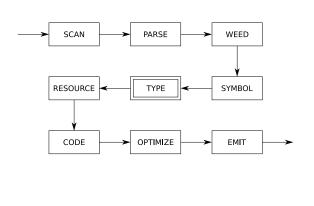
Type checking



The type checker has severals tasks:

- determine the types of all expressions;
- check that values and variables are used correctly; and
- resolve certain ambiguities by transforming the program.

Some languages have no type checker.

COMP 520 Fall 2012 Type checking (3)

A type describes possible values.

The JOOS types are:

- void: the empty type;
- int: the integers;
- char: the characters;
- boolean: true and false; and
- C: objects of class C or any subclass.

Plus an artificial type:

• polynull

which is the type of the polymorphic null constant.

COMP 520 Fall 2012

Type checking (4)

A $type\ annotation$:

int x;

Cons y;

specifies an *invariant* about the run-time behavior:

- x will always contain an integer value; and
- y will always contain null or an object of type Cons or any subclass.

Usual type annotations are not very expressive as invariants.

You can have types without annotations, through type inference (e.g. in ML).

Types can be arbitrarily complex in theory.

A program is *type correct* if the type annotations are valid invariants.

Type correctness is undecidable:

```
int x;
int j;

x = 0;
scanf("%i",&j);
TM(j);
x = true;
```

where TM(j) simulates the j'th Turing machine on empty input.

The program is type correct if and only if TM(j) does not halt on empty input.

A program is *statically* type correct if it satisfies some type rules.

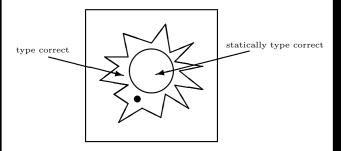
The type rules are chosen to be:

- simple to understand;
- efficient to decide; and
- conservative with respect to type correctness.

Type rules are rarely canonical.

COMP 520 Fall 2012 Type checking (7)

Static type systems are necessarily flawed:



There is always *slack*, i.e. programs that are unfairly rejected by the type checker. Some are even quite useful.

Can you think of such a program?

COMP 520 Fall 2012 Type checking (8)

Type rules may be specified:

- in ordinary prose:

 The argument to the sqrt function must be of type int; the result is of type real.
- as constraints on type variables:

$$sqrt(x): [sqrt(x)] = real \land [x] = int$$

• as logical rules:

$$\frac{\mathcal{S} \vdash \mathbf{x} : \mathbf{int}}{\mathcal{S} \vdash \mathbf{sqrt}(\mathbf{x}) : \mathbf{real}}$$

There are always three kinds:

- 1. declarations: introduction of variables;
- 2. propagations: expression type determines enclosing expression type; and
- 3. restrictions: expression type constrained by usage context

The judgement for statements:

$$L, C, M, V \vdash S$$

means that S is statically type correct with:

- ullet class library $m{L};$
- ullet current class C;
- \bullet current method M; and
- \bullet variables V.

The judgement for expressions:

$$L, C, M, V \vdash E : \tau$$

means that \boldsymbol{E} is statically type correct and has type $\boldsymbol{\tau}.$

The tuple L, C, M, V is an abstraction of the symbol table.

Type rules for statement sequence:

$$egin{aligned} rac{L,C,M,Vdash S_1 & L,C,M,Vdash S_2}{L,C,M,Vdash S_1 & S_2} \ rac{L,C,M,V[\mathtt{x}\mapsto au]dash S}{L,C,M,Vdash au,S} \end{aligned}$$

 $V[x \mapsto \tau]$ just says x maps to τ within V.

Corresponding JOOS source:

COMP 520 Fall 2012 Type checking (11)

Type rules for return statements:

$$egin{aligned} rac{type(L,C,M) = ext{void}}{L,C,M,V dash ext{ return}} \ rac{L,C,M,V dash E \colon au \quad type(L,C,M) = \sigma \quad \sigma := au}{L,C,M,V dash ext{ return } E} \end{aligned}$$

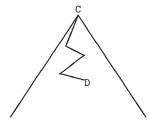
 $\sigma := \tau$ just says something of type σ can be assigned something of type τ .

