

HW 6

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<https://github.com/mokys1213/STATS-506-FA-2024/blob/main/HW6/hw6.pdf>

```
library(DBI)
library(parallel)
library(future)
library(data.table)

# Import the SQLite database of the Lahman data
lahman <- dbConnect(RSQLite::SQLite(), "lahman_1871-2022.sqlite")

# Reading in fielding data
Fielding=dbGetQuery(lahman, "SELECT * FROM Fielding")
# Calculating Range Factor
Fielding$RF=3*(Fielding$P0+Fielding$A)/Fielding$InnOuts
# Data cleaning
fielding=na.omit(Fielding[, c("teamID", "RF")])
fielding=fielding[!is.infinite(fielding$RF),]

# Calculating the average RF for each team
point_est=aggregate(fielding$RF,by=list(fielding$teamID), FUN =mean)
colnames(point_est)=c("teamID", "meanRF")
```

A

```
fielding_dat=data.table(fielding)

# Bootstrap using data.table
f = function(data) {
  tmp=data[,.SD[sample(.N, replace=TRUE)], by=teamID]
  return(tmp[,.(meanRF = mean(RF)), by=teamID])
}

# Checking the function
f(fielding_dat)
```

```
##      teamID    meanRF
##      <char>    <num>
##    1:   SFN 0.3935171
##    2:   CHN 0.4176912
##    3:   CHA 0.4095987
```

```
## 4: BOS 0.4042868
## 5: SEA 0.3938972
## ---
## 136: NYP 0.4116954
## 137: PHP 0.4260829
## 138: IN1 0.3881667
## 139: RIC 0.5833787
## 140: BL4 0.4195785
```

```
# Measuring time
system.time(f(fielding_dat))
```

```
## user system elapsed
## 0.012 0.001 0.013
```

A1: Without any parallel processing

```
reps=1000

# Using lapply
system.time({
  result1=lapply(seq_len(reps), function(x) f(fielding_dat))
})
```

```
## user system elapsed
## 11.597 0.523 12.291
```

A2: Using parallel processing with the parallel package

```
# Using mclapply
system.time({
  result2=mclapply(seq_len(reps), function(x) f(fielding_dat), mc.cores=5)
})
```

```
## user system elapsed
## 0.008 0.040 2.681
```

A3: Using futures with the future package

```
# Using future
plan(multisession)
system.time({
  result3=lapply(seq_len(reps), function(x) {
    future(f(fielding_dat), seed=TRUE)
  })
  result3 =lapply(result3,value)
})
```

```
##      user  system elapsed
## 56.943   1.785   73.628
```

B

```
# Generating a table showing the estimated RF and associated SE from the three approaches.
tablesum <- function(results) {
  bind=rbindlist(results)
  summary=bind[, .(meanRF=mean(meanRF), SE=sd(meanRF)), by=teamID]
  return(summary)
}

# Showing the results
print(tablesum(result1), n = 1e3)
```

```
##      teamID      meanRF      SE
##      <char>      <num>      <num>
## 1:      SFN 0.4015856 0.005548623
## 2:      CHN 0.4152027 0.004840454
## 3:      CHA 0.4062771 0.005333819
## 4:      BOS 0.4018672 0.005450617
## 5:      SEA 0.3862459 0.006413892
## 6:      NYA 0.4039726 0.005312711
## 7:      NYN 0.4023262 0.005483719
## 8:      ATL 0.3883860 0.005922788
## 9:      ML1 0.4411198 0.014990340
## 10:     ML4 0.4140520 0.008773802
## 11:     CAL 0.4163273 0.008530045
## 12:     BAL 0.3924154 0.005413244
## 13:     LAN 0.3947458 0.005632953
## 14:     OAK 0.4029759 0.006744534
## 15:     HOU 0.4011189 0.005986353
## 16:     WAS 0.3742871 0.008146508
## 17:     MIN 0.3917549 0.006009025
## 18:     PH3 0.4685152 0.087948995
## 19:     BR2 0.4003723 0.025805475
## 20:     PHI 0.4008488 0.004861431
## 21:     BSN 0.4552796 0.008723556
## 22:     PIT 0.4108443 0.004813931
## 23:     BRO 0.4424222 0.010274781
## 24:     TL2 0.4195331 0.061248408
## 25:     CLE 0.4006950 0.005150992
## 26:     DET 0.4068974 0.005486882
## 27:     FLO 0.3704923 0.010094110
## 28:     MIL 0.3590150 0.008352183
## 29:     COL 0.3895652 0.008198934
## 30:     SLN 0.4196549 0.004938733
## 31:     KCA 0.3908591 0.006094969
## 32:     TBA 0.3562090 0.007859806
## 33:     KC1 0.4066433 0.012945316
## 34:     TRO 0.4717319 0.042538102
```

