

# Lab Assignment II

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## Part 1:

### - Code for the function SUMCS:

```
function [xs] = SUMCS(t, A, omega)

%SUMCS Computes xs as the linear sum of M complex exponentials sampled at
%time points given from t, with amplitude information in A and angular
%frequency information in omega.

% t: 1×N vector that contains the time instants over which xs(t) is computed
% A: 1×M complex-valued vector. ith element is Ai
% omega: 1×M vector. ith element is  $\omega_i$ 

M = length(A);

xs = zeros(size(t));

for ii = 1:M

    xs = xs + A(ii)*exp(1j*omega(ii)*t);

end

end
```

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**- Code for Computing  $X_s$  using the function SUMCS:**

```
t = 0:0.001:1;

n = mod(21903608, 41); n=14

A = 3*rand(1,n) + 3j*rand(1,n);

omega = pi*rand(1,n);

y = SUMCS(t, A, omega);

%% Plots for Real and Imaginary Parts of  $X_s$ 

figure

subplot(1,2,1)

plot(t,real(y),'r')

grid on

title("Real Part of  $X_s$ ")

xlabel("t")

ylabel("Real( $X_s$ )")

subplot(1,2,2)

plot(t, imag(y), 'b')

grid on

title("Imaginary Part of  $X_s$ ")

xlabel("t")

ylabel("Imag( $X_s$ )")

%% Plots for Magnitude and Phase of  $X_s$ 
```

---

figure

subplot(1,2,1)

plot(t, abs(y))

title("Magnitude of  $X_s$ ")

xlabel("t")

ylabel(" $|X_s|$ ")

grid on

subplot(1,2,2)

plot(t, angle(y))

title("Phase of  $X_s$ ")

xlabel("t")

ylabel(" $\angle X_s$ ")

