Monte-Carlo examples in R

Serial vs parallel code Meelis Utt

Setup

Let's source the setup (function, analytical solution, number of iterations).

```
##
## > options(scipen = 1000)
##
## > n <- 10000000
##
## > header <- c("n", "computational", "analytical", "error",
## + "walltime", "type")
##
## > f <- function(x) {
## + return(x^2 + x^4 + sin(x) + cos(x) + x^25)
## + }
##</pre>
```

Serial implementations

start <- Sys.time()</pre>

> analytical <- integrate(f, 0, 1)\$value</pre>

source("Setup.R",echo = T)

Let's start with a simple implementation of Monte-Carlo method.

```
MCser1 <- function(n){</pre>
  start <- Sys.time()</pre>
  i \leftarrow runif(n,0,1)
  EX <- mean(f(i))</pre>
  end <- Sys.time()</pre>
  time <- difftime(end,start)</pre>
  error <- (EX - analytical) %>% abs
  return(c(n,EX,analytical,error,time,"MCser1"))
}
data.table(t(MCser1(n))) %>% setNames(header)
##
                    computational
                                           analytical
                                                                         error
## 1: 10000000 1.87353741604257 1.87296355073463 0.000573865307943233
                walltime
## 1: 2.04202342033386 MCser1
Let's try a bit more vectorized solution, using the *apply function.
MCser2 <- function(n,ncols=1000){</pre>
```

```
dt <- matrix(runif(n,0,1),ncol = ncols)</pre>
  EX <- sapply(1:ncols,function(i,dt){</pre>
      EX <- dt[,i] %>% f %>% mean
    },dt) %>% mean
  end <- Sys.time()</pre>
  time <- difftime(end,start)</pre>
  error <- (EX - analytical) %>% abs
  return(c(n,EX,analytical,error,time,"MCser2"))
}
data.table(t(MCser2(n))) %>% setNames(header)
##
                   computational
                                         analytical
                                                                     error
## 1: 10000000 1.87266314578146 1.87296355073463 0.000300404953171185
##
               walltime
                           type
## 1: 1.60613822937012 MCser2
Let's try an approach using data.table.
MCser3 <- function(n){</pre>
  start <- Sys.time()</pre>
  dt <- data.table(unif = runif(n,0,1))</pre>
  EX <- dt[,.(EX = mean(f(unif)))] %>% unlist %>% unname
  end <- Sys.time()</pre>
  time <- difftime(end,start)</pre>
  error <- (EX - analytical) %>% abs
  return(c(n,EX,analytical,error,time,"MCser3"))
data.table(t(MCser3(n))) %>% setNames(header)
              n
                   computational
                                         analytical
                                                                       error
## 1: 10000000 1.87295819430205 1.87296355073463 0.00000535643257837393
               walltime
## 1: 1.68406891822815 MCser3
Let's try divide-and-conquer approach with data.table.
MCser4 <- function(n,ncols=1000){</pre>
  start <- Sys.time()</pre>
  dt <- matrix(runif(n,0,1),ncol=ncols) %>% data.table
  EX <- dt[,lapply(.SD,f)][,lapply(.SD,mean)][,.(EX = sum(.SD)/ncols)] %>% unlist %>% unname
  end <- Sys.time()</pre>
  time <- difftime(end,start)</pre>
  error <- (EX - analytical) %>% abs
  return(c(n,EX,analytical,error,time,"MCser4"))
}
data.table(t(MCser4(n))) %>% setNames(header)
                   computational
                                         analytical
## 1: 10000000 1.87330731982586 1.87296355073463 0.00034376909123246
               walltime
                           type
## 1: 1.88429856300354 MCser4
```

