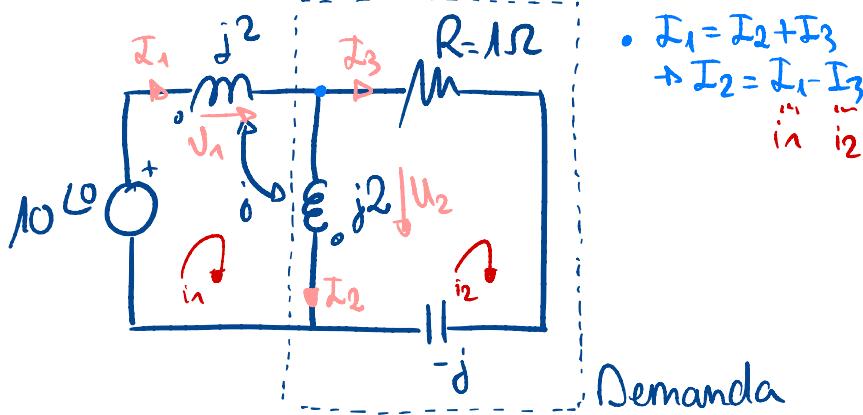


Robina tensión intensidad
mismo sentido

$$\begin{aligned} m1) (2j+2j-2j) I_1 + (-2j+j) I_3 &= 10 \\ m2) (-2j+j) I_1 + 2j I_3 + (1-j) I_3 &= 0 \end{aligned}$$

Problema 1



$$\begin{aligned} I_1 &= I_2 + I_3 \\ \rightarrow I_2 &= I_1 - I_3 \end{aligned}$$

Poniendo mismo sentido tensión e intensidad

$$U_1 = j2 I_1 - j I_2$$

$$U_2 = j2 I_2 - j I_1$$

$$\left. \begin{aligned} \text{in } 10^{\circ} &= U_1 + U_2 = j2 I_1 - j I_2 + j2 I_2 - j I_1 = j I_1 + j I_2 \\ &\quad I_2 = I_1 - I_3 \end{aligned} \right\} 10^{\circ} = j I_1 + j (I_1 - I_3) \rightarrow$$

$$\rightarrow 10^{\circ} = j2 I_1 - j I_3$$

$$\left. \begin{aligned} \text{in } 0 &= (1-j) I_3 - U_2 = (1-j) I_3 - (j2 I_2 - j I_1) \\ &\quad I_2 = I_1 - I_3 \end{aligned} \right\} 0 = (1-j) I_3 - j2 (I_1 - I_3) + j I_1 \rightarrow$$

$$\rightarrow 0 = I_3 - j I_3 - j2 I_1 + j2 I_3 + j I_1 = -j I_1 + (1+j) I_3$$

$$\left. \begin{aligned} \text{in } I_1 &= \frac{\begin{vmatrix} 10^{\circ} & -j \\ 0 & 1+j \end{vmatrix}}{\begin{vmatrix} j2 & -j \\ -j & 1+j \end{vmatrix}} = \frac{10^{\circ}(1+j)}{j2(1+j)+1} = \frac{10(1+j)}{j^2-1} = \frac{10(1+j)(-1-j2)}{(-1+j2)(-1-j2)} = \\ &= \frac{10(-1-j2-j+2)}{1+4} = \frac{10(1-j3)}{5} = 2(1-j3) \end{aligned} \right.$$

$$\left. \begin{aligned} \text{in } I_3 &= \frac{\begin{vmatrix} j2 & 10^{\circ} \\ -j & 0 \end{vmatrix}}{\begin{vmatrix} j2 & -j \\ -j & 1+j \end{vmatrix}} = \frac{10^{\circ} j}{j2(1+j)+1} = \frac{10 j}{j^2-1} = \frac{j10}{(-1+j2)(-1-j2)} = \\ &= \frac{10(2-j)}{1+4} = \frac{10(2-j)}{5} = 2(2-j) \end{aligned} \right.$$

a) P,Q generada o consumida en la demanda

b) P,Q generada o consumida en la fuente

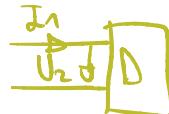
c) Analizar resultados

d) P,Q generada o consumida por todos los elementos

$$I_2 = I_1 - I_3 = 2(1-j3) - 2(2-j) = 2(-1+j2) = -2(1+j2)$$

a) P,Q generada o consumida en la demanda

$$U_2 = j2I_2 - jI_1 = j2(-2(1+j2)) - j(2(1-j3)) = j2(-2-j4-1+j3) = j2(-3-j) = \\ = 2(-j3+1) = 2(1-j3)$$