grid on

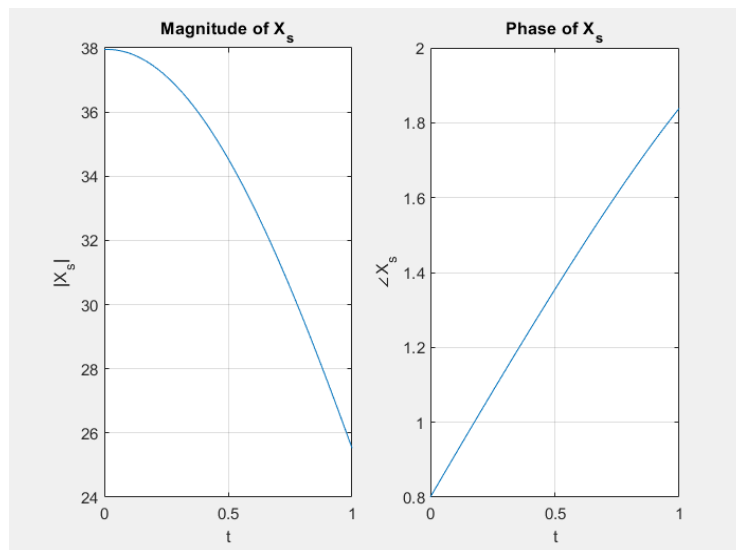


Figure 1: Magnitude And Phase of  $X_s$

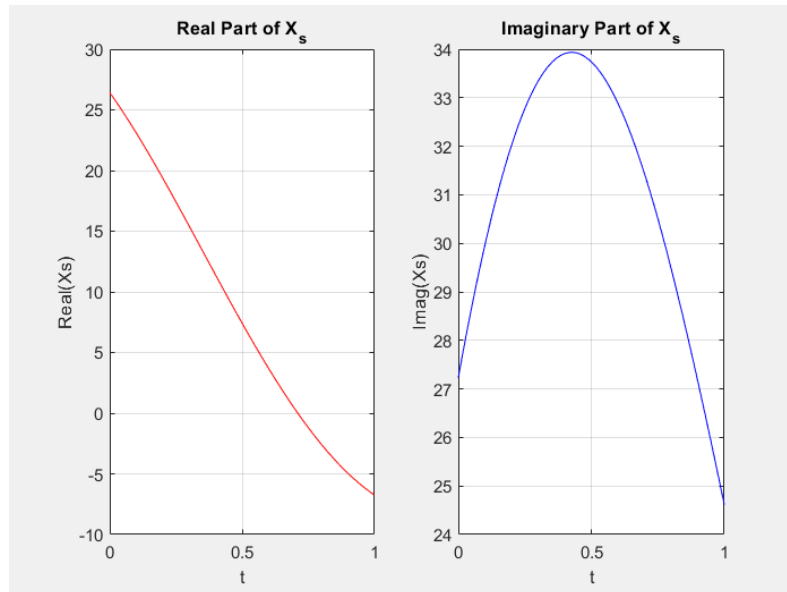


Figure 2: Real and Imaginary Parts of  $X_s$

## Part 2:

For this part, I attached a separate PDF file for graphing the function and solving the integral.

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## Part 3:

### - Code for the function FSWave:

**function [xt] = FSWave(t,K,T,W)**

%The function Xt computes the Fourier Synthesis of the function x(t).

%In other words, the function computes  $X_{\text{telda}}(t)$  i.e.

% the approximation of the fourier series over  $-1.5T < t < 1.5T$ .

% t: denotes the time grid over which  $\tilde{x}(t)$  is computed.

% xt: denotes the values of  $\tilde{x}(t)$  computed over t.

% K, T and W: denote the parameters K, T and W that appear in Eq. 4 and Eq. 5.

s = 1;

for ii = -K:K

$x_t = @(t)(1-2*t.^2).*\exp(-1i*2*pi*ii*t/T);$

$x_k(s) = (1/T)*\text{integral}(x_t,-W/2,W/2);$

    s = s+1;

end

xt = SUMCS(t,x\_k,2\*pi\*(-K:1:K)/T);

End

---

**- Code for Computing  $X_{ti}$ 's using the function FSWave:**

```
D11 = mod(21903608,11);
```

```
D5 = mod(21903608,5);
```

```
T = 2;
```

```
W=1;
```

```
K1 = 20 + D11;
```

```
t = [-5:0.001:5];
```

```
xt1 = FSWave(t,K,T,W);
```

```
figure;
```

```
title("The signal  $X_{1\_t}$ ");
```

```
subplot(2,1,1)
```

```
plot(t,real(xt1));
```

```
xlabel("t");
```

```
ylabel("Real Part of  $X_{t\_1}$ ");
```

```
grid on
```

```
subplot(2,1,2);
```

```
plot(t,imag(xt1))
```

```
xlabel("t");
```

```
ylabel("Imaginary Part of  $X_{t\_1}$ ");
```

```
grid on
```

```
K2 = 2 + D5;
```

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```
K3 = 7 + D5;

K4 = 15 + D5;

K5 = 50 + D5;

K6 = 100 + D5;

xt2 = FSWave(t,K2,T,W);

xt3 = FSWave(t,K3,T,W);

xt4 = FSWave(t,K4,T,W);

xt5 = FSWave(t,K5,T,W);

xt6 = FSWave(t,K6,T,W);

figure;

plot(t,real(xt2));

xlabel("t");

ylabel("X_t_2");

grid on

title("The signal X_t_2 (K = 5)");

figure;

plot(t,real(xt3));

title("The signal X_t_3 (K = 10)");

xlabel("t");

ylabel("X_t_3");

grid on
```

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```
figure;  
  
plot(t,real(xt4));  
  
title("The signal X_t_4 (K = 18)");  
  
xlabel("t");  
  
ylabel("X_t_4");  
  
grid on  
  
figure;  
  
plot(t,real(xt5));  
  
title("The signal X_t_5 (K = 53)");  
  
xlabel("t");  
  
ylabel("X_t_5");  
  
grid on  
  
figure;  
  
plot(t,real(xt6));  
  
title("The signal X_t_6 (K = 103)");  
  
xlabel("t");  
  
ylabel("X_t_6");  
  
grid on
```



