

PYTHON TASK - 7

47. Count Inversions

Objective: Count the number of inversions in an array, where an inversion is when for $a[i] > a[j]$ for $i < j$

Code:

Function to count inversions using Merge Sort

```
def merge_and_count(arr, temp_arr, left, mid, right):
```

```
    i = left # Left subarray index
```

```
    j = mid + 1 # Right subarray index
```

```
    k = left # Merged subarray index
```

```
    inv_count = 0
```

```
    while i <= mid and j <= right:
```

```
        if arr[i] <= arr[j]:
```

```
            temp_arr[k] = arr[i]
```

```
            i += 1
```

```
        else:
```

```
            temp_arr[k] = arr[j]
```

```
            inv_count += (mid - i + 1)
```

```
            j += 1
```

```
        k += 1
```

```
    while i <= mid:
```

```
        temp_arr[k] = arr[i]
```

```
        i += 1
```

```
        k += 1
```

```
    while j <= right:
```

```
        temp_arr[k] = arr[j]
```

```

        j += 1

        k += 1

    for i in range(left, right + 1):

        arr[i] = temp_arr[i]

    return inv_count


def count_inversions(arr, left, right):

    if left >= right:

        return 0

    mid = (left + right) // 2

    temp_arr = arr.copy()

    left_count = count_inversions(arr, left, mid)

    right_count = count_inversions(arr, mid + 1, right)

    merge_count = merge_and_count(arr, temp_arr, left, mid, right)

    return left_count + right_count + merge_count

arr = list(map(int, input("Enter numbers separated by spaces: ").split()))

print(f"Number of inversions: {count_inversions(arr, 0, len(arr) - 1)}")

```

Explanation:

- Uses a modified merge sort to count inversions while sorting the array.
 - Each inversion is counted when merging two halves of the array.
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48. Find the Longest Palindromic Substring

Objective: Find the longest palindromic substring in a given string.

Code:

```
def longest_palindrome(s):  
    if len(s) == 0:  
        return ""  
  
    start, max_length = 0, 1  
  
    for i in range(len(s)):  
        for j in range(i, len(s)):  
            if s[i:j+1] == s[i:j+1][::-1] and (j - i + 1) > max_length:  
                start, max_length = i, j - i + 1  
  
    return s[start:start + max_length]  
  
s = input("Enter a string: ")  
  
print(f"Longest palindromic substring: {longest_palindrome(s)}")
```

Explanation:

- Uses brute force to check all substrings and identify the longest palindrome.
 - Could be optimized using dynamic programming or the expand-around-center approach.
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49. Traveling Salesman Problem (TSP)

Objective: Find the shortest possible route that visits each city once and returns to the origin city.

Code:

```
from itertools import permutations

def tsp(graph, start):

    vertices = list(graph.keys())

    vertices.remove(start)

    min_path = float('inf')

    for perm in permutations(vertices):

        current_path_weight = 0

        k = start

        for j in perm:

            current_path_weight += graph[k][j]

            k = j

        current_path_weight += graph[k][start]

        min_path = min(min_path, current_path_weight)

    return min_path

graph = {

    'A': {'B': 10, 'C': 15, 'D': 20},

    'B': {'A': 10, 'C': 35, 'D': 25},

    'C': {'A': 15, 'B': 35, 'D': 30},

    'D': {'A': 20, 'B': 25, 'C': 30}

}

print(f"Shortest TSP path cost: {tsp(graph, 'A')}")
```

Explanation:

- Uses brute-force permutation to find the shortest cycle.
 - Can be optimized using dynamic programming (Held-Karp algorithm).
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50. Graph Cycle Detection

Objective: Detect whether a graph contains a cycle.

Code:

```
def dfs_cycle(graph, node, visited, parent):  
    visited[node] = True  
    for neighbor in graph[node]:  
        if not visited[neighbor]:  
            if dfs_cycle(graph, neighbor, visited, node):  
                return True  
        elif neighbor != parent:  
            return True  
    return False  
  
def has_cycle(graph):  
    visited = {node: False for node in graph}  
    for node in graph:  
        if not visited[node]:  
            if dfs_cycle(graph, node, visited, None):  
                return True  
    return False
```

```
graph = {  
    'A': ['B', 'C'],  
    'B': ['A', 'D'],  
    'C': ['A', 'D'],  
    'D': ['B', 'C']  
}  
  
print(f"Graph contains cycle: {has_cycle(graph)}")
```

Explanation:

- Uses DFS with a recursion stack to detect cycles in an undirected graph.
 - A back edge indicates a cycle.
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51. Longest Substring Without Repeating Characters

Objective: Given a string, find the length of the longest substring without repeating characters.