Por lo que la potencia en Demanda es:

$$S_{\text{dem}} = U_2 \cdot I_1^* = 2(1-j3) \cdot 2(1+j3) = 4(1+9) = 40 \text{ VA} \quad \begin{matrix} \rightarrow P=40 \text{ W} \\ \downarrow Q=0 \text{ VAr} \end{matrix}$$

Consumo potencia activa (40W) y no consume ni genera reactiva

b) P,Q generada o consumida en la fuente

$$S_g = 10 \cdot I_1^* = 10 \cdot 2(1+j3) = 20(1+j3) = 20 + j60 \text{ VA} \quad \begin{matrix} \rightarrow P=20 \text{ W} \\ \leftarrow Q=60 \text{ VAr} \end{matrix}$$

Genera potencia activa (20W) y reactiva (60VAr)

c) Analizar resultados

La fuente genera 20W, sin embargo, en demanda, se consumen 40W

d) P,Q generada o consumida por todos los elementos

$$I_3 = 2(2-j) = 4-j2 = \sqrt{4^2+2^2} = \sqrt{16+4} = \sqrt{20} = 2\sqrt{5}$$

$$P_R = R \cdot I_3^2 = 1 \cdot (2\sqrt{5})^2 = 4 \cdot 5 = 20 \text{ W}$$

$$Q_c = Z_L I_3^2 = -1 (2\sqrt{5})^2 = -4 \cdot 5 = -20 \text{ VAr}$$

Comprobamos

$$S_{\text{dem},I_2} = U_2 I_2^* = 2(1-j3)(-2(1-j2)) = -4(1-j2-j3-6) = -4(-5-j5) = 20(1-j) \\ = 20 - j20 \text{ VA} \quad \begin{matrix} \rightarrow P=20 \text{ W} \\ \downarrow Q=-20 \text{ VAr} \end{matrix}$$

$$U_n = j2 I_1 - j I_2 = j2 \cdot 2(1-j3) + j2(1+j2) = 2(j2+6+j-2) = 2(4+j3)$$

$$\begin{aligned} S_{\text{dem},L_1} &= U_n I_1^* = 2(4+j3) \cdot 2(1+j3) = 4(4+j12+j3-9) = 4(-5+j15) = 20(-1+j3) = \\ &= -20 + j60 \text{ VA} \quad \begin{matrix} P = -20 \text{ W} \\ Q = 60 \text{ VAr} \end{matrix} \end{aligned}$$

Comparando -

$$S_{\text{dem},L_1} = -20 \text{ W} + 60 \text{ VAr}$$

$$S_{\text{dem},L_2} = \begin{cases} 20 \text{ W}, & \\ -20 \text{ VAr} & \end{cases}$$

Entonces, tenemos:

Saliente

$$S_g = 20 + j60 \text{ VA}$$

Entrante

$$S_{\text{dem},L_2} = 20 + j20 \text{ VA}$$

$$S_{\text{dem},L_1} = -20 + j60 \text{ VA}$$

$$S_R = 20 \text{ W}$$

$$S_C = -j20 \text{ VAr}$$

Por lo tanto

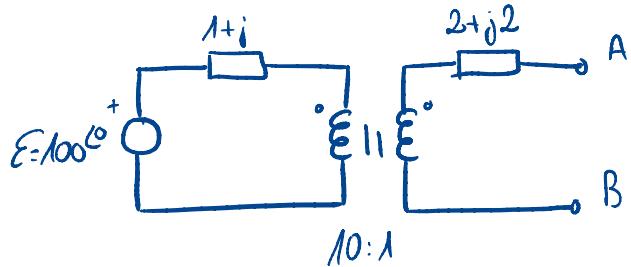
Potencia activa:

- Se generan 20 W en la fuente
- Se transfieren 20 W de la bobina 1 a la 2. (en el conjunto, la potencia activa es 0 W)
- Se consumen 20 W en la resistencia