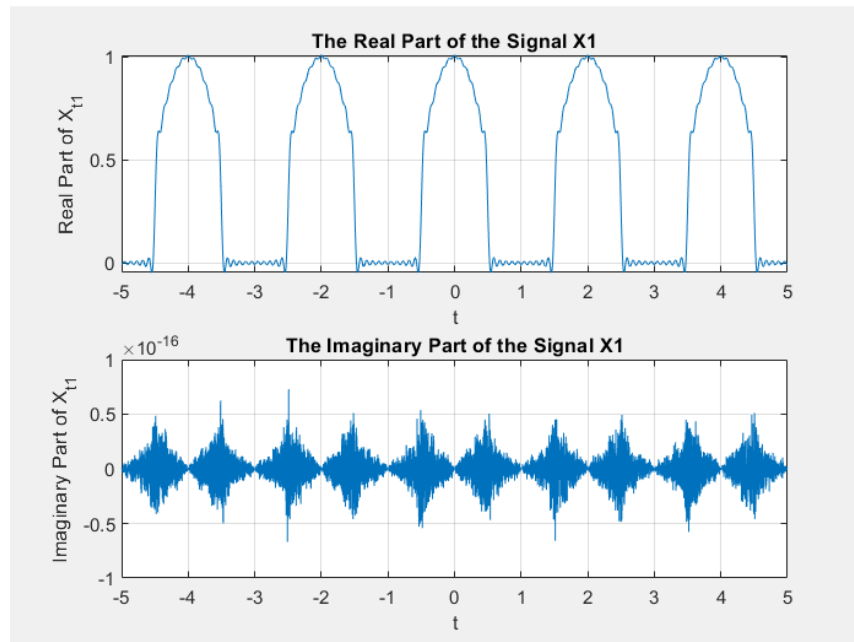


Figure 4: Real and Imaginary Parts of  $X_1(t)$  [K=21]

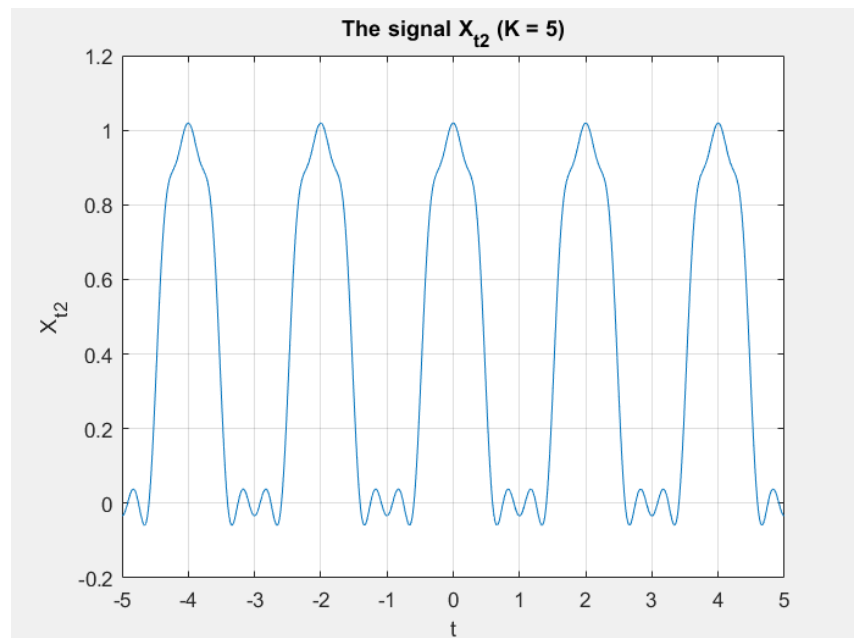


Figure 5: Signal  $X_2(t)$  [K=5]