##	35:	WS1	0.4641617	0.012818765
##	36:	CIN	0.4033354	0.004881936
##	37:	SLA	0.4656242	0.017047489
##	38:	SDN	0.3939570	0.005994215
##	39:	TEX	0.3854763	0.006127194
##	40:	LAA	0.3757023	0.009442694
##	41:	ARI	0.3663700	0.008360694
##	42:	TOR	0.3753444	0.006648025
##	43:	SR1	0.4651007	0.040514926
##	44:	SL4	0.4365461	0.016387032
##	45:	RC1	0.5735413	0.082624004
##	46:	PH2	0.4649533	0.033990321
##	47:	BS1	0.4528255	0.032241768
##	48:	HR1	0.3825420	0.038645452
##	49:	CN1	0.4400871	0.023781161
##	50:	MIA	0.3633644	0.011995360
##	51:	TRN	0.4806534	0.029661224
##	52:	BL2	0.4012179	0.015742796
##	53:	SE1	0.4181083	0.045361764
##	54:	PT1	0.4436742	0.023068564
##	55:	WSU	0.4016392	0.035555350
##	56:	CL3	0.4589168	0.029715639
##	57:	ML3	0.4643193	0.064412238
##	58:	MON	0.4181237	0.008306277
##	59:	KCU	0.4176300	0.030045098
##	60:	ANA	0.4155183	0.015349001
##	61:	WS2	0.3992829	0.012290963
##	62:	MID	0.4572700	0.061598959
##	63:	CL2	0.4358365	0.022202672
##	64:	NY1	0.4401587	0.009192382
##	65:	KC2	0.3815427	0.025660667
##	66:	CL4	0.4437824	0.016544081
##	67:	BR1	0.4358647	0.041004996
##	68:	CL1	0.3836684	0.039690060
##	69:	ELI	0.5259058	0.063860564
##	70:	WS6	0.4139049	0.056224486
##	71:	LS1	0.5307575	0.056369492
##	72:	WS3	0.4111216	0.046078156
##	73:	NY2	0.3890849	0.022881526
##	74:	HAR	0.4220154	0.045992540
##	75:	PRO	0.4658675	0.022646723
##	76:	LS3	0.4895347	0.015424618
##	77:	SL5	0.3764828	0.030431896
##	78:	WS9	0.4390964	0.036480422
##	79:	BLN	0.4497400	0.018971297
##	80:	MLA	0.4199814	0.037257102
##	81:	IN3	0.4194124	0.030388336
##	82:	BRP	0.4333528	0.055014201
##	83:	CN3	0.4350688	0.049875765
##	84:	LS2	0.4737589	0.016539072
##	85:	PH1	0.4535927	0.027016928
##	86:	PHA	0.4657977	0.018041976
##	87:	FW1	0.4433062	0.051831750
##	88:	BLA	0.4953166	0.032144523