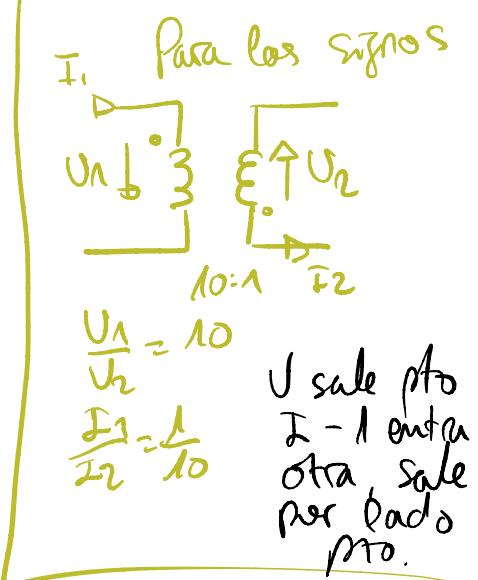
Potencia reactiva:

- Se generan 60 VAr en la fuente y 20 VAr en el condensador
- Se consumen 60 VAr en la bobina 1 y 20 VAr en la bobina 2

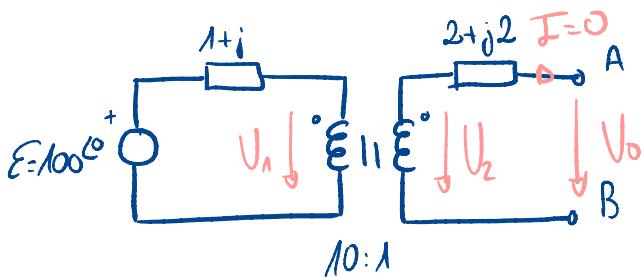
Problema 2



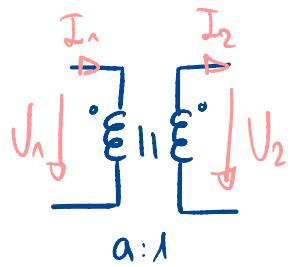
Thevenin
Norton



Tensión a circuito abierto



Sabiendo que:



- Tensiones transformador

$$\frac{U_1}{U_2} = a$$

- Potencias transformador

$$U_1 I_1^* = U_2 I_2^*$$

$$\frac{U_1}{U_2} = \frac{I_2^*}{I_1^*} = a \Rightarrow$$

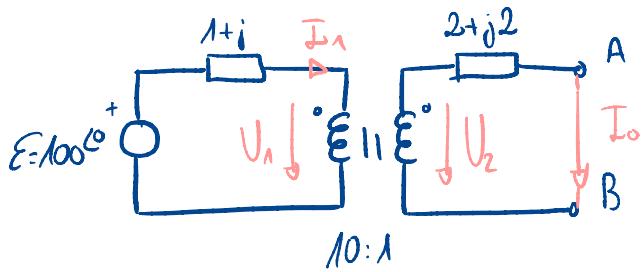
$$\Rightarrow \frac{I_1}{I_2} = \left(\frac{1}{a}\right)^*$$

Podemos concluir:

$$I_2 = 0 \rightarrow I_1 = 0$$

$$U_1 = E = 100^\circ \text{ V} \rightarrow U_2 = \frac{U_1}{a} = \frac{100^\circ}{10} = 10^\circ \text{ V} \rightarrow U_0 = 10^\circ \text{ V}$$

Intensidad de cortocircuito



$$E = (1+j)I_1 + U_1 \rightarrow 100^\circ = (1+j)I_1 + U_1 \rightarrow U_1 = 100^\circ - (1+j)I_1$$

$$U_1 = 10U_2 \rightarrow U_2 = \frac{U_1}{10} = \frac{100^\circ - (1+j)I_1}{10} \quad \left. \begin{array}{l} \\ \end{array} \right\} I_o(2+j2) = \frac{100^\circ - (1+j)I_1}{10}$$

$$U_2 = I_o(2+j2)$$

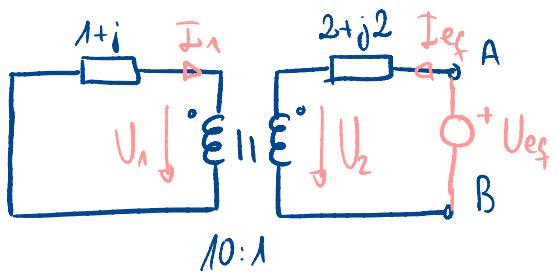
$$\frac{I_1}{I_o} = \left(\frac{1}{10}\right)^* \rightarrow \frac{I_1}{I_o} = \left(\frac{1}{10}\right)^* = \frac{1}{10} \rightarrow I_1 = \frac{I_o}{10}$$

