final Exam. 2016–2017 second trail

Subject_discreet mathematic

Class.first

Branch . all

Note: Answer 5 questions only, 14 marks for each

Q1) Prove by induction for $n \ge 1$:

$$1+4+7+....+(3n-2)=1/2 n (3n-1)$$

- Q2) Sketch the graph of f: $R \rightarrow R$ where: $f(x) = x^3 + x^2 + 2$. Determine if f(x) is: (a) function (b) onto, (c) one-to-one, (d) invertible? (Mention the reasons)
- Q3) Suppose that a person deposits 20,000 ID in a savings account at a bank yielding 13% per year with interest compounded annually. How much will be in the account after 38 years?
- Q4) In a group of 30 people:
 - 15 run (R),
 - 13 swim (S),
 - 13 cycle (C).
 - 5 run and swim,
 - 8 cycle and swim,
- 9 run and cycle,
 - 5 do all three activities.
 - a) How many of the 30 people do not do any of these activities?
 - b) Fill in the correct number of activities in each of the eight regions of the Venn diagram.
- Q5) Let $U = \{1, 2, ..., 9\}$ be the universal set,

and let
$$A = \{1, 2, 3, 4, 5\},\$$

$$B = \{4, 5, 6, 7\},\$$

$$C = \{5, 6, 7, 8, 9\},\$$

$$D = \{1, 3, 5, 7, 9\}$$
, Find:

- (a) A^{c} , B^{c} ,
- (b) A\B, B\A,
- (c) C\D, D\C;
- (d) A ⊕ B, C ⊕ D.
- $(f) D \cup C$

(e) $A \cap C$

- (-) -
- Q6) Consider the following relations on the set $A = \{1, 2, 3\}$:

$$R = \{(1, 1), (1, 2), (1, 3), (3, 3)\},\$$

$$S = \{(1, 1)(1, 2), (2, 1)(2, 2), (3, 3)\},\$$

$$A \times A = universal relation$$

Determine whether or not each of the above relations on A is:

(a) reflexive; (b) compatible; (c) transitive; (d) antisymmetric.

د اواس عرالین

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