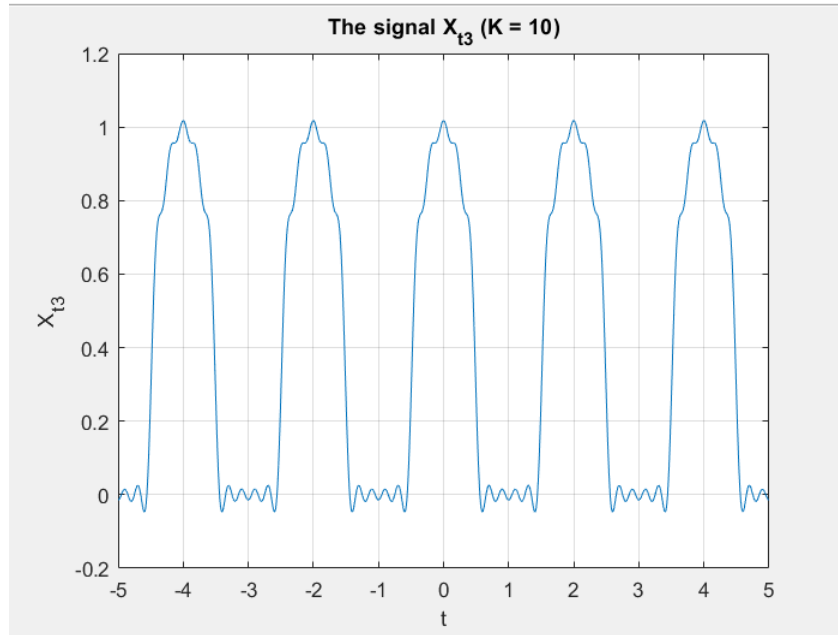


Figure 6: Signal  $X_3(t)$  [K=10]

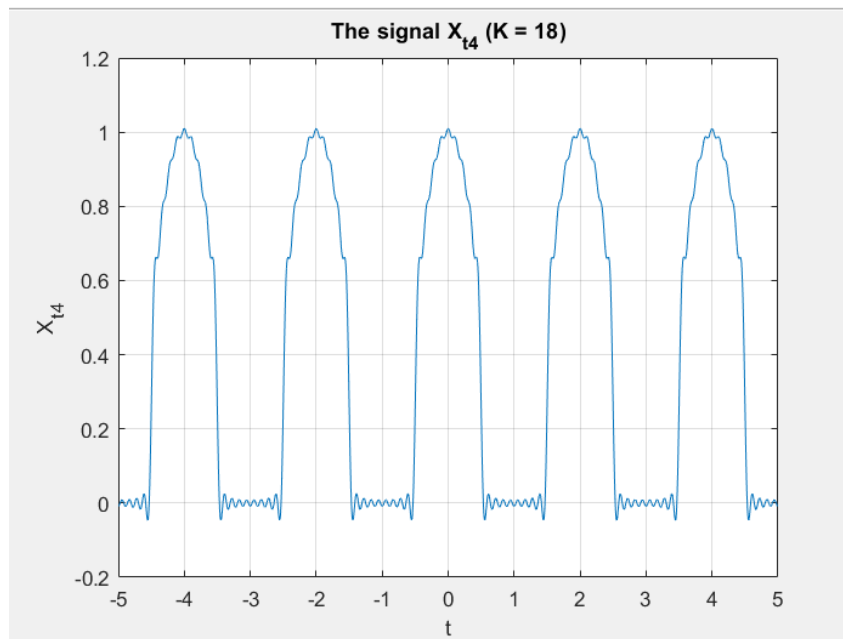


Figure 7: Signal  $X_4(t)$  [K=18]