Code:

```
def length_of_longest_substring(s):  
    char_index = {}  
    left = 0  
    max_length = 0  
    for right, char in enumerate(s):  
        if char in char_index and char_index[char] >= left:
```

```
        left = char_index[char] + 1

    char_index[char] = right

    max_length = max(max_length, right - left + 1)

return max_length

s = input("Enter a string: ")

print(f"Length of longest substring without repeating characters: {length_of_longest_substring(s)}")
```

Explanation:

- Uses a sliding window with a dictionary to track characters.
 - Adjusts the left boundary whenever a duplicate character is encountered.
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52. Find All Valid Parentheses Combinations

Objective: Generate all possible valid combinations of parentheses.

Code:

```
def generate_parentheses(n, open_count=0, close_count=0, current_str="", result=None):

    if result is None:
        result = []

    if open_count == n and close_count == n:
        result.append(current_str)
        return result

    if open_count < n:
```

```

        generate_parentheses(n, open_count + 1, close_count, current_str + "(", result)

    if close_count < open_count:

        generate_parentheses(n, open_count, close_count + 1, current_str + ")", result)

    return result

n = int(input("Enter number of pairs of parentheses: "))

print("Valid Parentheses Combinations:", generate_parentheses(n))

```

Explanation:

- Uses recursion and backtracking to generate valid combinations.
 - Ensures that an opening bracket always precedes a closing one.
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53. Zigzag Level Order Traversal of Binary Tree

Objective: Traverse a binary tree in a zigzag level order.

Code:

```

from collections import deque

class TreeNode:

    def __init__(self, val=0, left=None, right=None):

        self.val = val

        self.left = left

        self.right = right

def zigzag_level_order(root):

    if not root:

```



```

    return []

result, queue, left_to_right = [], deque([root]), True
while queue:

    level_size = len(queue)

    level_nodes = deque()

    for _ in range(level_size):

        node = queue.popleft()

        if left_to_right:

            level_nodes.append(node.val)

        else:

            level_nodes.appendleft(node.val)

        if node.left:

            queue.append(node.left)

        if node.right:

            queue.append(node.right)

    result.append(list(level_nodes))

    left_to_right = not left_to_right

return result

```

#Example usage:

```
#root = TreeNode(1, TreeNode(2), TreeNode(3))
```

```
#print(zigzag_level_order(root))
```

Explanation:

- Uses a deque to efficiently add elements at both ends.
 - Alternates between left-to-right and right-to-left traversal at each level.
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54. Palindrome Partitioning

Objective: Partition a string such that every substring is a palindrome.

Code:

```
def is_palindrome(s):  
    return s == s[::-1]  
  
def partition_helper(s, start, path, result):  
    if start == len(s):  
        result.append(path[:])  
        return  
  
    for end in range(start + 1, len(s) + 1):  
        if is_palindrome(s[start:end]):  
            path.append(s[start:end])  
            partition_helper(s, end, path, result)  
            path.pop()  
  
def palindrome_partition(s):  
    result = []  
    partition_helper(s, 0, [], result)  
    return result  
  
s = input("Enter a string: ")  
print("Palindrome Partitions:", palindrome_partition(s))
```

Explanation:

- Uses backtracking to explore all possible partitions.
 - Checks each substring to determine if it is a palindrome.
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7. Personal Budget Advisor

Objective: Build a program to track expenses and income, analyze spending patterns, and provide suggestions for saving money.

Code:

```
def add_transaction(transactions, category, amount, transaction_type):

    transactions.append({"category": category, "amount": amount, "type": transaction_type})

def calculate_summary(transactions):

    summary = {}

    for transaction in transactions:

        category = transaction["category"]

        amount = transaction["amount"]

        if transaction["type"] == "expense":

            summary[category] = summary.get(category, 0) + amount

    return summary

def provide_suggestions(income, expenses):

    savings = income - sum(expenses.values())

    print(f"Total Income: {income}")

    print(f"Total Expenses: {sum(expenses.values())}")

    print(f"Savings: {savings}")

    if savings < 0:

        print("Warning: You are overspending! Try reducing expenses in high-spending categories.")

    else:

        print("Good job! Consider investing or saving more.")

def main():

    transactions = []

    income = float(input("Enter your monthly income: "))
```

```

while True:

    action = input("Enter transaction (category amount type[expense/income]) or 'done': ")

    if action.lower() == 'done':

        break

    try:

        category, amount, transaction_type = action.split()

        amount = float(amount)

        if transaction_type not in ["expense", "income"]:

            raise ValueError("Transaction type must be 'expense' or 'income'")

        add_transaction(transactions, category, amount, transaction_type)

    except ValueError as e:

        print(f"Invalid input: {e}")

    expenses = calculate_summary(transactions)

    provide_suggestions(income, expenses)

if __name__ == "__main__":

    main()

```

Explanation:

- Users can input income and transactions (expenses or income).
 - The program tracks expenses by category and provides financial advice.
 - Basic validation ensures correct input format.
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