##	89:	PH4	0.4127230	0.015564623
##	90:	TL1	0.4571707	0.047584297
##	91:	WS8	0.4463205	0.021726605
##	92:	CHU	0.3428147	0.037015189
##	93:	BLU	0.3828468	0.041752543
##	94:	WS5	0.4103414	0.051439715
##	95:	IN2	0.4648709	0.045539411
##	96:	PHU	0.4807114	0.046933258
##	97:	WIL	0.3802887	0.059775518
##	98:	CLP	0.4056035	0.042826402
##	99:	BL3	0.4441119	0.039147787
##	100:	SLU	0.3923151	0.039074887
##	101:	KCN	0.4415656	0.048107401
##	102:	CN2	0.4386645	0.020628854
##	103:	MLU	0.5073960	0.129686663
##	104:	DTN	0.4218506	0.017442103
##	105:	BFP	0.4641852	0.051966220
##	106:	CL6	0.4098781	0.028563606
##	107:	CHP	0.4747089	0.052760891
##	108:	NH1	0.4410844	0.051488788
##	109:	CNU	0.4474828	0.050742757
##	110:	SPU	0.4610643	0.085990610
##	111:	KEO	0.5174475	0.112212223
##	112:	WS7	0.4507936	0.049633423
##	113:	RC2	0.4727813	0.044291827
##	114:	BL1	0.4399462	0.028813231
##	115:	SL2	0.3919014	0.058166453
##	116:	SL3	0.3987293	0.039511631
##	117:	SR2	0.4116983	0.040263192
##	118:	CL5	0.4410159	0.044714822
##	119:	NY4	0.4416192	0.024834697
##	120:	NY3	0.3809282	0.040519770
##	121:	PTP	0.4469741	0.052152338
##	122:	BR3	0.4470881	0.022739839
##	123:	ML2	0.4379202	0.052418984
##	124:	WOR	0.4249979	0.034565020
##	125:	PHN	0.4509289	0.042758157
##	126:	ALT	0.3888404	0.052384957
##	127:	WS4	0.4627325	0.057248510
##	128:	CH2	0.4377042	0.034642850
##	129:	SL1	0.3360628	0.063221335
##	130:	BSU	0.4182306	0.057617986
##	131:	BR4	0.4409474	0.047697351
##	132:	CH1	0.4303330	0.061009497
##	133:	BFN	0.4518598	0.021036686
##	134:	BSP	0.4316373	0.046686950
##	135:	BS2	0.4338238	0.048604672
##	136:	NYP	0.4253920	0.046571359
##	137:	PHP	0.4413326	0.057354723
##	138:	IN1	0.4102675	0.066602627
##	139:	RIC	0.5084548	0.062392455
##	140:	BL4	0.4324159	0.057403901
##		teamID	meanRF	SE

```
print(tablesom(result2), n = 1e3)
```

```
##      teamID      meanRF      SE
##      <char>      <num>      <num>
##  1:   SFN 0.4014654 0.005443352
##  2:   CHN 0.4151156 0.004875964
##  3:   CHA 0.4061641 0.005571379
##  4:   BOS 0.4019716 0.005604711
##  5:   SEA 0.3865818 0.006613502
##  6:   NYA 0.4037381 0.005319315
##  7:   NYN 0.4022923 0.005507249
##  8:   ATL 0.3883248 0.006123525
##  9:   ML1 0.4401429 0.014842617
## 10:   ML4 0.4144956 0.008735224
## 11:   CAL 0.4163691 0.008612240
## 12:   BAL 0.3926185 0.005554469
## 13:   LAN 0.3952064 0.005660156
## 14:   OAK 0.4032095 0.007075038
## 15:   HOU 0.4015026 0.006159849
## 16:   WAS 0.3743384 0.007959814
## 17:   MIN 0.3916289 0.005678865
## 18:   PH3 0.4689911 0.089054648
## 19:   BR2 0.3990262 0.025196203
## 20:   PHI 0.4007613 0.004483625
## 21:   BSN 0.4558867 0.009253671
## 22:   PIT 0.4108975 0.004895764
## 23:   BRO 0.4426302 0.009888797
## 24:   TL2 0.4192080 0.061056446
## 25:   CLE 0.4007240 0.005184637
## 26:   DET 0.4066766 0.005452332
## 27:   FLO 0.3705256 0.010153952
## 28:   MIL 0.3595080 0.008343490
## 29:   COL 0.3891338 0.007674044
## 30:   SLN 0.4200579 0.005182955
## 31:   KCA 0.3911530 0.006102213
## 32:   TBA 0.3566819 0.007973467
## 33:   KC1 0.4079047 0.012365538
## 34:   TRO 0.4722205 0.042115411
## 35:   WS1 0.4635334 0.012272567
## 36:   CIN 0.4033035 0.004979030
## 37:   SLA 0.4662554 0.017754267
## 38:   SDN 0.3940204 0.005983366
## 39:   TEX 0.3850001 0.006261527
## 40:   LAA 0.3762473 0.009364963
## 41:   ARI 0.3661683 0.008648266
## 42:   TOR 0.3751432 0.006280236
## 43:   SR1 0.4646271 0.038549752
## 44:   SL4 0.4364402 0.016758221
## 45:   RC1 0.5755878 0.083462763
## 46:   PH2 0.4644014 0.033438000
## 47:   BS1 0.4522637 0.032480972
## 48:   HR1 0.3824582 0.038577900
## 49:   CN1 0.4409243 0.023727181
```