Parallel implementations

Let's try different parallel implementations. First let's start with package parallel.

```
MCpar1 <- function(n){</pre>
  start <- Sys.time()</pre>
  # Calculate the number of cores
  no_cores <- detectCores()</pre>
  # Initiate cluster
  cl <- makeCluster(no_cores)</pre>
  intermean <- parSapply(cl, rep(n/no_cores,no_cores),function(ni,f){</pre>
      EX <- mean(f(runif(ni,0,1)))</pre>
    },f
  on.exit(stopCluster(cl))
  EX <- mean(intermean)
  end <- Sys.time()</pre>
  time <- difftime(end,start)</pre>
  error <- (EX - analytical) %>% abs
  return(c(n,EX,analytical,error,time,"MCpar1"))
data.table(t(MCpar1(n))) %>% setNames(header)
                                          analytical
              n
                    computational
## 1: 10000000 1.87339102185438 1.87296355073463 0.000427471119751388
               walltime
                           type
## 1: 1.32567048072815 MCpar1
Now let's try approach analogical to MCser2.
MCpar2 <- function(n){</pre>
  start <- Sys.time()</pre>
  # Calculate the number of cores
  no cores <- detectCores()</pre>
  cl <- makeCluster(no_cores)</pre>
  dt <- matrix(runif(n,0,1),ncol = no_cores)</pre>
  intermean <- parSapply(cl, 1:no_cores,function(i,f,dt){</pre>
      EX <- mean(f(dt[,i]))</pre>
    },f,dt
  on.exit(stopCluster(cl))
  EX <- mean(intermean)</pre>
  end <- Sys.time()</pre>
  error <- (EX - analytical) %>% abs
  time <- difftime(end,start)</pre>
  return(c(n,EX,analytical,error,time,"MCpar2"))
data.table(t(MCpar2(n))) %>% setNames(header)
                   computational
                                          analytical
              n
## 1: 10000000 1.87304020083651 1.87296355073463 0.000076650101882958
               walltime
## 1: 4.93123769760132 MCpar2
This approach was not very good. But let's have one more try at analogical solution to MCser2.
MCpar2_2 <- function(n,ncols=1000){</pre>
  start <- Sys.time()</pre>
  # Calculate the number of cores
  no_cores <- detectCores()</pre>
```

```
cl <- makeCluster(no_cores)</pre>
  dt <- matrix(runif(n,0,1),ncol = ncols)</pre>
  intermean <- parSapply(cl, 1:ncols,function(i,f,dt){</pre>
      EX <- mean(f(dt[,i]))</pre>
    },f,dt
  on.exit(stopCluster(cl))
  EX <- mean(intermean)</pre>
  end <- Sys.time()</pre>
  error <- (EX - analytical) %>% abs
  time <- difftime(end,start)</pre>
  return(c(n,EX,analytical,error,time,"MCpar2_2"))
data.table(t(MCpar2_2(n))) %>% setNames(header)
##
                   computational
                                         analytical
                                                                      error
## 1: 10000000 1.87279591153091 1.87296355073463 0.000167639203717762
               walltime
                             type
## 1: 4.82105684280396 MCpar2_2
This solution was bit better, but still worse than the previous examples.
Let's try the package foreach now.
MCpar3 <- function(n){</pre>
  start <- Sys.time()</pre>
  # Calculate the number of cores
  no_cores <- detectCores()</pre>
  # Initiate cluster
  cl<-makeCluster(no cores)</pre>
  # registerDoParallel(cl)
  EX <- foreach(ni = rep(n/no_cores,no_cores),.combine=mean,.export="f") %dopar%
    mean(f(runif(ni,0,1)))
  on.exit(stopCluster(cl))
  # stopImplicitCluster()
  end <- Sys.time()</pre>
  time <- difftime(end,start)</pre>
  error <- (EX - analytical) %>% abs
  return(c(n,EX,analytical,error,time,"MCpar3"))
data.table(t(MCpar3(n))) %>% setNames(header)
## Warning: executing %dopar% sequentially: no parallel backend registered
##
                   computational
                                         analytical
                                                                      error
## 1: 10000000 1.87332913732254 1.87296355073463 0.000365586587907529
               walltime
```

Benchmarking

1: 2.03123497962952 MCpar3

Now, let's visualize the walltimes of implemented solutions.

```
iterations <- c(1,2.5,5,7.5)*10**(7)#(5:7)
funs <- c(
    MCser1,MCser2,MCser3,MCser4,</pre>
```

```
MCpar1,MCpar3 #MCpar2,MCpar2_2,
)
data <- sapply(funs,function(f,iterations){</pre>
 sapply(iterations, function(n){
   f(n)
 })
},iterations) %>%
 matrix(ncol=6,byrow=T) %>%
 data.table %>%
 setNames(header) %>%
 mutate_at(header[-grep(x=header,pattern="type")],as.numeric)
data
##
             n computational analytical
                                                error
                                                       walltime
##
   1: 10000000
                    1.873144
                               1.872964 0.00018006442
                                                       1.679950 MCser1
##
   2: 25000000
                    1.872934
                               1.872964 0.00002993648 4.520063 MCser1
## 3: 50000000
                    1.872776    1.872964    0.00018749121    9.524911 MCser1
## 4: 75000000
                               1.872964 0.00007335057 14.163665 MCser1
                    1.873037
## 5: 10000000
                    1.873000
                               1.872964 0.00003679440
                                                      1.872934 MCser2
## 6: 25000000
                    1.873036
                              1.872964 0.00007210419 4.387838 MCser2
## 7: 5000000
                             1.872964 0.00002604306 8.864731 MCser2
                    1.872938
## 8: 75000000
                               1.872964 0.00003098338 12.007296 MCser2
                    1.872995
                              1.872964 0.00026519163 1.755220 MCser3
## 9: 10000000
                    1.872698
## 10: 25000000
                    1.872981
                               1.872964 0.00001748658 4.360301 MCser3
## 11: 50000000
                    1.872957
                               1.872964 0.00000608254 9.454168 MCser3
## 12: 75000000
                               1.872964 0.00006552740 13.830856 MCser3
                    1.872898
## 13: 10000000
                    1.873285
                              1.872964 0.00032096333 2.406975 MCser4
## 14: 25000000
                    1.872999
                              1.872964 0.00003529201 4.818219 MCser4
## 15: 50000000
                    1.872987
                               1.872964 0.00002313410 9.413631 MCser4
## 16: 75000000
                    1.872992
                               1.872964 0.00002803494 12.982518 MCser4
## 17: 10000000
                    1.872892
                               1.872964 0.00007109093 1.288364 MCpar1
## 18: 25000000
                    ## 19: 50000000
                    1.872944
                               1.872964 0.00001965172 4.578090 MCpar1
## 20: 75000000
                    1.872952
                               1.872964 0.00001173007
                                                      6.752777 MCpar1
                    1.872822
## 21: 10000000
                              1.872964 0.00014118409 2.141526 MCpar3
## 22: 25000000
                    1.873535
                              1.872964 0.00057168676 4.074641 MCpar3
## 23: 50000000
                    1.872938
                               1.872964 0.00002530814 7.826763 MCpar3
## 24: 75000000
                    1.872941
                               1.872964 0.00002210452 11.566591 MCpar3
             n computational analytical
                                                error walltime
ggplot(data=data,aes(x=n,y=walltime,group=type,color=type)) +
 geom_point() +
 geom_line() +
 labs(
      title="Serial vs parallel implementations",
      x="Nr of iterations",
      y="Walltime (sec)"
 theme(
       plot.title = element_text(hjust = 0.5),
       plot.subtitle = element_text(hjust = 0.5)
 guides(color=guide_legend(title="Function"))
```

Serial vs parallel implementations

