

1-1.4-9c

EE24BTECH11009 - Mokshith Kumar Reddy

Question:

In what ratio does the point $(-4, 6)$ divide the line segment joining the points $A(-6, 0)$ and $B(3, -8)$?

Solution:

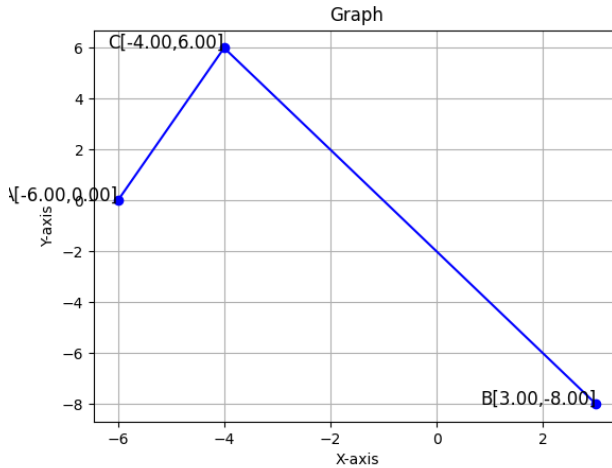


Fig. 0.1: Stem Plot of $y(n)$

Fig. ?? we can see that the given point doesn't lie on the line segment joining A and B.

$$d_1 = \|(A - C)\| \quad (0.1)$$

$$\Rightarrow (A - C)(A - C)^T \quad (0.2)$$

$$\Rightarrow \begin{pmatrix} -2 & -6 \end{pmatrix} \begin{pmatrix} -2 \\ -6 \end{pmatrix} \quad (0.3)$$

$$d_1 = \sqrt{2^2 + 6^2} = \sqrt{40} \quad (0.4)$$

$$(0.5)$$

$$d_2 = \|(B - C)\| \tag{0.6}$$

$$\implies (B - C)(B - C)^T \tag{0.7}$$

$$\implies \begin{pmatrix} 7 & -14 \end{pmatrix} \begin{pmatrix} 7 \\ -14 \end{pmatrix} \tag{0.8}$$

$$d_2 = \sqrt{7^2 + 14^2} = 7\sqrt{5} \tag{0.9}$$

$$\therefore \frac{d_1}{d_2} = \frac{\sqrt{40}}{7\sqrt{5}} \tag{0.10}$$

Parameter	Description
A	$\begin{pmatrix} -6 \\ 0 \end{pmatrix}$
B	$\begin{pmatrix} 3 \\ -8 \end{pmatrix}$
C	$\begin{pmatrix} -4 \\ 6 \end{pmatrix}$
d_1	$d_1 = \ (A - C)\ $
d_2	$d_2 = \ (B - C)\ $

TABLE 0