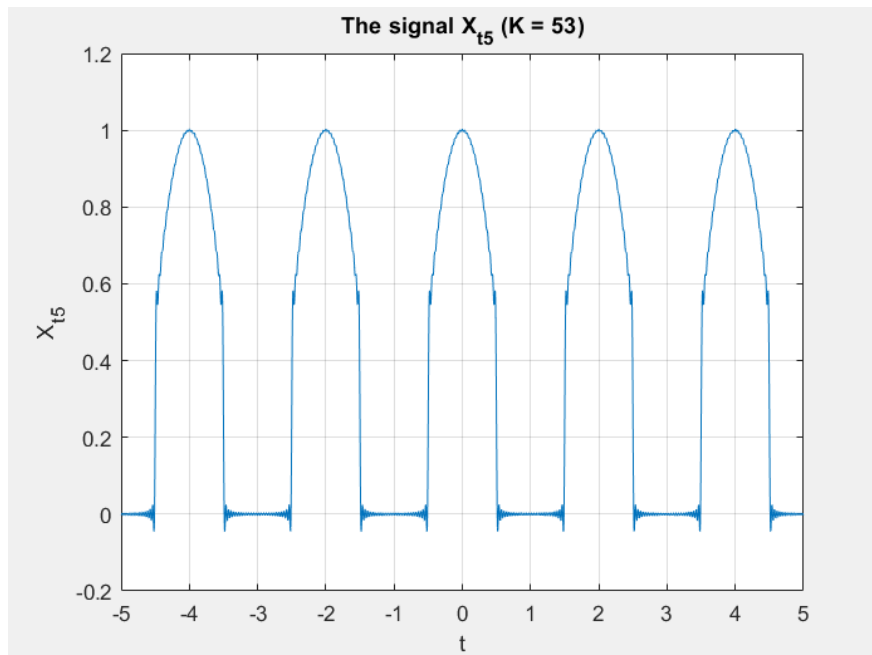


Figure 8: Signal  $X_5(t)$  [K=53]

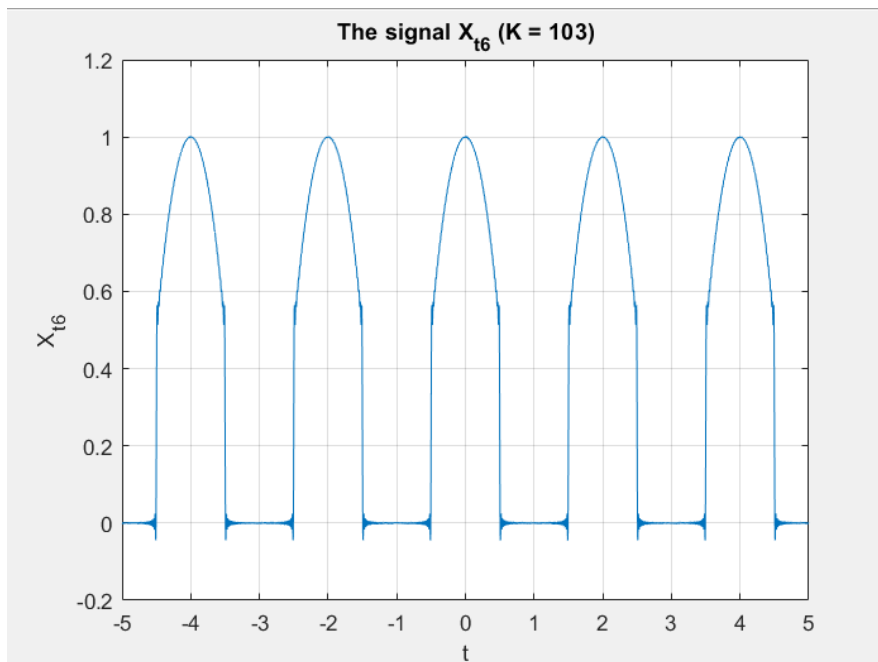


Figure 9: Signal  $X_6(t)$  [K=103]

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## Part 4

a) This operation results in a reflection around the y-axis. For this particular function, there is no change since it is an even function. However, for other functions, the **FSWave** will be indexed differently (starting from K until -K instead of -K until K)

### Code:

```
function [xt] = FSWave(t,K,T,W)

s = 1;

for ii = -K:K

    x_t = @(t)(1-2*t.^2).*exp(-1i*2*pi*-ii*t/T);

    x_k(s) = (1/T)*integral(x_t,-W/2,W/2);

    s = s+1;

end

xt = SUMCS(t,x_k,2*pi*(-K:1:K)/T);

End
```