##	50:	MIA	0.3641633	0.012389181
##	51:	TRN	0.4812443	0.030071181
##	52:	BL2	0.4010386	0.015952175
##	53:	SE1	0.4170236	0.042921637
##	54:	PT1	0.4426714	0.022964696
##	55:	WSU	0.3989184	0.034402519
##	56:	CL3	0.4595419	0.029388992
##	57:	ML3	0.4627936	0.061707823
##	58:	MON	0.4168636	0.008617441
##	59:	KCU	0.4174459	0.032120394
##	60:	ANA	0.4147788	0.015179625
##	61:	WS2	0.3987252	0.012970048
##	62:	MID	0.4633911	0.062196106
##	63:	CL2	0.4354306	0.023363323
##	64:	NY1	0.4401348	0.009144253
##	65:	KC2	0.3811373	0.026217348
##	66:	CL4	0.4449726	0.016457299
##	67:	BR1	0.4381126	0.043767605
##	68:	CL1	0.3825971	0.039164888
##	69:	ELI	0.5261571	0.062368489
##	70:	WS6	0.4193702	0.056039170
##	71:	LS1	0.5281010	0.058301366
##	72:	WS3	0.4087467	0.046491526
##	73:	NY2	0.3887807	0.022697157
##	74:	HAR	0.4162494	0.046368955
##	75:	PRO	0.4660797	0.021988128
##	76:	LS3	0.4893312	0.015699802
##	77:	SL5	0.3757008	0.029418376
##	78:	WS9	0.4377929	0.036202944
##	79:	BLN	0.4496816	0.018332557
##	80:	MLA	0.4187304	0.039134932
##	81:	IN3	0.4205419	0.030404763
##	82:	BRP	0.4360232	0.055093171
##	83:	CN3	0.4377519	0.049909226
##	84:	LS2	0.4734669	0.015614219
##	85:	PH1	0.4543023	0.027137332
##	86:	PHA	0.4655620	0.017668018
##	87:	FW1	0.4387507	0.050075165
##	88:	BLA	0.4964733	0.031412333
##	89:	PH4	0.4129613	0.015713004
##	90:	TL1	0.4547512	0.046511769
##	91:	WS8	0.4472436	0.020774946
##	92:	CHU	0.3425424	0.037505675
##	93:	BLU	0.3873445	0.042983458
##	94:	WS5	0.4046470	0.049634286
##	95:	IN2	0.4642031	0.046898956
##	96:	PHU	0.4827670	0.046514024
##	97:	WIL	0.3821357	0.058193110
##	98:	CLP	0.4052256	0.045836243
##	99:	BL3	0.4463687	0.040843488
##	100:	SLU	0.3935738	0.039856210
##	101:	KCN	0.4422416	0.047544105
##	102:	CN2	0.4390991	0.020897039
##	103:	MLU	0.5147740	0.128924068

```

## 104:   DTN  0.4225362 0.017054329
## 105:   BFP  0.4619448 0.053001935
## 106:   CL6  0.4107172 0.027156349
## 107:   CHP  0.4757945 0.049684404
## 108:   NH1  0.4392346 0.047132225
## 109:   CNU  0.4470959 0.052858066
## 110:   SPU  0.4626847 0.082729773
## 111:   KEO  0.5054762 0.111800998
## 112:   WS7  0.4482926 0.047693413
## 113:   RC2  0.4731018 0.043884938
## 114:   BL1  0.4428298 0.030402385
## 115:   SL2  0.3957445 0.059777618
## 116:   SL3  0.3963887 0.039404156
## 117:   SR2  0.4137706 0.040552425
## 118:   CL5  0.4425696 0.045736958
## 119:   NY4  0.4413813 0.025668759
## 120:   NY3  0.3818018 0.041561453
## 121:   PTP  0.4485407 0.052673313
## 122:   BR3  0.4487129 0.022875081
## 123:   ML2  0.4402394 0.056347354
## 124:   WOR  0.4238398 0.034861673
## 125:   PHN  0.4503025 0.039609685
## 126:   ALT  0.3868348 0.048512136
## 127:   WS4  0.4676806 0.058847291
## 128:   CH2  0.4399678 0.035906559
## 129:   SL1  0.3384520 0.065556036
## 130:   BSU  0.4206429 0.058981727
## 131:   BR4  0.4399792 0.046990115
## 132:   CH1  0.4277067 0.060972945
## 133:   BFN  0.4511865 0.020295827
## 134:   BSP  0.4308282 0.049596613
## 135:   BS2  0.4294871 0.047170174
## 136:   NYP  0.4232235 0.048630060
## 137:   PHP  0.4441681 0.057445982
## 138:   IN1  0.4080384 0.065359147
## 139:   RIC  0.5100174 0.070025076
## 140:   BL4  0.4279211 0.057139006
##      teamID    meanRF      SE