Corresponding JOOS source:

COMP 520 Fall 2012 Type checking (12)

Assignment compatibility:

- int:=int;
- int:=char;
- char:=char;
- boolean:=boolean;
- C:=polynull; and
- C:=D, if $D \leq C$.



Corresponding JOOS source:

```
int assignTYPE(TYPE *s, TYPE *t)
{ if (s->kind==refK && t->kind==polynullK) return 1;
  if (s->kind==intK && t->kind==charK) return 1;
  if (s->kind!=t->kind) return 0;
  if (s->kind==refK) return subClass(t->class,s->class);
  return 1;
}
```

Type rule for expression statements:

```
\frac{L,C,M,V \vdash E : \tau}{L,C,M,V \vdash E}
```

Corresponding JOOS source:

```
case expK:
    typeImplementationEXP(s->val.expS,class);
    break;
```

Type rule for if-statement:

```
\frac{L,C,M,V \vdash E : \texttt{boolean} \quad L,C,M,V \vdash S}{L,C,M,V \vdash \texttt{if } (E) \ S}
```

Corresponding JOOS source:

COMP 520 Fall 2012 Type checking (15)

Type rule for minus:

```
\frac{L,C,M,V \vdash E_1 : \texttt{int} \quad L,C,M,V \vdash E_2 : \texttt{int}}{L,C,M,V \vdash E_1 ‐ E_2 : \texttt{int}}
```

Corresponding JOOS source:

```
case minusK:
    typeImplementationEXP(e->val.minusE.left,class);
    typeImplementationEXP(e->val.minusE.right,class);
    checkINT(e->val.minusE.left->type,e->lineno);
    checkINT(e->val.minusE.right->type,e->lineno);
    e->type = intTYPE;
    break:
```

Implicit integer cast:

$$\frac{L,C,M,V \vdash E: \texttt{char}}{L,C,M,V \vdash E: \texttt{int}}$$

Corresponding JOOS source:

```
int checkINT(TYPE *t, int lineno)
{ if (t->kind!=intK && t->kind!=charK) {
    reportError("int type expected",lineno);
    return 0;
    }
    return 1;
}
```

Type rule for variables:

$$\frac{V(\mathbf{x}) = \tau}{L, C, M, V \vdash \mathbf{x} : \tau}$$

Corresponding JOOS source:

```
case idK:
    e->type = typeVar(e->val.idE.idsym);
    break;
```

Type rule for assignment:

$$\frac{L,C,M,V \vdash \mathbf{x} \colon \tau \ L,C,M,V \vdash E \colon \sigma \ \tau := \sigma}{L,C,M,V \vdash \mathbf{x} = E \colon \tau}$$

Corresponding JOOS source:

```
case assignK:
    e->type = typeVar(e->val.assignE.leftsym);
    typeImplementationEXP(e->val.assignE.right,class);
    if (!assignTYPE(e->type,e->val.assignE.right->type)) {
        reportError("illegal assignment",e->lineno);
    }
    break;
```

COMP 520 Fall 2012

Type checking (16)

Type rule for equality:

```
L,C,M,V \vdash E_1:\tau_1 L,C,M,V \vdash E_2:\tau_2 \tau_1:=\tau_2 \ \lor \ \tau_2:=\tau_1 L,C,M,V \vdash E_1 == E_2: \texttt{boolean}
```

Corresponding JOOS source:

Type rule for this:

```
L,C,M,V \vdash \texttt{this}: C
```

Corresponding JOOS source:

```
case thisK:
    if (class==NULL) {
        reportError("'this' not allowed here",e->lineno);
    }
    e->type = classTYPE(class);
    break;
```

