# Security Protocols and Verification

Design and Analysis of Cryptographic Protocols

Garance Frolla Ely Marthouret Ewan Decima

Team: ASKO OM8464A2

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### 1 Initial Knowledge

At the beginning of the protocol, agents A and B are assumed to know all public keys, especially each other's. Both A and B also know their respective symmetric keys ( $K_{AS}$  and  $K_{BS}$ ) shared with an honest server S and there clocks are synchronised on the S one. Furthermore, each participant is aware of the chosen protocol and the following specifications.

# 2 Ely the big frog

- 1.  $A \rightarrow B : \{|\langle A, N_A \rangle|\}_{K_{AB}}$
- 2.  $A \to S : \{ |\langle B, \tau, \lambda, K_{AB} \rangle | \}_{K_{AS}}$
- 3.  $S \to B : \{ |\langle A, \tau, \lambda, K_{AB} \rangle| \}_{K_{BS}}$
- 4.  $B \to A : \{|N_A + 1|\}_{K_{AB}}$

## 3 Protocol Description

### 3.1 Messages cost and description

This protocol begins with entity A generating a nonce, denoted as  $N_A$ . A then encrypts her identity together with the nonce using the freshly generated session key  $K_{AB}$ . The transmitted data is structured as follows:  $\{|\langle A, N_A \rangle|\}_{K_{AB}}$ . This message costs **63**.

After sending the first message, A sends to the honest and trusted server S, using the shared key  $K_{AS}$ , the identity of B, a timestamp  $\tau$ , a lifetime period  $\lambda$  to confirm the key and the session key  $K_{AB}$ . The transmitted data is structured as follows:  $\{|\langle B, \tau, \lambda, K_{AB} \rangle|\}_{K_{AS}}$ . This message costs **166**.

First, S checks whether  $t \geq \tau + \lambda$ , where t denotes the time at which S receives the message from A. If this condition holds, S aborts. Otherwise, using the shared key  $K_{BS}$ , S sends to B essentially the same message as before, except that A is replaced with B. The transmitted data is structured as follows:  $\{|\langle A, \tau, \lambda, K_{AB} \rangle|\}_{K_{BS}}$ . This message costs: **166**.

B receives the message  $\{|\langle A, \tau, \lambda, K_{AB} \rangle|\}_{K_{BS}}$  and obtains the session key  $K_{AB}$ . He also learns the validity period  $\lambda$ , starting from time  $\tau$ , during which A will accept his response. This measure provides protection against ticket theft. Indeed, even if an attacker manages to intercept a ticket, they will not be able to use it after its expiration. When B receives this message at time t, if  $t \geq \tau + \lambda$ , then B aborts.

Otherwise, B respond to the first message of A, he can decrypt  $\{|\langle A, N_A \rangle|\}_{K_{AB}}$  with the session key. Key confirmation lies in the fact that B sends back  $N_A + 1$  to A. In this way, A knows that B has successfully retrieved the key. This allows combining key confirmation with the challenge–response mechanism for the authentication of B with respect to A. The transmitted data is structured as follows:  $\{|N_A + 1|\}_{K_{AB}}$ . This message costs  $\mathbf{12}$ .

At the end, when A receives the last message from B at time t, she checks whether  $t \geq \tau + \lambda$ . If this condition holds, A rejects the message and aborts. Otherwise, the key exchange protocol succeeds.

The total cost is: 409.

#### 3.2 Value Generated

- $N_A$  is a nonce generated by A.
- $K_{AB}$  is a perfectly random symmetric key generated by A.
- $\tau$  is a timestamp generated by A based on the clock synchronized by S.
- $\lambda$  is a duration generated by A, small enough to be secure but long enough to establish a communication.

#### 3.3 Security Properties

In addition to the security properties specified in the project description, we have:

• Freshness:  $K_{AB}$  is freshly generated by A, independently of B and of the current time. Each new session results in a newly generated key  $K_{AB}$ .

- Authentification: When B receives the first message  $\{|\langle A, N_A \rangle|\}_{K_{AB}}$ , he can't be sure that A sends it to him. But after receiving  $\{|\langle A, \tau, \lambda, K_{AB} \rangle|\}_{K_{BS}}$  from S he can be sure of the origin of the first message. Indeed, A uses S to authenticate to B. Since the message containing A's identity is encrypted with  $K_{BS}$ , B can be sure that A initiated the conversation.
- Key confirmation: After receiving the third message, B obtains the session key  $K_{AB}$  from S. To confirm possession of this key, B sends back to A the value  $N_A + 1$ , encrypted under  $K_{AB}$ . This proves to A that B has indeed obtained the correct key.
- Secrecy: Nobody except for agents A and B know the session key  $K_{AB}$ . Indeed, all messages transmitted over the network are encrypted using symmetric encryption.
- Integrity: Each message is encrypted with a symmetric key, ensuring that only an entity possessing the corresponding key  $(K_{AB}, K_{AS}, \text{ or } K_{BS})$  can modify its contents.