Scheme

The `define` form is used to assign values to symbols. It has the following syntax:

```
(define <symbol> <expression>)
```

```
scm> (define pi (+ 3 0.14))
pi
scm> pi
3.14
```

To evaluate the `define` expression:

1. Evaluate the final sub-expression (`<expression>`), which in this case evaluates to `3.14`.
2. Bind that value to the symbol (`symbol`), which in this case is `pi`.
3. Return the symbol.

The `define` form can also define new procedures, described in the "Defining Functions" section. The `define` form can create a procedure and give it a name:

```
(define (<symbol> <param1> <param2> ...) <body>)
```

For example, this is how we would define the `double` procedure:

```
scm> (define (double x) (* x 2))
double
scm> (double 3)
6
```

Here's an example with three arguments:

```
scm> (define (add-then-mul x y z)
        (* (+ x y) z))
scm> (add-then-mul 3 4 5)
35
```

When a `define` expression is evaluated, the following occurs: 1. Create a procedure with the given parameters and `<body>`. 2. Bind the procedure to the `<symbol>` in the current frame. 3. Return the `<symbol>`.

The following two expressions are equivalent:

```
scm> (define add (lambda (x y) (+ x y)))
add
scm> (define (add x y) (+ x y))
add
```

Atomic expressions (also called *atoms*) are expressions without sub-expressions, such as numbers, boolean values, and symbols.

```
scm> 1234     ; integer
1234
scm> 123.4    ; real number
123.4
scm> #f       ; the Scheme equivalent of False in Python
#f
```

A Scheme *symbol* is equivalent to a Python name. A symbol evaluates to the value bound to that symbol in the current environment. (They are called symbols rather than names because they include + and other arithmetic symbols.)

```
scm> quotient        ; A symbol bound to a built-in procedure
#[quotient]
scm> +               ; A symbol bound to a built-in procedure
#[+]
```

In Scheme, *all* values except #f (equivalent to False in Python) are true values (unlike Python, which has other false values, such as 0).

```
scm> #t
#t
scm> #f
#f
```

The if special form evaluates one of two expressions based on a predicate.

```
(if <predicate> <if-true> <if-false>)
```

The rules for evaluating an if special form expression are as follows:

1. Evaluate the <predicate>.
2. If the <predicate> evaluates to a true value (anything but #f), evaluate and return the value of the <if-true> expression. Otherwise, evaluate and return the value of the <if-false> expression.

For example, this expression does not error and evaluates to 5, even though the sub-expression `(/ 1 (- x 3))` would error if evaluated.

```
scm> (define x 3)
x
scm> (if (> (- x 3) 0) (/ 1 (- x 3)) (+ x 2))
5
```

The `<if-false>` expression is optional.

```
scm> (if (= x 3) (print x))
3
```

Let's compare a Scheme `if` expression with a Python `if` statement:

- In Scheme:

```
    (if (> x 3) 1 2)
```

- In Python:

```
    if x > 3:
        1
    else:
        2
```

The Scheme `if` expression evaluates to a number (either 1 or 2, depending on `x`). The Python statement does not evaluate to anything, and so the 1 and 2 cannot be used or accessed.

Another difference between the two is that it's possible to add more lines of code into the suites of the Python `if` statement, while a Scheme `if` expression expects just a single expression in each of the `<if-true>` and `<if-false>` positions.

One final difference is that in Scheme, you cannot write `elif` clauses.

Q1: Perfect Fit

Definition: A perfect square is `k*k` for some integer `k`.

Implement `fit`, which takes non-negative integers `total` and `n`. It returns whether there are **n different** positive perfect squares that sum to `total`.

Important: Don't use the Scheme interpreter to tell you whether you've implemented it correctly. Discuss! On the final exam, you won't have an interpreter.

```
    ; Return whether there are n perfect squares with no repeats that sum to total

    (define (fit total n)
        (define (f total n k)
            (if (and (= n 0) (= total 0))
                #t
            (if (< total (* k k))
                #f
            'YOUR-CODE-HERE



            )))
        (f total n 1))

    (expect (fit 10 2) #t)  ; 1*1 + 3*3
    (expect (fit 9 1)  #t)  ; 3*3
    (expect (fit 9 2)  #f)  ;
    (expect (fit 9 3)  #f)  ; 1*1 + 2*2 + 2*2 doesn't count because of repeated 2*2
    (expect (fit 25 1)  #t) ; 5*5
    (expect (fit 25 2)  #t) ; 3*3 + 4*4
```

Use the (or _ _) special form to combine two recursive calls: one that uses k*k in the sum and one that does not. The first should subtract k*k from total and subtract 1 from n; the other should leaves total and n unchanged.