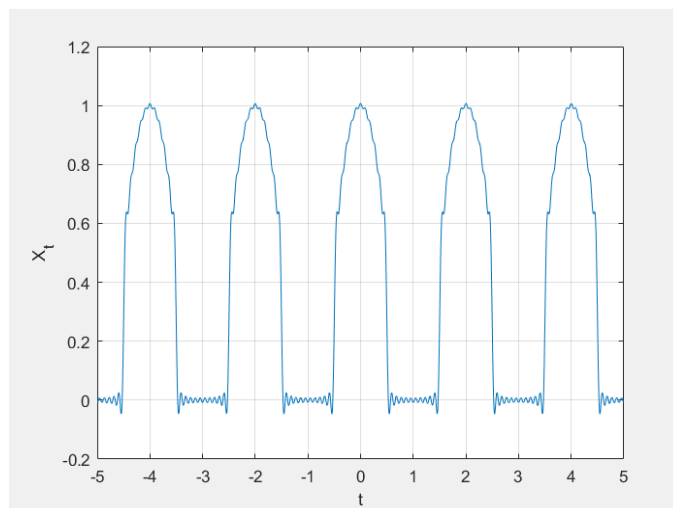


Figure 10: Signal X(t) [K=21]

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**b)** This operation results in a shift to the right by  $t_0 = 0.6$ . To achieve that, the iteration of the loop was changed.

**Code:**

```
function [xt] = FSWave(t,K,T,W,t0)

s = 1;

for ii = -K:K

    x_t = @(t)(1-2*t.^2).*exp(-1i*2*pi*ii*(t+t0)/T);

    x_k(s) = (1/T)*integral(x_t,-W/2,W/2);

    s = s+1;

end

xt = SUMCS(t,x_k,2*pi*(-K:1:K)/T);

end
```

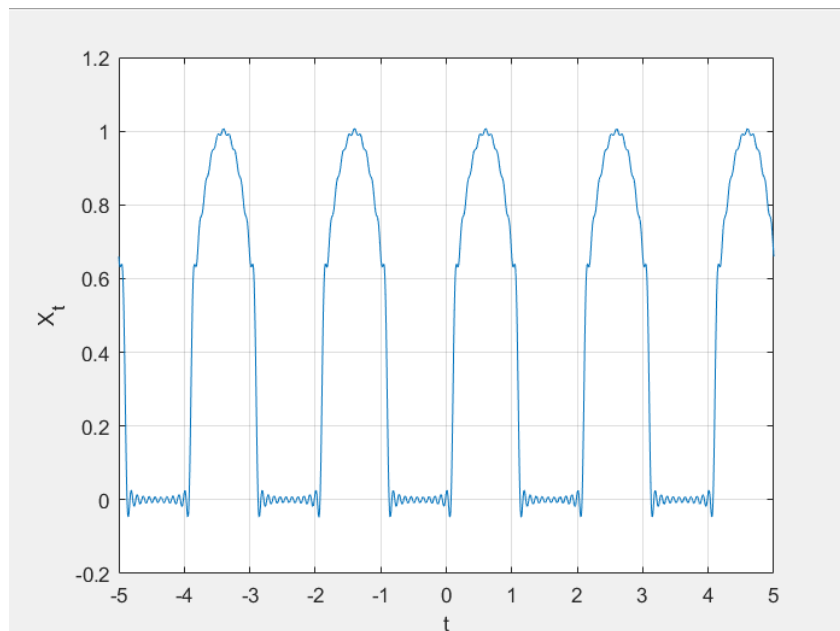


Figure 11: Signal  $X(t)$  [ $K=21$ ] shifted to the right with  $t_0 = 0.6$

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c) This operation corresponds to taking a derivative with respect to  $t$ , and can be achieved by adding the term  $jk2\pi/T$  to the loop.

**Code:**

```
function [xt] = FSWave(t,K,T,W)

s = 1;

for ii = -K:K

    x_t = @(t)(1-2*t.^2).*(1i*ii*2*pi/T).*exp(-1i*2*pi*ii*t/T);

    x_k(s) = (1/T)*integral(x_t,-W/2,W/2);

    s = s+1;

end

xt = SUMCS(t,x_k,2*pi*(-K:1:K)/T);

End
```