```

```
print(tablesุม(result3), n = 1e3)
```

```

##      teamID    meanRF      SE
##      <char>    <num>    <num>
##  1:   SFN  0.4020027 0.005499027
##  2:   CHN  0.4150729 0.004774425
##  3:   CHA  0.4058265 0.005543303
##  4:   BOS  0.4018623 0.005281289
##  5:   SEA  0.3864168 0.006337147
##  6:   NYA  0.4038713 0.005550762
##  7:   NYN  0.4023526 0.005558205
##  8:   ATL  0.3882148 0.005919950
##  9:   ML1  0.4421785 0.015336414
## 10:   ML4  0.4140864 0.009191521
## 11:   CAL  0.4157758 0.007945086

```


##	12:	BAL	0.3923183	0.005454746
##	13:	LAN	0.3949039	0.005646110
##	14:	OAK	0.4031497	0.006768886
##	15:	HOU	0.4013114	0.006028147
##	16:	WAS	0.3743151	0.007978804
##	17:	MIN	0.3916913	0.005743764
##	18:	PH3	0.4660780	0.086461158
##	19:	BR2	0.4010329	0.026233865
##	20:	PHI	0.4009381	0.004862864
##	21:	BSN	0.4556994	0.008787236
##	22:	PIT	0.4113301	0.004854216
##	23:	BRO	0.4423843	0.010231063
##	24:	TL2	0.4181026	0.061767121
##	25:	CLE	0.4005702	0.005410103
##	26:	DET	0.4068211	0.005408750
##	27:	FLO	0.3705360	0.009823277
##	28:	MIL	0.3589800	0.008283465
##	29:	COL	0.3896212	0.007712818
##	30:	SLN	0.4197300	0.005229595
##	31:	KCA	0.3904650	0.006312580
##	32:	TBA	0.3567485	0.008203569
##	33:	KC1	0.4080144	0.012942366
##	34:	TRO	0.4713135	0.042262172
##	35:	WS1	0.4635700	0.012439979
##	36:	CIN	0.4032252	0.004842085
##	37:	SLA	0.4667640	0.017027565
##	38:	SDN	0.3939787	0.005806459
##	39:	TEX	0.3852003	0.005982521
##	40:	LAA	0.3755464	0.009157181
##	41:	ARI	0.3661391	0.008401004
##	42:	TOR	0.3749111	0.006527189
##	43:	SR1	0.4658480	0.038912665
##	44:	SL4	0.4357454	0.017047647
##	45:	RC1	0.5764453	0.079367580
##	46:	PH2	0.4635437	0.032357437
##	47:	BS1	0.4513139	0.033075996
##	48:	HR1	0.3839234	0.038511906
##	49:	CN1	0.4420533	0.023897161
##	50:	MIA	0.3638169	0.012396546
##	51:	TRN	0.4812331	0.029756431
##	52:	BL2	0.4012957	0.015998075
##	53:	SE1	0.4166973	0.043352936
##	54:	PT1	0.4429240	0.023621942
##	55:	WSU	0.3995913	0.034750931
##	56:	CL3	0.4585162	0.029565323
##	57:	ML3	0.4639499	0.061097882
##	58:	MON	0.4169643	0.008660215
##	59:	KCU	0.4165945	0.030833172
##	60:	ANA	0.4151118	0.015692492
##	61:	WS2	0.3988202	0.013096947
##	62:	MID	0.4561584	0.062623574
##	63:	CL2	0.4366970	0.022723743
##	64:	NY1	0.4395884	0.008718195
##	65:	KC2	0.3806696	0.025268556

```