Q2: Interleave

Implement the function `interleave`, which takes two lists `lst1` and `lst2` as arguments. `interleave` should return a list that interleaves the elements of the two lists. (In other words, the resulting list should contain elements alternating between `lst1` and `lst2`, starting at `lst1`).

If one of the input lists to `interleave` is shorter than the other, then `interleave` should alternate elements from both lists until one list has no more elements, and then the remaining elements from the longer list should be added to the end of the new list. If `lst1` is empty, you may simply return `lst2` and vice versa.

```scheme
(define (interleave lst1 lst2)
'YOUR-CODE-HERE




















)
```

Scheme Lists & Quotation

> As you read through this section, it may be difficult to understand the differences between the various representations of Scheme containers. We recommend that you use our online Scheme interpreter to see the box-and-pointer diagrams of pairs and lists that you're having a hard time visualizing! (Use the command (autodraw) to toggle the automatic drawing of diagrams.)

Lists

Scheme lists are very similar to the linked lists we've been working with in Python. Just like how a linked list is constructed of a series of Link objects, a Scheme list is constructed with a series of pairs, which are created with the constructor cons.

Scheme lists require that the cdr is either another list or nil, an empty list. A list is displayed in the interpreter as a sequence of values (similar to the __str__ representation of a Link object). For example,

```
scm> (cons 1 (cons 2 (cons 3 nil)))
(1 2 3)
```

Here, we've ensured that the second argument of each cons expression is another cons expression or nil.
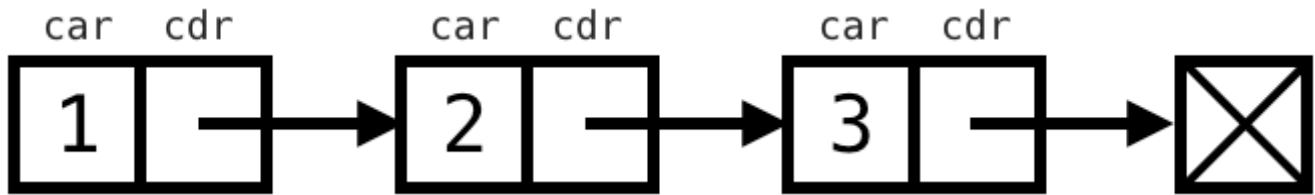
list

We can retrieve values from our list with the car and cdr procedures, which now work similarly to the Python Link's first and rest attributes. (Curious about where these weird names come from? Check out their etymology.)

```
scm> (define a (cons 1 (cons 2 (cons 3 nil))))  ; Assign the list to the name a
a
scm> a
(1 2 3)
scm> (car a)
1
scm> (cdr a)
(2 3)
scm> (car (cdr (cdr a)))
3
```

If you do not pass in a pair or nil as the second argument to cons, it will error:

```
scm> (cons 1 2)
Error
```

list Procedure

There are a few other ways to create lists. The list procedure takes in an arbitrary number of arguments and constructs a list with the values of these arguments:

```
scm> (list 1 2 3)
(1 2 3)
scm> (list 1 (list 2 3) 4)
(1 (2 3) 4)
scm> (list (cons 1 (cons 2 nil)) 3 4)
((1 2) 3 4)
```

Note that all of the operands in this expression are evaluated before being put into the resulting list.

Quote Form

We can also use the quote form to create a list, which will construct the exact list that is given. Unlike with the list procedure, the argument to ' is *not* evaluated.

```
scm> '(1 2 3)
(1 2 3)
scm> '(cons 1 2)           ; Argument to quote is not evaluated
(cons 1 2)
scm> '(1 (2 3 4))
(1 (2 3 4))
```

Built-In Procedures for Lists

There are a few other built-in procedures in Scheme that are used for lists. Try them out in the interpreter!

```
scm> (null? nil)                  ; Checks if a value is the empty list
True
scm> (append '(1 2 3) '(4 5 6)) ; Concatenates two lists
(1 2 3 4 5 6)
scm> (length '(1 2 3 4 5))       ; Returns the number of elements in a list
5
```

