Iterators, Generators, Efficiency

Discussion 5: July 9, 2024

Iterators

An **iterable** is any value that can be iterated through, or gone through one element at a time. One construct that we've used to iterate through an iterable is a for statement:

```
for elem in iterable:
    # do something
```

In general, an **iterable** is an object on which calling the built-in **iter** function returns an *iterator*. An **iterator** is an object on which calling the built-in **next** function returns the next value.

For example, a list is an iterable value.

```
>>> s = [1, 2, 3, 4]
>>> next(s)
                  # s is iterable, but not an iterator
TypeError: 'list' object is not an iterator
>>> t = iter(s)
                  # Creates an iterator
>>> t
<list_iterator object ...>
>>> next(t)
                  # Calling next on an iterator
>>> next(t)
                  # Calling next on the same iterator
>>> next(iter(t)) # Calling iter on an iterator returns itself
>>> t2 = iter(s)
>>> next(t2)
                  # Second iterator starts at the beginning of s
>>> next(t)
                  # First iterator is unaffected by second iterator
>>> next(t)
                  # No elements left!
StopIteration
>>> s
                  # Original iterable is unaffected
[1, 2, 3, 4]
```

You can also use an iterator in a for statement because all iterators are iterable. But note that since iterators keep their state, they're only good to iterate through an iterable once:

```
>>> t = iter([4, 3, 2, 1])
>>> for e in t:
... print(e)
4
3
2
1
>>> for e in t:
... print(e)
```

There are built-in functions that return iterators.

```
>>> m = map(lambda x: x * x, [3, 4, 5])
>>> next(m)
9
>>> next(m)
16
>>> f = filter(lambda x: x > 3, [3, 4, 5])
>>> next(f)
4
>>> next(f)
5
>>> z = zip([30, 40, 50], [3, 4, 5])
>>> next(z)
(30, 3)
>>> next(z)
(40, 4)
```

Q1: WWPD: Iterators

What would Python display?

```
>>> s = "cs61a"
>>> s_iter = iter(s)
>>> next(s_iter)
```

```
>>> next(s_iter)
```

```
>>> list(s_iter)
```

```
>>> s = [[1, 2, 3, 4]]
>>> i = iter(s)
>>> j = iter(next(i))
>>> next(j)
```

```
>>> s.append(5)
>>> next(i)
```

```
>>> next(j)
```

```
>>> list(j)
```

```
>>> next(i)
```

Q2: Repeated

Implement repeated, which takes in an iterator t and an integer k greater than 1. It returns the first value in t that appears k times in a row.

Important: Call **next** on t only the minimum number of times required. Assume that there is an element of t repeated at least k times in a row.

Hint: If you are receiving a StopIteration exception, your repeated function is calling next too many times.

```
def repeated(t, k):
   """Return the first value in iterator t that appears k times in a row,
   calling next on t as few times as possible.
   >>> s = iter([10, 9, 10, 9, 9, 10, 8, 8, 8, 7])
   >>> repeated(s, 2)
   >>> t = iter([10, 9, 10, 9, 9, 10, 8, 8, 8, 7])
   >>> repeated(t, 3)
   >>> u = iter([3, 2, 2, 2, 1, 2, 1, 4, 4, 5, 5, 5])
   >>> repeated(u, 3)
   2
   >>> repeated(u, 3)
   5
   >>> v = iter([4, 1, 6, 6, 7, 7, 8, 8, 2, 2, 2, 5])
   >>> repeated(v, 3)
   2
   assert k > 1
   "*** YOUR CODE HERE ***"
```

Generators

A generator is an iterator that is returned by calling a generator function, which is a function that contains yield statements instead of return statements. The ways to use an iterator are to call next on it or to use it as an iterable (for example, in a for statement).

We can create our own custom iterators by writing a *generator function*, which returns a special type of iterator called a **generator**. Generator functions have yield statements within the body of the function instead of return statements. Calling a generator function will return a generator object and will *not* execute the body of the function.

For example, let's consider the following generator function:

```
def countdown(n):
    print("Beginning countdown!")
    while n >= 0:
        yield n
        n -= 1
    print("Blastoff!")
```

Calling countdown(k) will return a generator object that counts down from k to 0. Since generators are iterators, we can call **iter** on the resulting object, which will simply return the same object. Note that the body is not executed at this point; nothing is printed and no numbers are outputted.

```
>>> c = countdown(5)
>>> c
<generator object countdown ...>
>>> c is iter(c)
True
```

So how is the counting done? Again, since generators are iterators, we call **next** on them to get the next element! The first time **next** is called, execution begins at the first line of the function body and continues until the **yield** statement is reached. The result of evaluating the expression in the **yield** statement is returned. The following interactive session continues from the one above.

```
>>> next(c)
Beginning countdown!
5
```

Unlike functions we've seen before in this course, generator functions can remember their state. On any consecutive calls to next, execution picks up from the line after the yield statement that was previously executed. Like the first call to next, execution will continue until the next yield statement is reached. Note that because of this, Beginning countdown! doesn't get printed again.