## 66: CL4 0.4454312 0.016900875
## 67: BR1 0.4372849 0.043969044
## 68: CL1 0.3844542 0.039587726
## 69: ELI 0.5275753 0.062036759
## 70: WS6 0.4151643 0.058175022
## 71: LS1 0.5297775 0.055746450
## 72: WS3 0.4080525 0.045591350
## 73: NY2 0.3897475 0.023582947
## 74: HAR 0.4158674 0.046440372
## 75: PRO 0.4651514 0.022153411
## 76: LS3 0.4889190 0.015595433
## 77: SL5 0.3741587 0.029793941
## 78: WS9 0.4385071 0.036768880
## 79: BLN 0.4491186 0.019057801
## 80: MLA 0.4203107 0.037054016
## 81: IN3 0.4188397 0.031970979
## 82: BRP 0.4345763 0.054928428
## 83: CN3 0.4360100 0.051831352
## 84: LS2 0.4734168 0.016256287
## 85: PH1 0.4544291 0.027726291
## 86: PHA 0.4654056 0.017789607
## 87: FW1 0.4402167 0.050184855
## 88: BLA 0.4938332 0.030837295
## 89: PH4 0.4121453 0.014879365
## 90: TL1 0.4552594 0.048596536
## 91: WS8 0.4479207 0.021820671
## 92: CHU 0.3419787 0.035314841
## 93: BLU 0.3842919 0.041279192
## 94: WS5 0.4082562 0.051562812
## 95: IN2 0.4638614 0.046144067
## 96: PHU 0.4780305 0.045249486
## 97: WIL 0.3820870 0.061608628
## 98: CLP 0.4040893 0.044919796
## 99: BL3 0.4440157 0.040153194
## 100: SLU 0.3925639 0.039548351
## 101: KCN 0.4423467 0.050913978
## 102: CN2 0.4382885 0.020172763
## 103: MLU 0.5150337 0.128047011
## 104: DTN 0.4221191 0.016575940
## 105: BFP 0.4632638 0.053904048
## 106: CL6 0.4114028 0.028658871
## 107: CHP 0.4756650 0.050071333
## 108: NH1 0.4407976 0.047348308
## 109: CNU 0.4449681 0.049144091
## 110: SPU 0.4630574 0.088382229
## 111: KEO 0.5117600 0.117424227
## 112: WS7 0.4525335 0.047367236
## 113: RC2 0.4759832 0.046205525
## 114: BL1 0.4423453 0.029520413
## 115: SL2 0.3923168 0.057969989
## 116: SL3 0.3965585 0.038824402
## 117: SR2 0.4123703 0.040099103
## 118: CL5 0.4411244 0.043511654
## 119: NY4 0.4420907 0.024957413

```

```
## 120:   NY3  0.3818029  0.041146568
## 121:   PTP  0.4485610  0.052509020
## 122:   BR3  0.4482644  0.022290666
## 123:   ML2  0.4406556  0.056567941
## 124:   WOR  0.4236178  0.033893648
## 125:   PHN  0.4524009  0.041580204
## 126:   ALT  0.3874818  0.049803691
## 127:   WS4  0.4642801  0.059124515
## 128:   CH2  0.4376474  0.036265108
## 129:   SL1  0.3388403  0.062056697
## 130:   BSU  0.4189833  0.057032787
## 131:   BR4  0.4405334  0.048290913
## 132:   CH1  0.4287401  0.059669971
## 133:   BFN  0.4514544  0.020450530
## 134:   BSP  0.4323097  0.048596153
## 135:   BS2  0.4302785  0.046405446
## 136:   NYP  0.4243027  0.047925187
## 137:   PHP  0.4419361  0.057272274
## 138:   IN1  0.4068618  0.063429217
## 139:   RIC  0.5083798  0.068834129
## 140:   BL4  0.4304018  0.058906899
##      teamID    meanRF      SE
```

C

Without Parallel Processing (lapply) it took 11.7 seconds for 1000 simulations

Using parallel (mclapply) it took 2.6 seconds for 1000 simulations

Using future Package, it took 72.8 seconds for 1000 simulations

Using parallel (mclapply) is the best choice for this problem. It is the fastest.

But all three methods resulted similar mean estimates and standard errors