Q3: Nested Lists

Create the nested list depicted below three different ways: using `list`, `quote`, and `cons`.
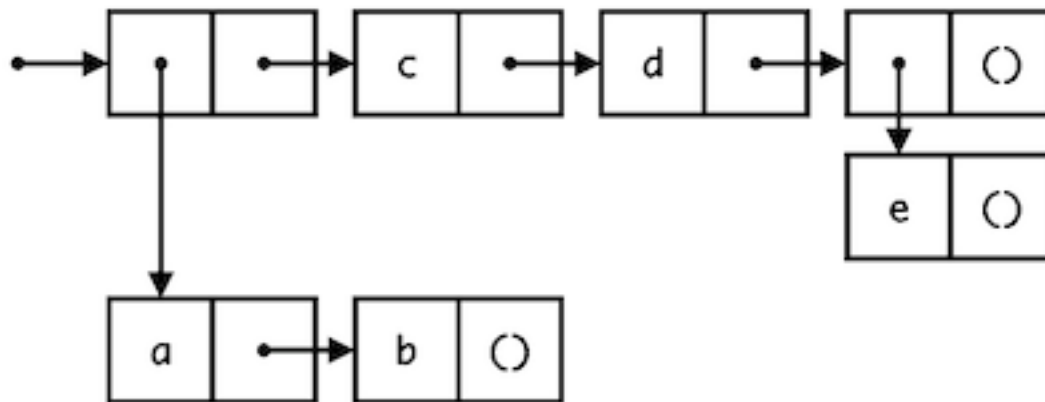
First, describe the list together: "It looks like there are four elements, and the first element is …" If you get stuck, look at the hint below. (But try to describe it yourself first!)

A four-element list in which the first element is a list containing both `a` and `b`, the second element is `c`, the third element is `d`, and the fourth element is a list containing just `e`.

Next, use calls to `list` to construct this list. If you run this code and then (`draw with-list`) in code.cs61a.org, the `draw` procedure will draw what you've built.

```
    (define with-list
        (list
            'YOUR-CODE-HERE


        )
    )
    ; (draw with-list)   ; Uncomment this line to draw with-list
```

Every call to list creates a list, and there are three different lists in this diagram: a list containing `a` and `b`: (`list 'a 'b`), a list containing `e`: (`list 'e`), and the whole list of four elements: (`list _ 'c 'd _`). Try to put these expressions together.

Now, use `quote` to construct this list.

```
    (define with-quote
        '(
            'YOUR-CODE-HERE


        )

    )
    ; (draw with-quote)  ; Uncomment this line to draw with-quote
```

One quoted expression is enough, but it needs to match the structure of the linked list using Scheme notation. So, your task is to figure out how this list would be displayed in Scheme.

The nested list drawn above is a four-element list with lists as its first and last elements: `((a b) c d (e))`. Quoting that expression will create the list.

Now, use `cons` to construct this list. Don't use `list`. You can use `first` in your answer.

```
(define first
    (cons 'a (cons 'b nil)))
```

```
    (define with-cons
        (cons
            'YOUR-CODE-HERE


        )
    )
    ; (draw with-cons)  ; Uncomment this line to draw with-cons
```

The provided `first` is the first element of the result, so the answer takes the form:

```
first ____
```

You can either fill in the blank with a quoted three-element list:

```
'(___ ___ ___)
   c   d   (e)
```

or with nested calls to `cons`:

```
(cons ___ (cons ___ (cons ___ nil)))
       c         d         (e)
```

Q4: Pair Up

Implement `pair-up`, which takes a list `s`. It returns a list of lists that together contain all of the elements of `s` in order. Each list in the result should have 2 elements. The last one can have up to 3.

Look at the examples together to make sure everyone understands what this procedure does.

```
;;; Return a list of pairs containing the elements of s.
;;;
;;; scm> (pair-up '(3 4 5 6 7 8))
;;; ((3 4) (5 6) (7 8))
;;; scm> (pair-up '(3 4 5 6 7 8 9))
;;; ((3 4) (5 6) (7 8 9))
(define (pair-up s)
    (if (<= (length s) 3)
        'YOUR-CODE-HERE




    ))


(expect (pair-up '(3 4 5 6 7 8)) ((3 4) (5 6) (7 8)) )
(expect (pair-up '(3 4 5 6 7 8 9)) ((3 4) (5 6) (7 8 9)) )
```

`pair-up` takes a list (of numbers) and returns a list of lists, so when `(length s)` is less than or equal to 3, return a list containing the list `s`. For example, `(pair-up (list 2 3 4))` should return `((2 3 4))`.

Use `(cons _ (pair-up _))` to create the result, where the first argument to `cons` is a list with two elements: the `(car s)` and the `(car (cdr s))`. The argument to `pair-up` is everything after the first two elements.

Discussion: What's the longest list `s` for which `(pair-up (pair-up s))` will return a list with only one element? (Don't just guess and check; discuss!)

Q5: List Insert

Write a Scheme function that, when given an element, a list, and an index, inserts the element into the list at that index. You can assume that the index is in bounds for the list.

```
(define (insert element lst index)
    'YOUR-CODE-HERE




)


(expect (insert 2 '(1 7 9) 2) (1 7 2 9))


(expect (insert 'a '(b c) 0) (a b c))
```

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You're done! Excellent work this week. Please be sure to ask your section TA for the attendance form link and fill it out for credit. (one submission per person per section).