3

The next 3 calls to next will continue to yield consecutive descending integers until 0. On the following call, a StopIteration error will be raised because there are no more values to yield (i.e. the end of the function body was reached before hitting a yield statement).

```
>>> next(c)
2
>>> next(c)
>>> next(c)
>>> next(c)
Blastoff!
StopIteration
```

Separate calls to countdown will create distinct generator objects with their own state. Usually, generators shouldn't restart. If you'd like to reset the sequence, create another generator object by calling the generator function again.

```
>>> c1, c2 = countdown(5), countdown(5)
>>> c1 is c2
False
>>> next(c1)
5
>>> next(c2)
5
```

Here is a summary of the above:

- A generator function has a yield statement and returns a generator object.
- Calling the iter function on a generator object returns the same object without modifying its current state.
- The body of a generator function is not evaluated until next is called on a resulting generator object. Calling the next function on a generator object computes and returns the next object in its sequence. If the sequence is exhausted, StopIteration is raised.
- A generator "remembers" its state for the next next call. Therefore,
 - the first **next** call works like this:
 - 1. Enter the function and run until the line with yield.
 - 2. Return the value in the yield statement, but remember the state of the function for future next calls.
 - And subsequent next calls work like this:
 - 1. Re-enter the function, start at the line after the yield statement that was previously executed, and run until the next yield statement.
 - 2. Return the value in the yield statement, but remember the state of the function for future next calls.

- Calling a generator function returns a brand new generator object (like calling iter on an iterable object).
- A generator should not restart unless it's defined that way. To start over from the first element in a generator, just call the generator function again to create a new generator.

Another useful tool for generators is the yield from statement. yield from will yield all values from an iterator or iterable.

This generator function yields all of the Fibonacci numbers.

```
def gen_fib():
    n, add = 0, 1
    while True:
        yield n
        n, add = n + add, n
```

Explain the following expression to each other so that everyone understands how it works. (It creates a list of the first 10 Fibonacci numbers.)

```
(lambda t: [next(t) for _ in range(10)])(gen_fib())
```

Then, complete the expression below by writing only names and parentheses in the blanks so that it evaluates to the smallest Fibonacci number that is larger than 2024.

```
def gen_fib():
    n, add = 0, 1
    while True:
        yield n
        n, add = n + add, n

----(____(lambda n: n > 2024, _____))
```

One solution has the form: next(___(lambda n: n > 2024, ___)) where the first blank uses a built-in function to create an iterator over just large numbers and the second blank creates an iterator over all Fibonacci numbers.

Q3: Something Different

Implement differences, a generator function that takes t, a non-empty iterator over numbers. It yields the differences between each pair of adjacent values from t. If t iterates over a positive finite number of values n, then differences should yield n-1 times.

```
def differences(t):
    """Yield the differences between adjacent values from iterator t.

>>> list(differences(iter([5, 2, -100, 103])))
    [-3, -102, 203]
    >>> next(differences(iter([39, 100])))
61
    """
    "*** YOUR CODE HERE ***"
```

Presentation Time. Explain why differences will always yield n-1 times for an iterator t over n values.

Q4: Primes Generator

Write a function primes_gen that takes a single argument n and yields all prime numbers less than or equal to n in decreasing order. Assume $n \ge 1$. You may use the is_prime function included below, which we implemented in Discussion 3.

First approach this problem using a for loop and using yield.

```
def is_prime(n):
    """Returns True if n is a prime number and False otherwise.
    >>> is_prime(2)
    True
   >>> is_prime(16)
    False
   >>> is_prime(521)
    True
    0.00
    def helper(i):
        if i > (n ** 0.5): # Could replace with i == n
            return True
        elif n % i == 0:
            return False
        return helper(i + 1)
    return helper(2)
def primes_gen(n):
    """Generates primes in decreasing order.
    >>> pg = primes_gen(7)
    >>> list(pg)
    [7, 5, 3, 2]
    0.00
    "*** YOUR CODE HERE ***"
```

Now that you've done it using a for loop and yield, try using yield from!

```
def is_prime(n):
   """Returns True if n is a prime number and False otherwise.
   >>> is_prime(2)
   True
   >>> is_prime(16)
   False
   >>> is_prime(521)
   True
   def helper(i):
      if i > (n ** 0.5): # Could replace with i == n
         return True
      elif n % i == 0:
         return False
      return helper(i + 1)
   return helper(2)
def primes_gen(n):
   """Generates primes in decreasing order.
   >>> pg = primes_gen(7)
   >>> list(pg)
   [7, 5, 3, 2]
   if _____:
      return
   if _____:
      yield _____
   yield from _____
```

Q5: Partitions

Tree-recursive generator functions have a similar structure to regular tree-recursive functions. They are useful for iterating over all possibilities. Instead of building a list of results and returning it, just yield each result.

You'll need to identify a *recursive decomposition*: how to express the answer in terms of recursive calls that are simpler. Ask yourself what will be yielded by a recursive call, then how to use those results.