$$\rightarrow I_o(2+j2) = \frac{100^\circ - (1+j)\frac{I_o}{10}}{10} \rightarrow 100I_o(2+j2) = 1000 - (1+j)I_o \rightarrow$$

$$\rightarrow 201(1+j)I_o = 1000 \rightarrow I_o = \frac{1000}{201(1+j)} = \frac{1000(1-j)}{201(1+j)(1-j)} = \frac{1000(1-j)}{201(1+1)} = \frac{500(1-j)}{201}$$

Impedancia equivalente

$$Z_{eq} = \frac{U_o}{I_o} = \frac{\frac{10}{500(1-j)}}{\frac{201}{500(1-j)}} = \frac{201}{50(1-j)} = \frac{201(1+j)}{50(1-j)(1+j)} = \frac{201(1+j)}{100}$$



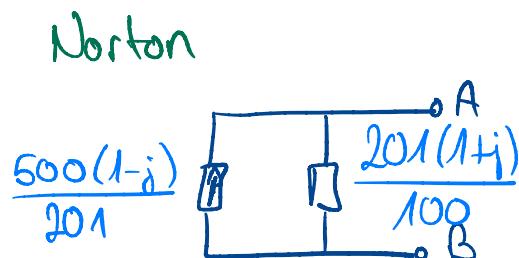
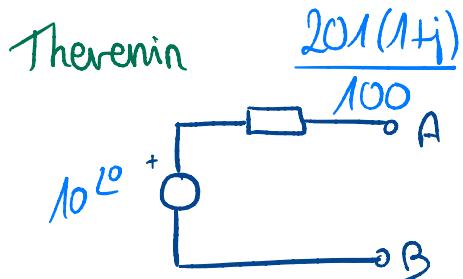
$$\left. \begin{aligned} 0 &= (1+j)I_1 + U_1 \Rightarrow U_1 = -(1+j)I_1 \\ U_1 &= 10U_2 \end{aligned} \right\} \left. \begin{aligned} 10U_2 &= -(1+j)I_1 \Rightarrow U_2 = \frac{-(1+j)I_1}{10} \end{aligned} \right\}$$

$$U_{eq} = I_{eq}(2+j2) + U_2$$

$$\rightarrow U_{eq} = I_{eq}(2+j2) - \frac{(1+j)I_1}{10}$$

$$\left. \begin{aligned} \frac{I_1}{-I_{eq}} &= \left(\frac{1}{10}\right)^* \Rightarrow \frac{I_1}{-I_{eq}} = \left(\frac{1}{10}\right)^* = \frac{1}{10} \Rightarrow I_1 = \frac{-I_{eq}}{10} \end{aligned} \right\}$$

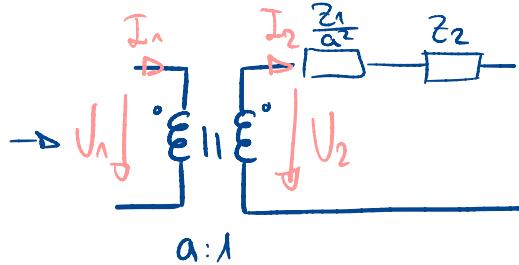
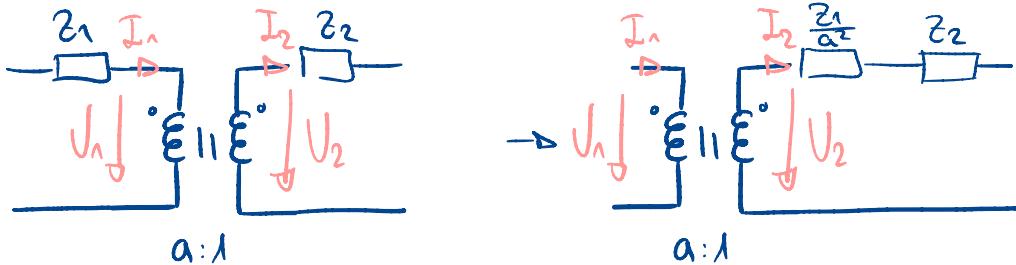
$$U_{eq} = I_{eq}(2+j2) + \frac{(1+j)I_{eq}}{100} \xrightarrow{I_{eq}} \frac{U_{eq}}{I_{eq}} = \frac{200(1+j) + (1+j)}{100} = \frac{201(1+j)}{100}$$