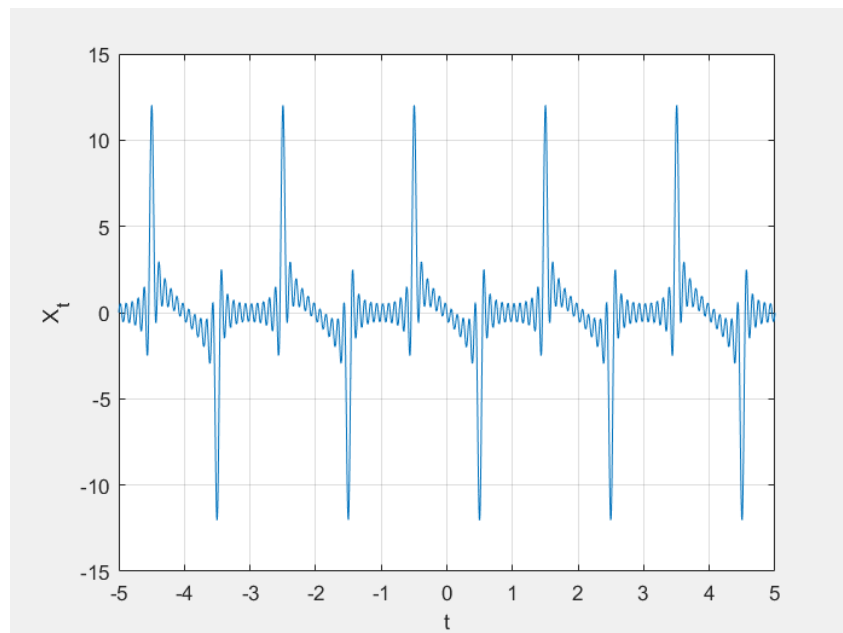


Figure 12: The Derivative of the Original Signal  $X_t$

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**d)** This operation corresponds to the conjugate symmetry property of real signal, and it is achieved by adding if statements to slice the domain of K.

**Code:**

```
function [xt] = FSWave(t,K,T,W)

s = 1;

for ii = -K:K

    if K==0

        x_t = @(t)(1-2*t.^2).*exp(-1i*2*pi*ii*t/T);

    end

    if K < 0

        x_t = @(t)(1-2*t.^2).*exp(-1i*2*pi*(-(ii+1+K))*t/T);

    end

    if K > 0

        x_t = @(t)(1-2*t.^2).*(1i*ii*2*pi/T).*exp(-1i*2*pi*(ii+1-K)*t/T);

    end

    x_k(s) = (1/T)*integral(x_t,-W/2,W/2);

    s = s+1;

end

xt = SUMCS(t,x_k,2*pi*(-K:1:K)/T);

end
```

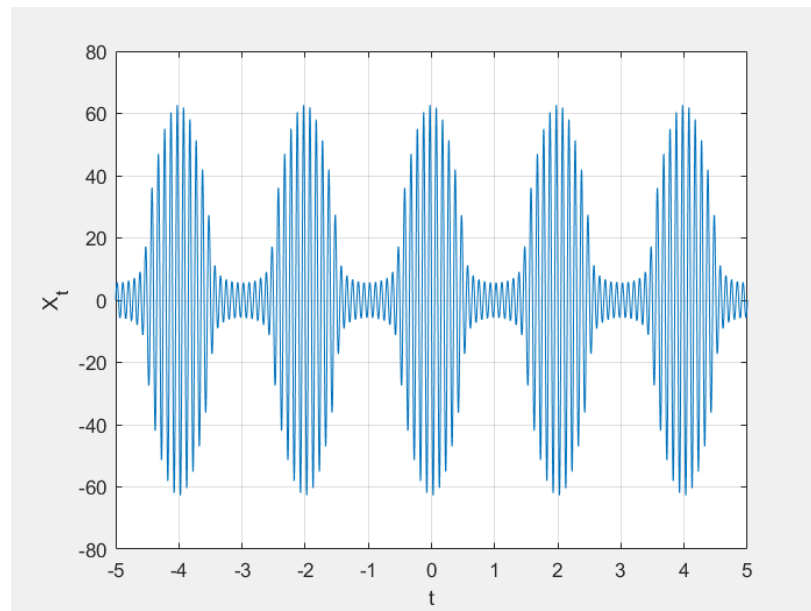


Figure 13: Conjugate SymmetricResult of the Signal  $X(t)$  [K=21]