Type rule for cast:

```
\frac{L,C,M,V \vdash E : \tau \quad \tau \leq \mathtt{C} \ \lor \ \mathtt{C} \leq \tau}{L,C,M,V \vdash (\mathtt{C})E : \ \mathtt{C}}
```

Corresponding JOOS source:

COMP 520 Fall 2012

Type checking (19)

Type checking (20)

Type rule for instanceof:

$$\frac{L,C,M,V \vdash E : \tau \quad \tau \leq \texttt{C} \ \lor \ \texttt{C} \leq \tau}{L,C,M,V \vdash E \text{ instanceof C: boolean}}$$

Corresponding JOOS source:

Why the predicate:

COMP 520 Fall 2012

$$au \leq \mathtt{C} \, \lor \, \mathtt{C} \leq au$$

for "(C) \boldsymbol{E} " and " \boldsymbol{E} instanceof C"?



succeeds $\tau \leq C$



really useful $C \leq \tau$



fails

 $\tau \not\leq \mathsf{C} \land \mathsf{C} \not\leq \tau$

Circle denotes type and all its subtypes. For instance, the following would fail to type check, as no subtype of List can ever be a subtype of the final (!) class String:

```
List 1;
if(l instanceof String) ...
```

Type rule for method invocation:

```
L, C, M, V \vdash E : \sigma \land \sigma \in L
 \exists \rho : \sigma \leq \rho \land m \in methods(\rho)
 \neg static(m)
 L, C, M, V \vdash E_i : \sigma_i
 argtype(L, \rho, m, i) := \gamma_i \wedge \gamma_i := \sigma_i
 type(L, \rho, m) = \tau
\overline{L,C,M,V \vdash E.m(E_1,\ldots,E_n): \tau}
```

Corresponding JOOS source:

```
case invokeK:
  t = typeImplementationRECEIVER(
           e->val.invokeE.receiver,class);
  typeImplementationARGUMENT(e->val.invokeE.args,class);
  if (t->kind!=refK) {
     reportError("receiver must be an object",e->lineno);
      e->type = polynullTYPE;
     s = lookupHierarchy(e->val.invokeE.name,t->class);
     if (s==NULL || s->kind!=methodSym) {
         reportStrError("no such method called %s",
                        e->val.invokeE.name,e->lineno);
         e->type = polynullTYPE;
     } else {
         e->val.invokeE.method = s->val.methodS;
         if (s->val.methodS.modifier==modSTATIC) {
            reportStrError(
                  "static method %s may not be invoked",
                  e->val.invokeE.name,e->lineno);
         \verb|typeImplementationFORMALARGUMENT(|
             s->val.methodS->formals,
             e->val.invokeE.args,e->lineno);
         e->type = s->val.methodS->returntype;
  }
  break;
```

COMP 520 Fall 2012

Type checking (23)

Type rule for constructor invocation:

```
L, C, M, V \vdash E_i : \sigma_i
\exists \vec{\tau} : constructor(L, C, \vec{\tau}) \land
           \vec{\tau} := \vec{\sigma} \wedge
           (\forall \vec{\gamma}: constructor(L, C, \vec{\gamma}) \land \vec{\gamma} := \vec{\sigma}
                         \vec{\gamma} := \vec{\tau}
     L,C,M,V \vdash 	ext{new } \mathtt{C}(E_1,\ldots,E_n) : \mathtt{C}
```

```
Corresponding JOOS source:
case newK:
    if (e->val.newE.class->modifier==modABSTRACT) {
        reportStrError("illegal abstract constructor %s",
                        e->val.newE.class->name,
                        e->lineno);
    typeImplementationARGUMENT(e->val.newE.args,this);
     e->val.newE.constructor =
       selectCONSTRUCTOR(e->val.newE.class->constructors,
                         e->val.newE.args.
                         e->lineno):
     e->type = classTYPE(e->val.newE.class);
    break:
```

Different kinds of type rules are:

• axioms:

COMP 520 Fall 2012

$$L, C, M, V \vdash \mathtt{this} : C$$

• predicates:

$$au < exttt{C} \lor exttt{C} < au$$

• inferences:

```
L,C,M,V \vdash E_1 : \mathtt{int} \quad L,C,M,V \vdash E_2 : \mathtt{int}
              L,C,M,V \vdash E_1 - E_2 : int
```

Type checking (24)

A type proof is a tree in which:

- nodes are inferences; and
- leaves are axioms or true predicates.