Definition. For positive integers n and m, a partition of n using parts up to size m is an addition expression of positive integers up to m in non-decreasing order that sums to n.

Implement partition_gen, a generator function that takes positive n and m. It yields the partitions of n using parts up to size m as strings.

Reminder: For the partitions function we studied in lecture (video), the recursive decomposition was to enumerate all ways of partitioning n using at least one m and then to enumerate all ways with no m (only m-1 and lower).

```
def partition_gen(n, m):
    """Yield the partitions of n using parts up to size m.
    >>> for partition in sorted(partition_gen(6, 4)):
            print(partition)
    1 + 1 + 1 + 1 + 1 + 1
    1 + 1 + 1 + 1 + 2
    1 + 1 + 1 + 3
    1 + 1 + 2 + 2
    1 + 1 + 4
    1 + 2 + 3
    2 + 2 + 2
    2 + 4
    3 + 3
    assert n > 0 and m > 0
    if n == m:
        yield ____
    if n - m > 0:
        "*** YOUR CODE HERE ***"
    if m > 1:
        "*** YOUR CODE HERE ***"
```

Yield a partition with just one element, n. Make sure you yield a string.

The first recursive case uses at least one m, and so you will need to yield a string that starts with p but also includes m. The second recursive case only uses parts up to size m-1. (You can implement the second case in one line using yield from.)

Presentation Time. Explain why this implementation of partition_gen does not include base cases for n < 0, n == 0, or m == 0 even though the original implementation of partitions from lecture (video) had all three.

Efficiency

Recall that the order of growth of a function expresses how long it takes for the function to run, and is defined in terms of the function's input sizes.

For example, let's say that we have the function get_x which is defined as follows:

```
def get_x(x):
    return x
```

get x has one expression in it. That one expression takes the same amount of time to run, no matter what x is, or more importantly, how large x gets. This is called constant time.

The main two ways that a function in your program will get a running time different than just constant time is through either iteration or recursion. Let's start with some iteration examples!

The (simple) way you figure out the running time of a particular while loop is to simply count the cost of each operation in the body of the while loop, and then multiply that cost by the number of times that the loop runs. For example, look at the following method with a loop in it:

```
def foo(n):
    i, sum = 1, 0
    while i <= n:</pre>
         sum, i = sum + i, i + 1
    return sum
```

This loop has one statement in it sum, i = sum + i, i + 1. This statement is considered to run in constant time, as none of its operations rely on the size of the input. Individually, sum = sum + 1 and i = i + 1 are both constant time operations. However, when we're looking at order of growth, we take the maximum of those 2 values and use that as the running time. In 61A, we are not concerned with how long primitive functions, such as addition, multiplication, and variable assignment, take in order to run - we are mainly concerned with how many more times a loop is executed or how many more recursive calls occur as the input increases. In this example, we execute the loop n times, and for each iteration, we only execute constant time operations, so we get an order of growth of linear.

Here are a couple of basic functions, along with their running times. Try to understand why they have the given running time.

1. Constant

```
def bar(n):
    i = 0
    while i < 10:
        n = n * 2
        i += 1
    return n
```

2. Logarithmic

```
def bar(n):
   i = 1
   while n:
       i = i * 3
       n = n // 2
   return i
```

3. Linear

```
def bar(n):
    i, a, b = 1, 1, 0
    while i <= n:</pre>
        a, b, i = a + b, a, i + 1
     return a
```

4. Quadratic

```
def bar(n):
    sum = 0
    a, b = 0, 0
    while a < n:</pre>
        while b < n:</pre>
             sum += (a*b)
             b += 1
        b = 0
        a += 1
    return sum
```

5. Exponential

```
def bar(n):
   if n == 0:
       return 1
   else:
       return bar(n - 1) + bar(n - 1)
```

Q6: Bonk

Describe the order of growth of the function below.

```
def bonk(n):
    sum = 0
    while n >= 2:
        sum += n
        n = n / 2
    return sum
```

Choose one of:

- Constant
- Logarithmic
- Linear
- Quadratic
- Exponential
- None of these

Q7: Boom

What is the order of growth in time for the following function boom? Use big-notation.

```
def boom(n):
    sum = 0
    a, b = 1, 1
    while a <= n*n:
        while b <= n*n:
        sum += (a*b)
        b += 1
        b = 0
        a += 1
    return sum</pre>
```

Optional (Bonus Efficiency Problem)

This next one is significantly harder (a little beyond what you might expect to see on exams) but try it out for a fun challenge! ### Q8

This question is very challenging. This is much beyond what we expect you to know for the exam. This is here merely to challenge you.

```
def boink(n):
    if n == 1:
        return 1
    sum = 0
    i = 1
    while i < n:
        sum += boink(i)
        i += 1
    return sum</pre>
```

Submit Attendance

You're done! Excellent work this week. Please be sure to ask your section TA for the attendance form link and fill it out for credit. (one submission per person per section).