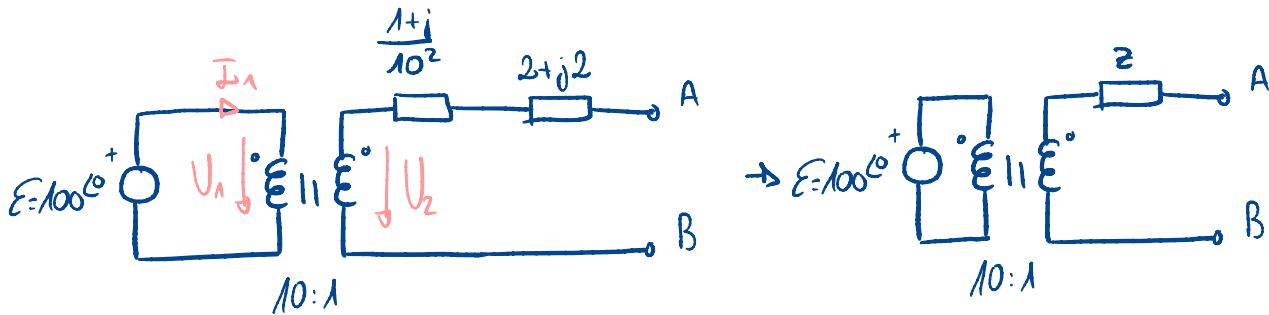
Usa que

$$\left. \begin{array}{l} U_1 I_1^* = U_2 I_2^* \\ U = IR \end{array} \right\} I_1^2 R_1 = I_2^2 R_2 \rightarrow \frac{I_1^2}{I_2^2} = \frac{R_2}{R_1}$$

$$\left. \begin{array}{l} \frac{I_1}{I_2} = \left(\frac{1}{a}\right)^* \\ \frac{R_2}{R_1} = \left(\frac{1}{a}\right)^2 \end{array} \right\} R_2 = \frac{R_1}{a^2}$$

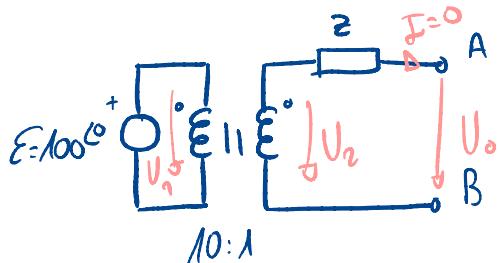


Entonces, tenemos:



$$Z = \frac{1+j}{10^2} + 2+j2 = \frac{1+j + 200(1+j)}{100} = \frac{201(1+j)}{100}$$

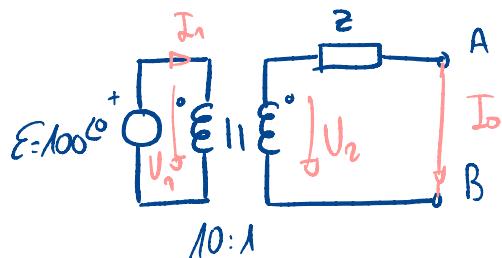
Tensión a circuito abierto:



$$\left. \begin{array}{l} E = U_1 \\ U_1 = 10U_2 \\ U_2 = U_o \end{array} \right\} U_o = \frac{E}{10} = 10 \angle 0^\circ$$

Corriente de cortocircuito:

$$U_o = I_o R_{eq} \rightarrow I_o = \frac{U_o}{R_{eq}} = \frac{10^{\circ}}{\frac{20\Omega(1+j)}{100}} = \frac{500(1-j)}{20\Omega}$$



$$\left. \begin{array}{l} E = U_1 \\ U_1 = 10U_2 \\ U_2 = E/Z \end{array} \right\} E = 10I_o Z \rightarrow I_o = \frac{E}{10Z} = \frac{100^{\circ}}{10 \frac{20\Omega(1+j)}{100}} = \frac{500(1-j)}{20\Omega}$$