A program is statically type correct iff it is the root of some type proof.

A type proof is just a trace of a successful run of the type checker.

An example type proof:

$$\frac{V[x\mapsto A][y\mapsto B](y)=B}{\mathcal{S}\vdash y:B} \frac{\frac{V[x\mapsto A][y\mapsto B](x)=A}{\mathcal{S}\vdash x:A}}{\mathcal{S}\vdash (B)x:B} \xrightarrow{B:=B}$$

$$\frac{L,C,M,V[x\mapsto A][y\mapsto B]\vdash y=(B)x:B}{L,C,M,V[x\mapsto A][y\mapsto B]\vdash y=(B)x;}$$

$$\frac{L,C,M,V[x\mapsto A]\vdash B\ y;\ y=(B)x;}{L,C,M,V\vdash A\ x;\ B\ y;\ y=(B)x;}$$

where $\mathcal{S} = L, C, M, V[x \mapsto A][y \mapsto B]$ and we assume that $B \leq A$.

COMP 520 Fall 2012

Type checking (27)

Type rules for plus:

$$\frac{L,C,M,V \vdash E_1 \colon \text{int} \quad L,C,M,V \vdash E_2 \colon \text{int}}{L,C,M,V \vdash E_1 \vdash E_2 \colon \text{int}}$$

$$\frac{L,C,M,V \vdash E_1 \colon \text{String} \quad L,C,M,V \vdash E_2 \colon \tau}{L,C,M,V \vdash E_1 \vdash E_2 \colon \text{String}}$$

$$\frac{L,C,M,V \vdash E_1 \colon \tau \quad L,C,M,V \vdash E_2 \colon \text{String}}{L,C,M,V \vdash E_1 \vdash E_2 \colon \text{String}}$$

The operator + is overloaded.

COMP 520 Fall 2012 Type checking (28)

```
Corresponding JOOS source:
case plusK:
    typeImplementationEXP(e->val.plusE.left,class);
    typeImplementationEXP(e->val.plusE.right,class);
    e->type = typePlus(e->val.plusE.left,
                       e->val.plusE.right,e->lineno);
    break;
TYPE *typePlus(EXP *left, EXP *right, int lineno)
{ if (equalTYPE(left->type,intTYPE) &&
      equalTYPE(right->type,intTYPE)) {
     return intTYPE;
 if (!equalTYPE(left->type,stringTYPE) &&
     !equalTYPE(right->type,stringTYPE)) {
    reportError("arguments for + have wrong types",
                lineno);
 left->tostring = 1;
 right->tostring = 1;
 return stringTYPE;
```

COMP 520 Fall 2012 Type checking (29) COMP 520 Fall 2012 Type checking (30)

A *coercion* is a conversion function that is inserted automatically by the compiler.

The code:

"abc" + 17 + x

is transformed into:

"abc" + (new Integer(17).toString()) + x.toString()

What effect would a rule like:

$$\frac{L,C,M,V \vdash E_1 \colon \tau \quad L,C,M,V \vdash E_2 \colon \sigma}{L,C,M,V \vdash E_1 + E_2 \colon \mathtt{String}}$$

have on the type system if it were included?

The testing strategy for the type checker involves a further extension of the pretty printer, where the type of every expression is printed explicitly.

These types are then compared to a corresponding manual construction for a sufficient collection of programs.

Furthermore, every error message should be provoked by some test program.